

Reionization + Galaxy Formation; First Stars; 21-cm Cosmology

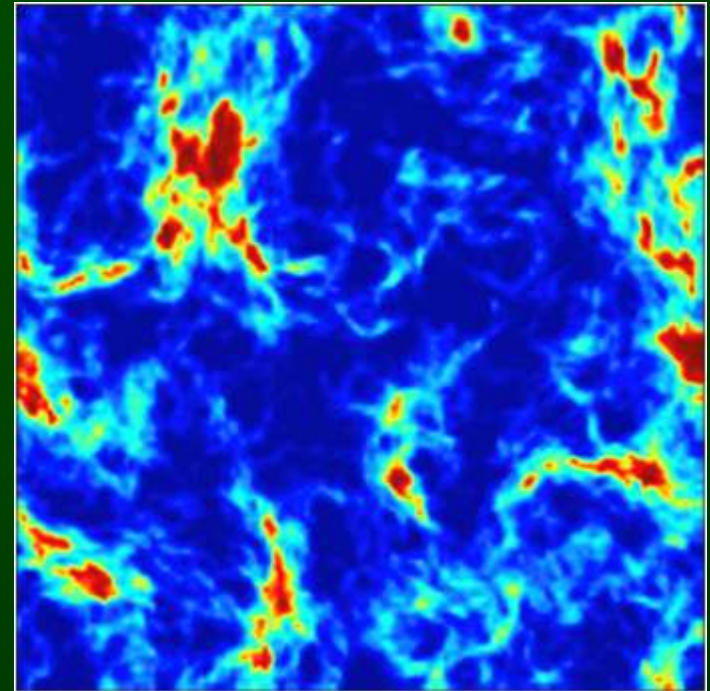
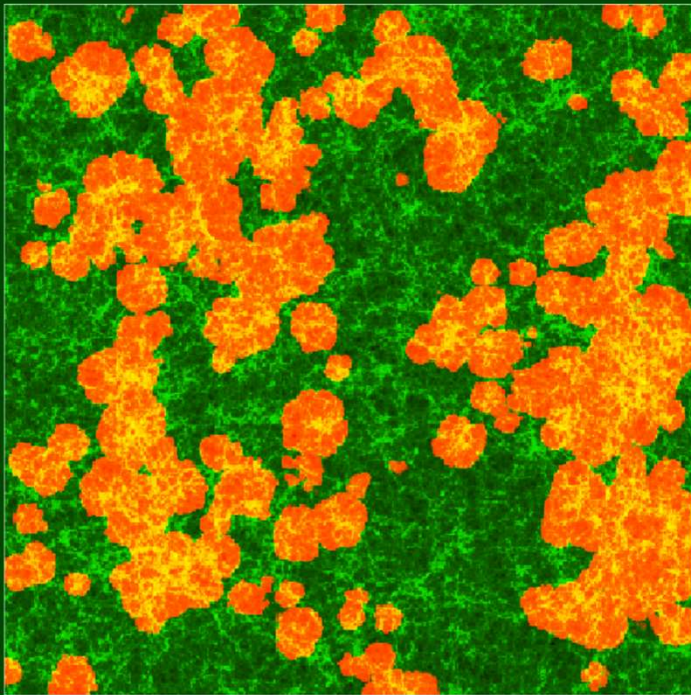
Rennan Barkana

רנן ברקנא

TEL AVIV UNIVERSITY



אוניברסיטת תל-אביב



Cosmology

Robertson-Walker metric:

(R, θ, ϕ)

Scale factor:

$a(t)$

$$ds^2 = dt^2 - a^2(t) \left[\frac{dR^2}{1 - kR^2} + R^2 (d\theta^2 + \sin^2 \theta d\phi^2) \right]$$

Friedmann equation:

$$H^2(t) = \frac{8\pi G}{3} \rho - \frac{k}{a^2}$$

$$H(t) = d \ln a(t) / dt$$

Energy conservation:

$$d(\rho a^3) = -p d(a^3)$$

Critical density:

$$\rho_c(t) \equiv \frac{3H^2(t)}{8\pi G}$$

$$\Omega \equiv \frac{\rho}{\rho_c}$$

Friedmann equation:

$$\frac{H(t)}{H_0} = \left[\frac{\Omega_m}{a^3} + \Omega_\Lambda + \frac{\Omega_r}{a^4} + \frac{\Omega_k}{a^2} \right]^{1/2}$$

$$\Omega_0 = \Omega_m + \Omega_\Lambda + \Omega_r$$

$$\Omega_k \equiv -\frac{k}{H_0^2} = 1 - \Omega_0$$

Cosmology

$$\frac{H(t)}{H_0} = \left[\frac{\Omega_m}{a^3} + \Omega_\Lambda + \frac{\Omega_r}{a^4} + \frac{\Omega_k}{a^2} \right]^{1/2}$$

Einstein-de Sitter (EdS) model ($\Omega_m = 1, \Omega_\Lambda = \Omega_r = \Omega_k = 0$)

High z (first stars):

$$H(z) \approx H_0 \frac{\sqrt{\Omega_m}}{a^{3/2}}$$

Planck 2018:

$$h=0.677, \Omega_m=0.311, \Omega_b=0.0490$$

$$H_0 = 100 h \text{ km s}^{-1} \text{ Mpc}^{-1}$$

Redshift:

$$a = \frac{1}{1+z}$$

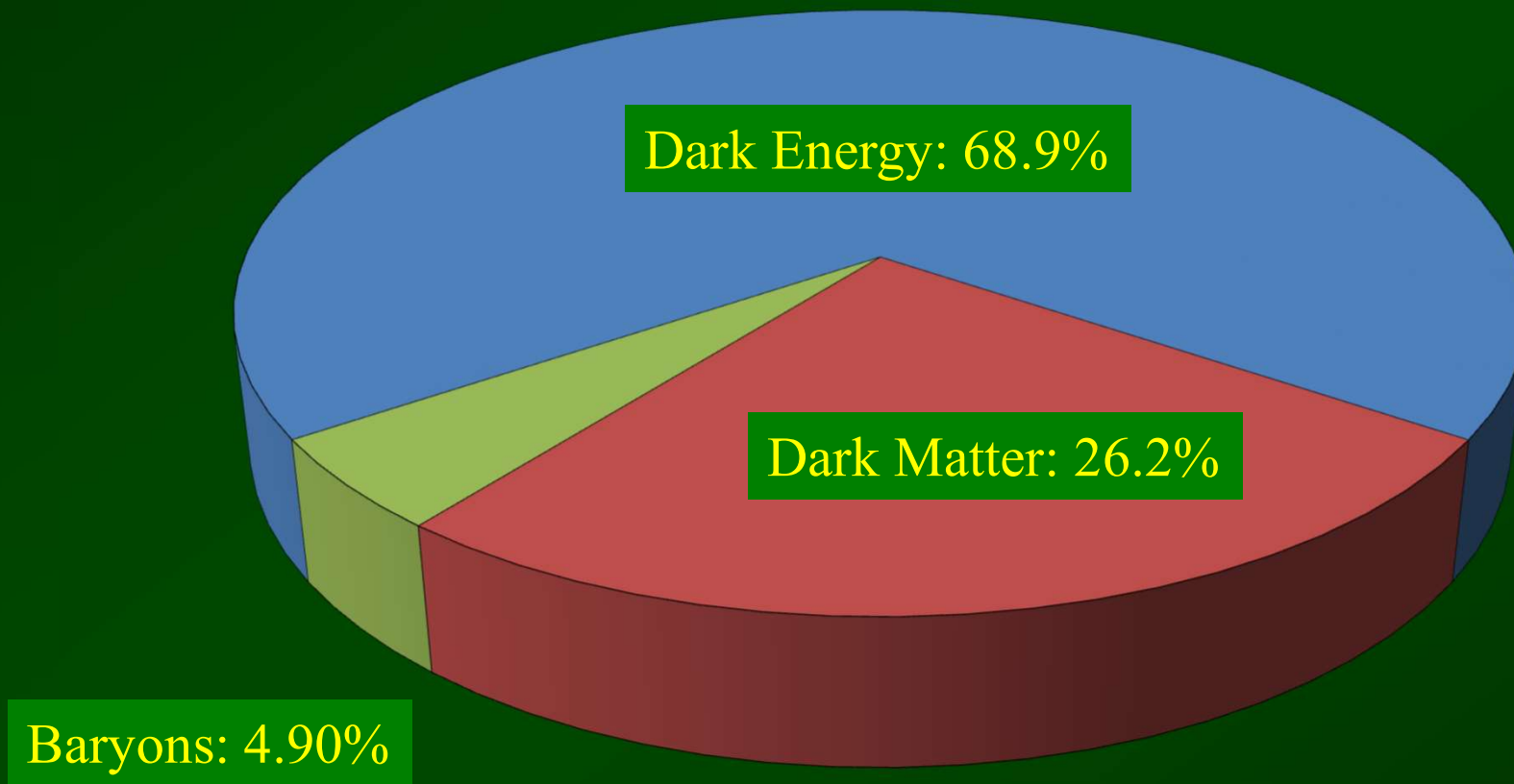
Hubble expansion:

$$v = Hr$$

Cosmic age:

$$t \approx \frac{2}{3 H_0 \sqrt{\Omega_m}} (1+z)^{-3/2} = 5.49 \times 10^8 \left(\frac{\Omega_m h^2}{0.141} \right)^{-1/2} \left(\frac{1+z}{10} \right)^{-3/2} \text{ yr}$$

Cosmological Pie



Linear Perturbation Theory

Density perturbation:

$$\delta(\mathbf{x}) \equiv \frac{\rho(\mathbf{r})}{\bar{\rho}} - 1$$

$$\mathbf{x} = \mathbf{r}/a$$

Comoving coordinates

Peculiar velocity:

$$\mathbf{u} \equiv \mathbf{v} - H\mathbf{r}$$

Linearized fluid eq's =>

$$\frac{\partial^2 \delta}{\partial t^2} + 2H \frac{\partial \delta}{\partial t} = 4\pi G \bar{\rho} \delta$$

Growing mode:

$$D(a) = a \quad (\text{EdS})$$

$$D(a) \approx 1.28a \quad (\text{High } z)$$

$$D(z=0) = 1$$

Fourier space:

$$\delta_{\mathbf{k}} = \int d^3x \delta(\mathbf{x}) e^{-i\mathbf{k} \cdot \mathbf{x}}$$

$$k = \frac{2\pi}{\lambda}$$

Power spectrum:

$$\langle \delta_{\mathbf{k}} \delta_{\mathbf{k}'}^* \rangle = (2\pi)^3 P(k) \delta_D^{(3)}(\mathbf{k} - \mathbf{k}')$$

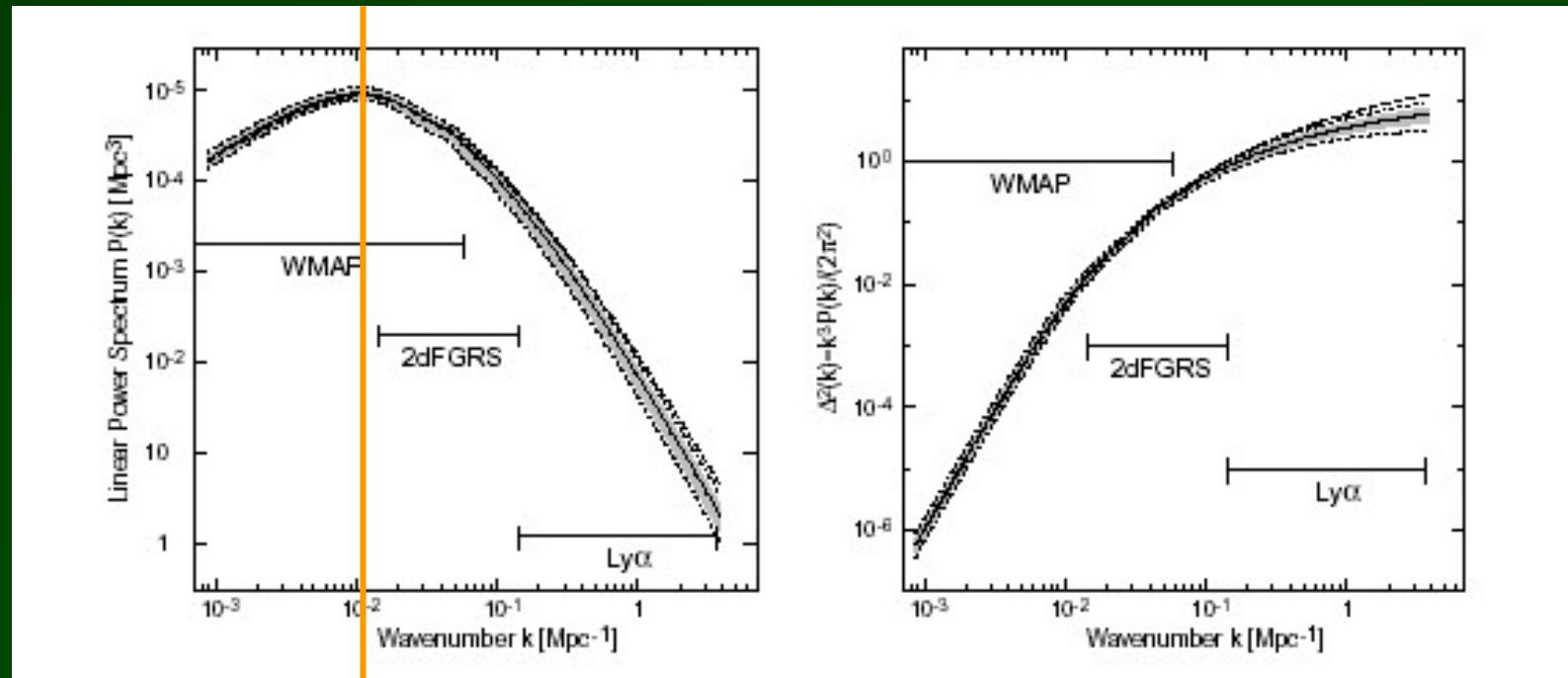
Linear Power Spectrum

Inflation: Gaussian random field

$$P(k) \propto k^n$$

$$n \sim 1$$

$$P(k) \propto k^{n-4}$$



horizon cH^{-1} at matter-radiation equality

$$\sigma^2 = \int_0^\infty \frac{dk}{2\pi^2} k^2 P(k)$$

Non-linear Collapse

Mass scale:

$$M = \frac{4}{3}\pi\bar{\rho}_0 R^3 = 1.64 \times 10^8 \left(\frac{\Omega_m h^2}{0.141} \right) \left(\frac{R}{100 \text{ kpc}} \right)^3 M_\odot$$

Variance:

$$j_1(x) = (\sin x - x \cos x)/x^2$$

$$S(M) = \sigma^2(M) = \sigma^2(R) = \int_0^\infty \frac{dk}{2\pi^2} k^2 P(k) \left[\frac{3j_1(kR)}{kR} \right]^2$$

$$\sigma_8 \equiv \sigma(R = 8h^{-1} \text{Mpc})$$

Spherical collapse:
(EdS)

$$\delta_{\text{crit}}(z) = \frac{1.686}{D(z)}$$

Virial density:

$$\Delta_c = 18\pi^2 \simeq 178$$

$$U = -2K$$

Circular velocity:

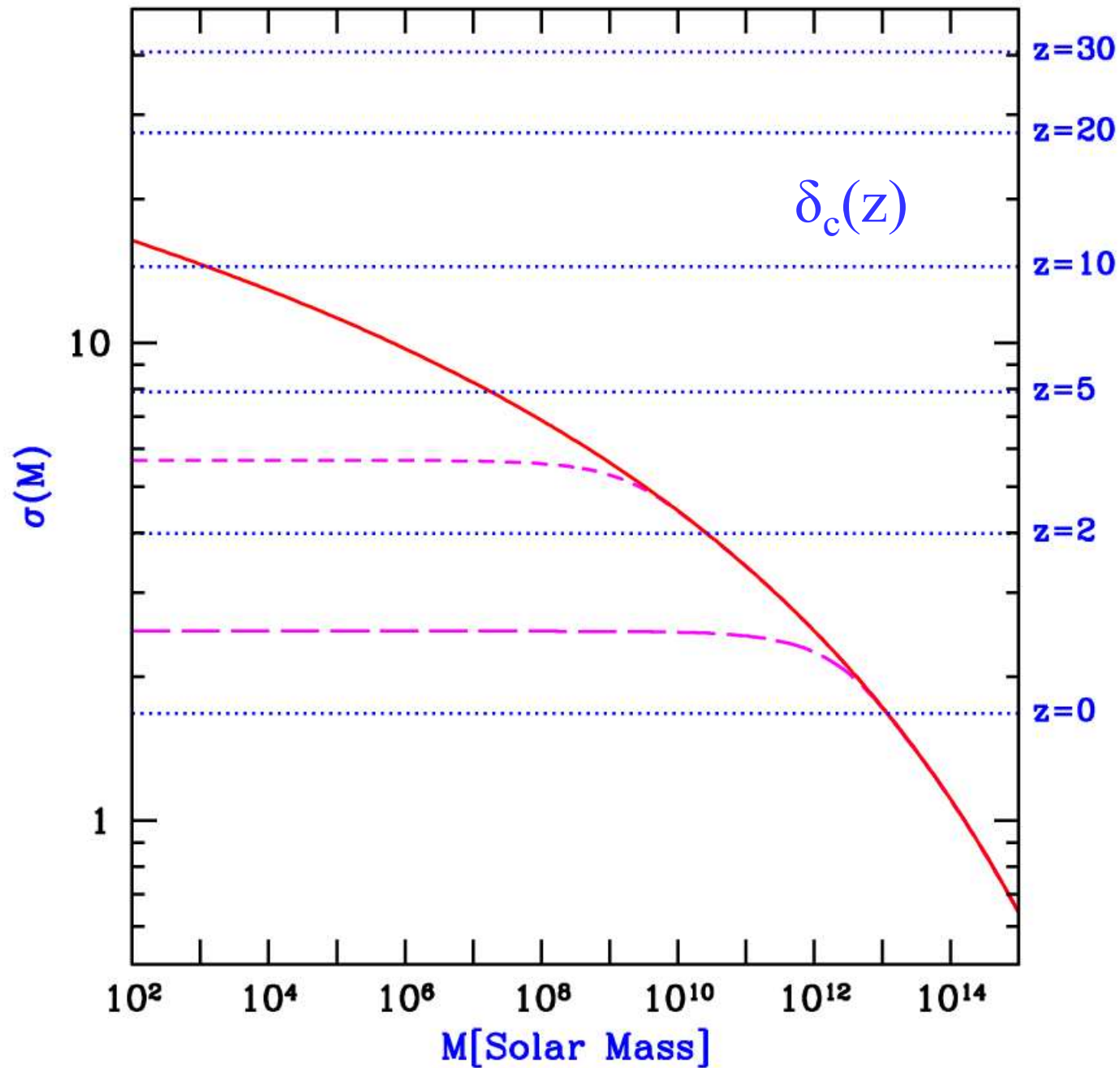
$$V_c = \left(\frac{GM}{r_{\text{vir}}} \right)^{1/2} = 16.9 \left(\frac{\Omega_m h^2}{0.141} \right)^{1/6} \left(\frac{M}{10^8 M_\odot} \right)^{1/3} \left(\frac{\Delta_c}{18\pi^2} \right)^{1/6} \left(\frac{1+z}{10} \right)^{1/2} \text{ km s}^{-1}$$

Virial temperature:

$$T_{\text{vir}} = \frac{\mu m_p V_c^2}{2k_B} = 1.03 \times 10^4 \left(\frac{\Omega_m h^2}{0.141} \right)^{1/3} \left(\frac{\mu}{0.6} \right) \left(\frac{M}{10^8 M_\odot} \right)^{2/3} \left(\frac{\Delta_c}{18\pi^2} \right)^{1/3} \left(\frac{1+z}{10} \right) \text{ K}$$

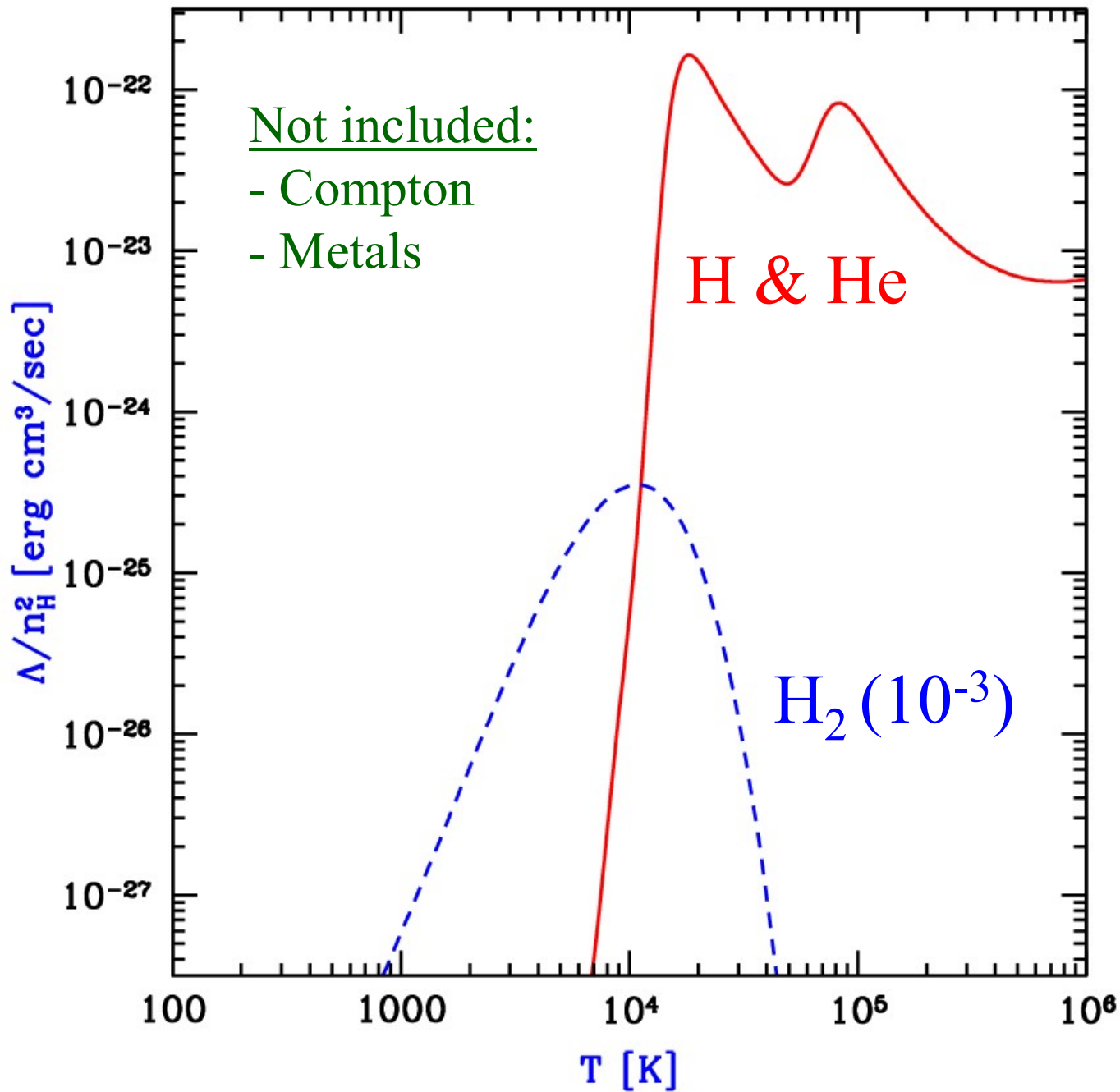
Mean molecular weight:

$$\mu = 1.22 \text{ (neutral), } 0.61 \text{ (ionized H), } 0.59 \text{ (fully ionized He)}$$



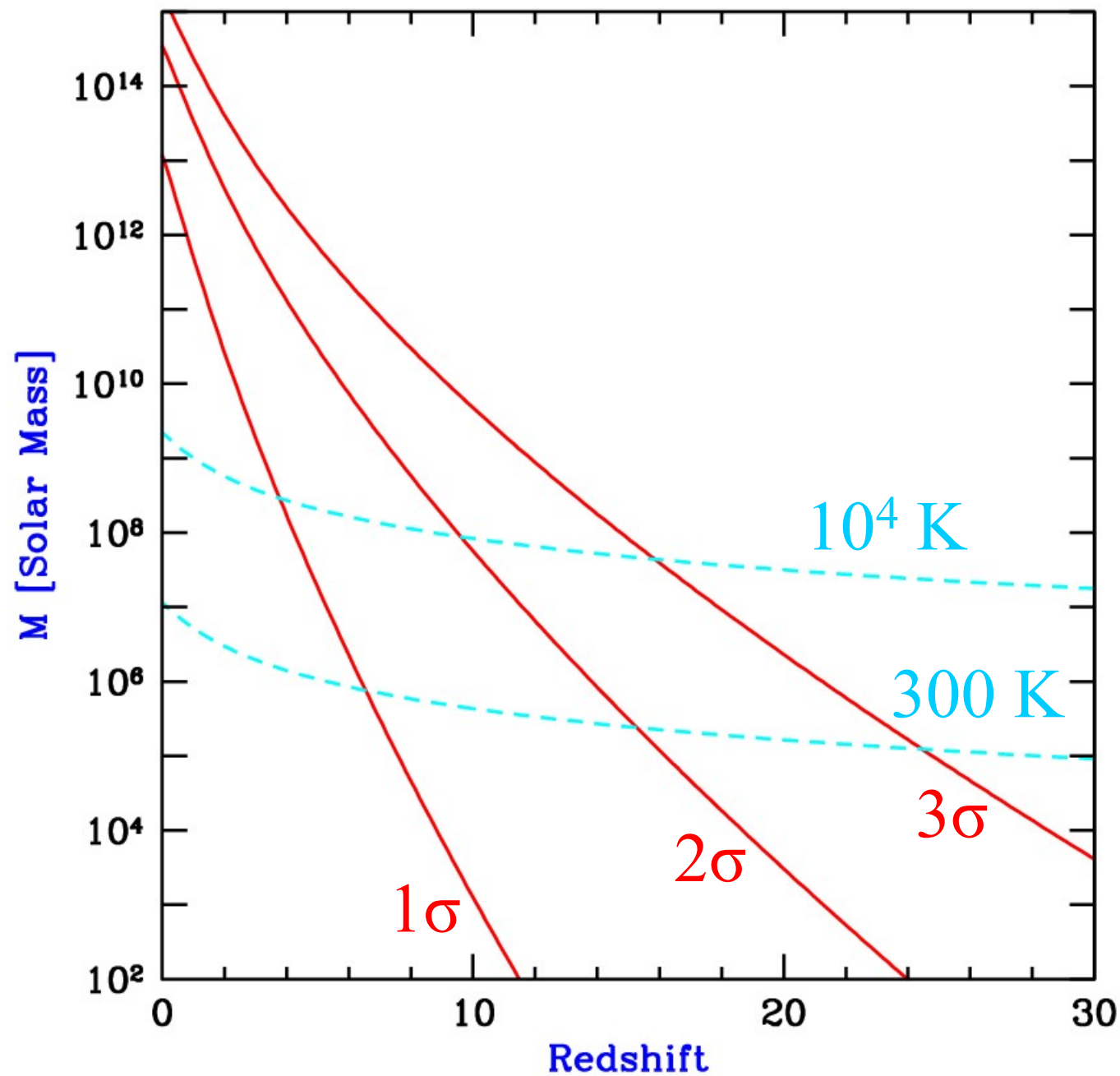
**Typical
fluctuations
compared
with the
critical value**

**Barkana
& Loeb
2001**



**Cooling
rate of a
primordial
cosmic gas**

**Barkana
& Loeb
2001**



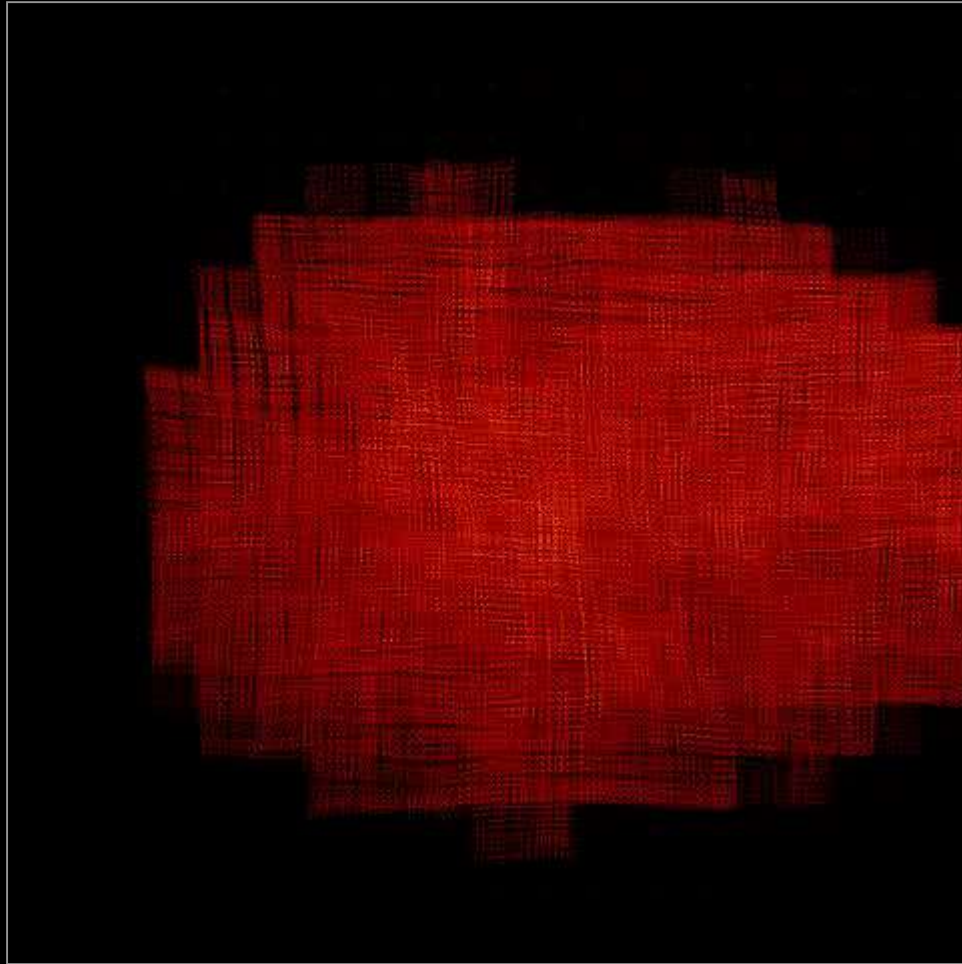
**Galactic
halos**

**Barkana
& Loeb
2001**

Hierarchical Galaxy Formation:

CDM

20 kpc box

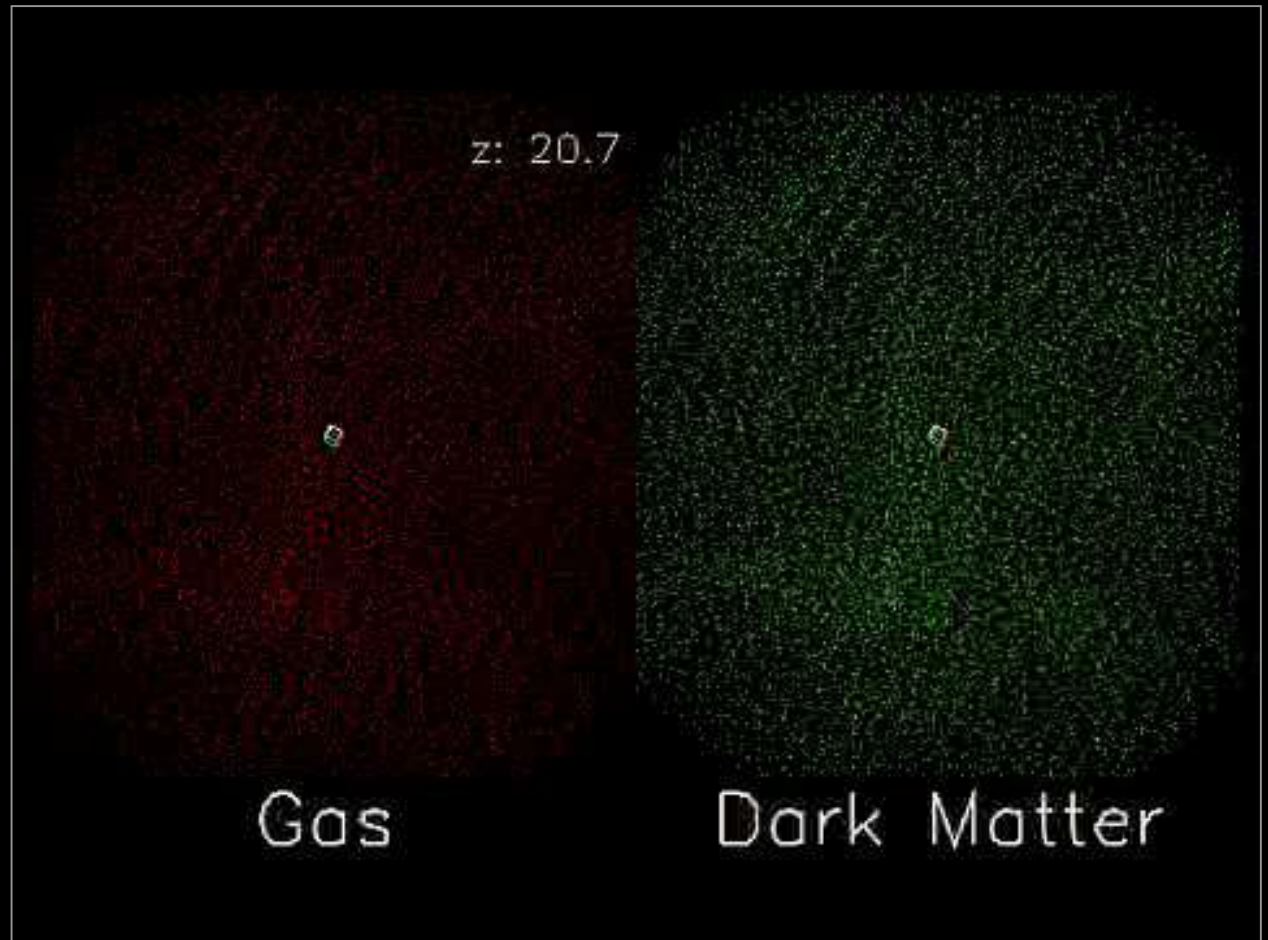


Credits: Matthias Steinmetz

<http://www.aip.de/People/MSteinmetz/E/movies.html>

Hierarchical Galaxy Formation:

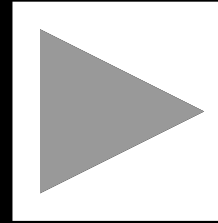
CDM



Credits: Matthias Steinmetz

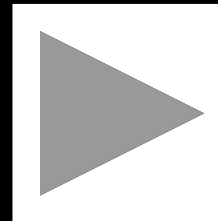
<http://www.aip.de/People/MSteinmetz/E/movies.html>

The universe today:



<http://www.mpa-garching.mpg.de/galform/millennium/>

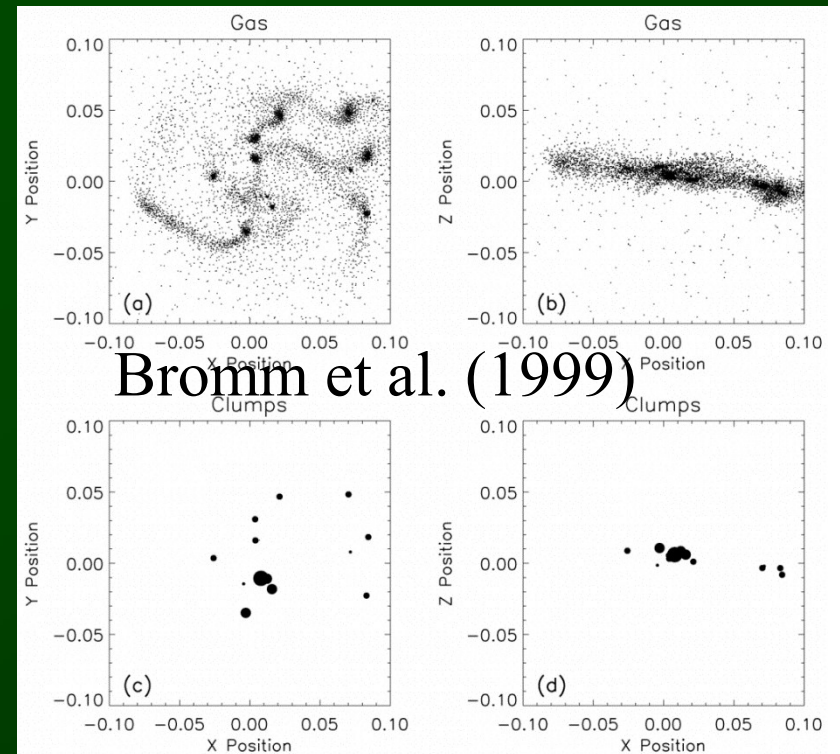
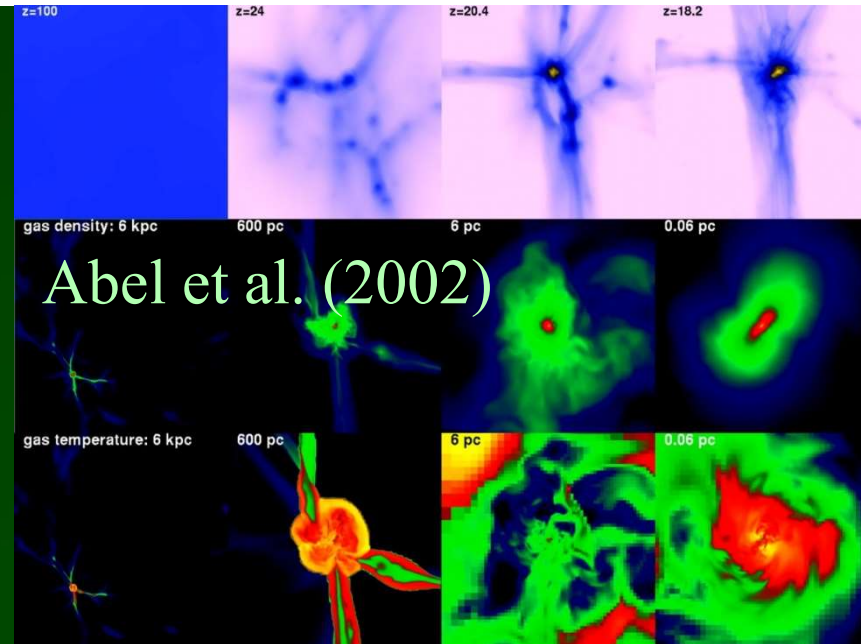
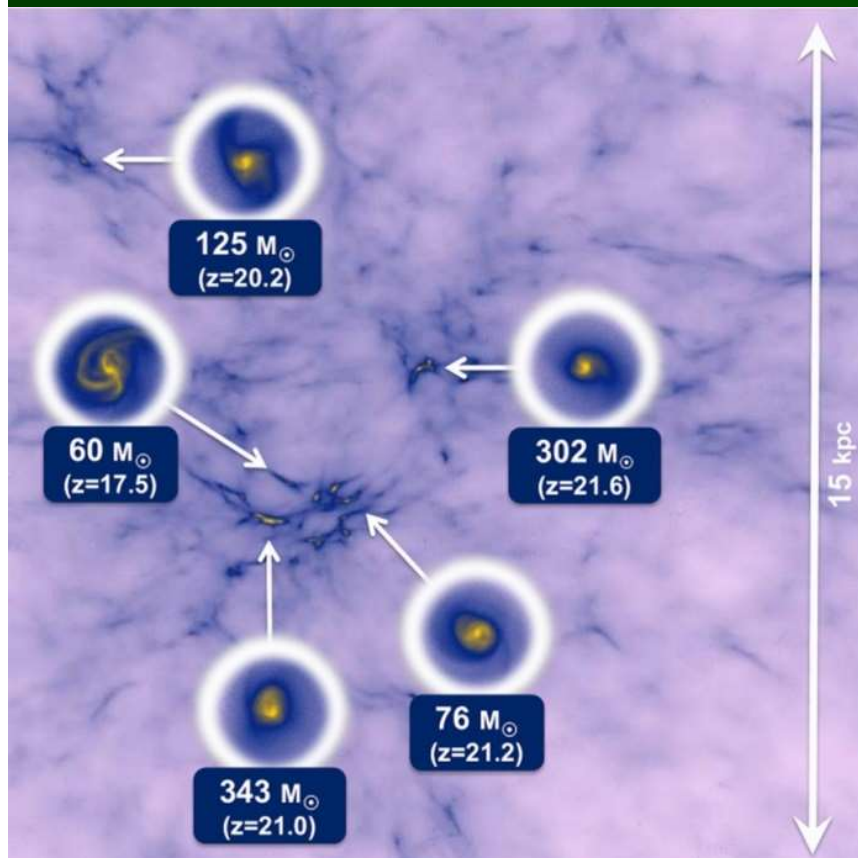
Formation of a
galaxy cluster:



http://www.mpa-garching.mpg.de/galform/data_vis/

The First Star (simulations)

Hirano et al. (2014)



Strong Clustering of Early Galaxies

Extended Press-Schechter
Peak-Background Split

Press & Schechter 1974

Bardeen, Bond,

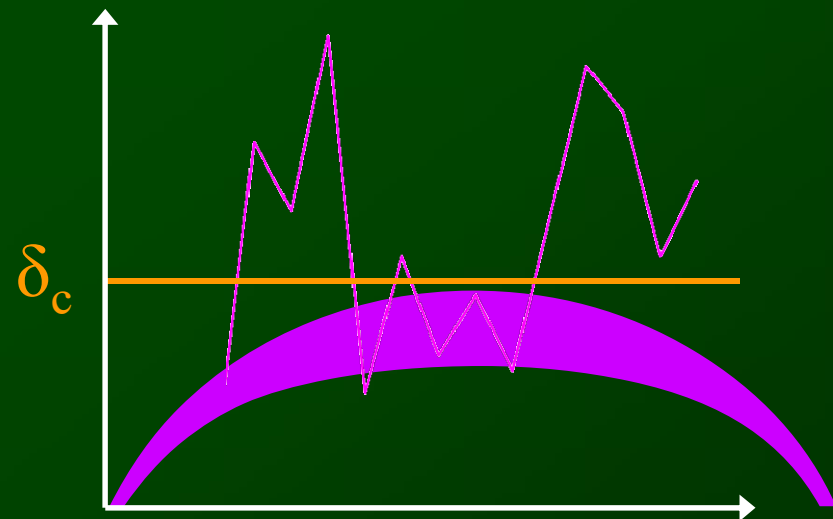
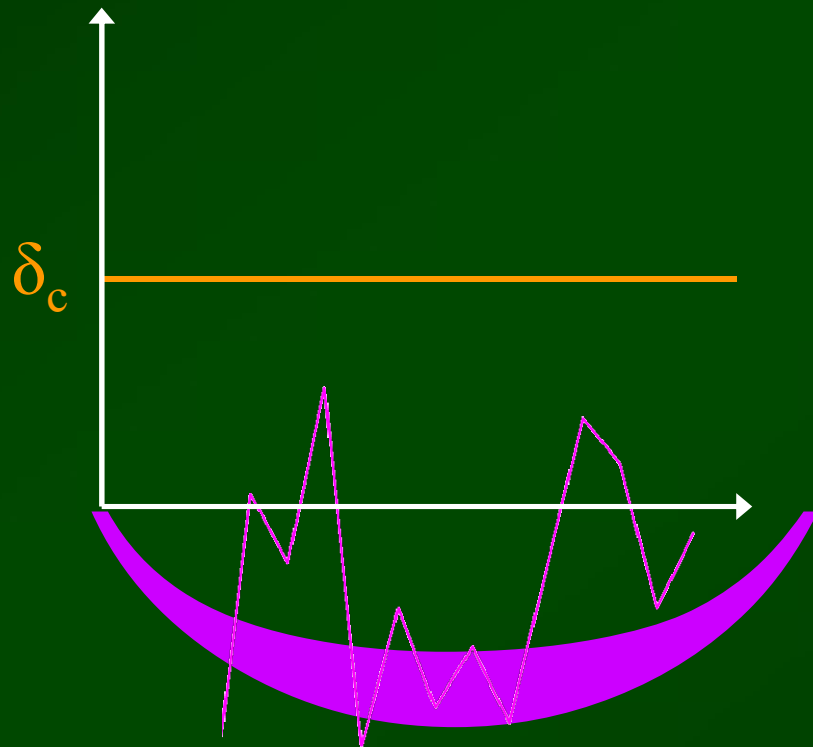
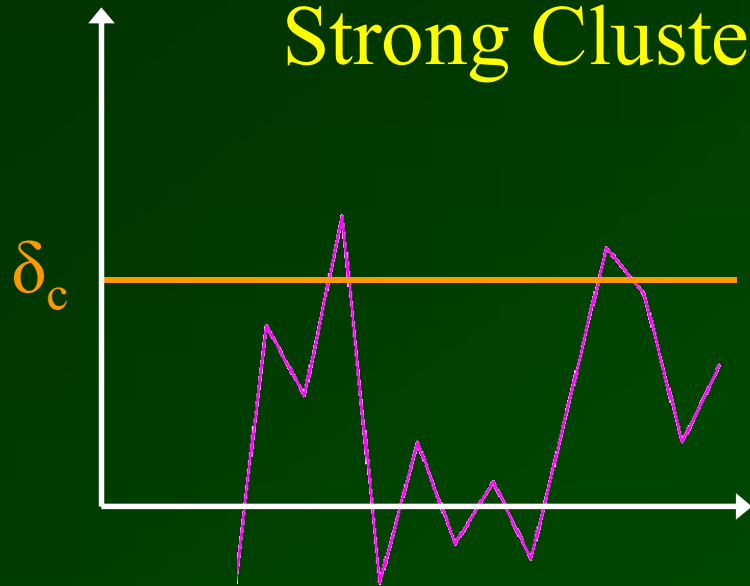
Kaiser, & Szalay 1986

Kaiser 1984

Bond, Cole, Efstathiou, & Kaiser 1991

Cole & Kaiser 1989

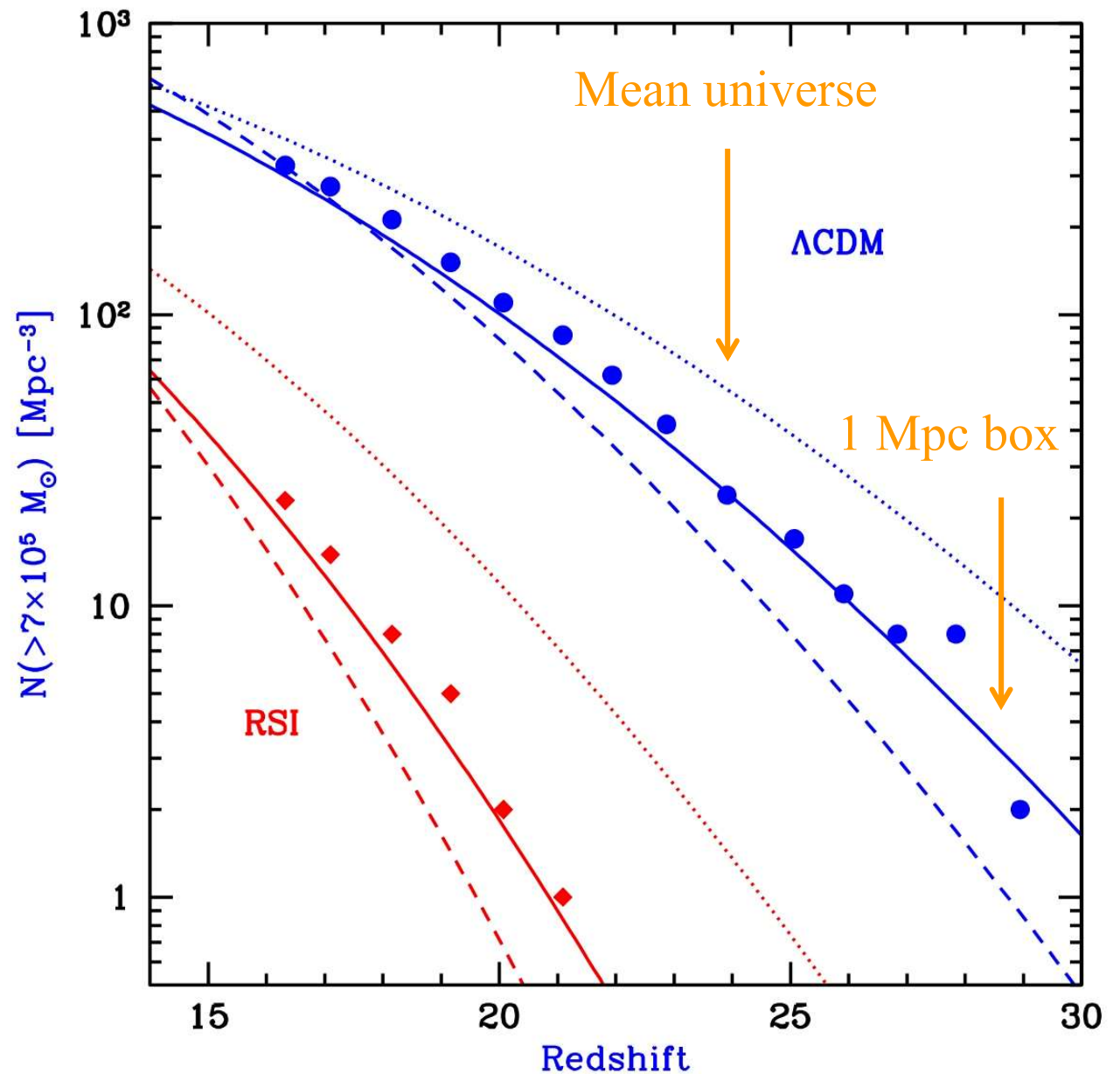
Mo & White 1996



The First Star (theory)

Simulations:
Yoshida et al. (2003)

RB & Loeb (2004)



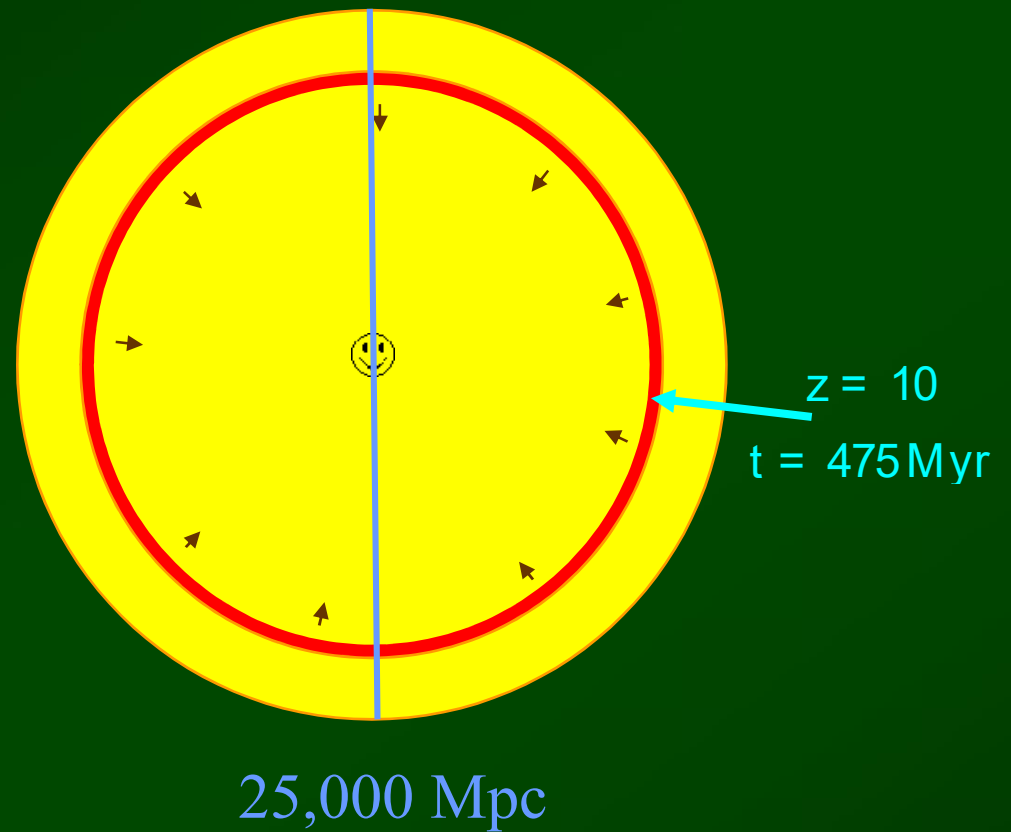
The First Star (theory)

Naoz, Noter, & RB (2006)

$z \sim 65$ ($t \sim 30$ Myr)

Compare:

$z \sim 30$ ($t \sim 100$ Myr)



Small galaxies

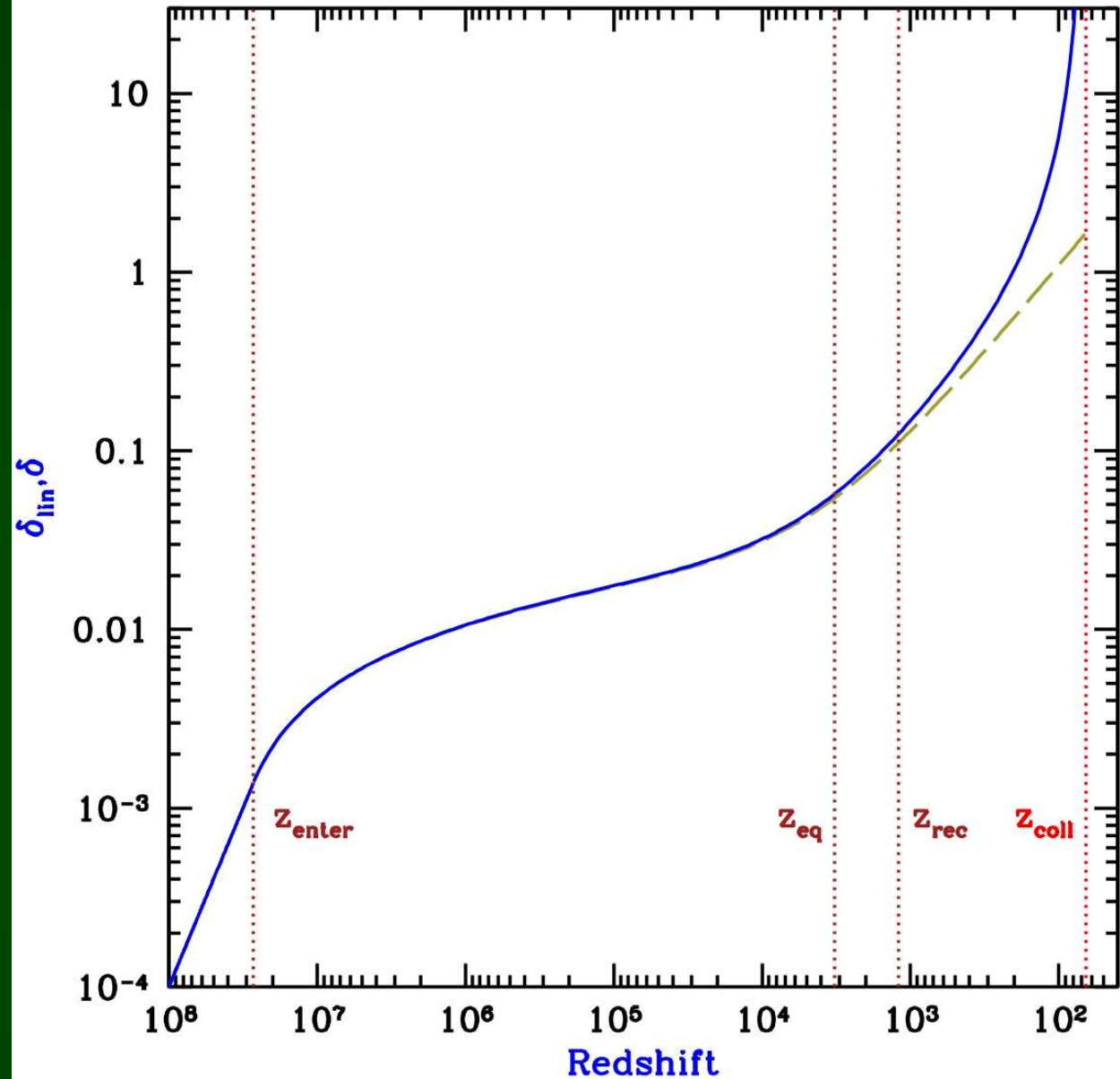


Large scales

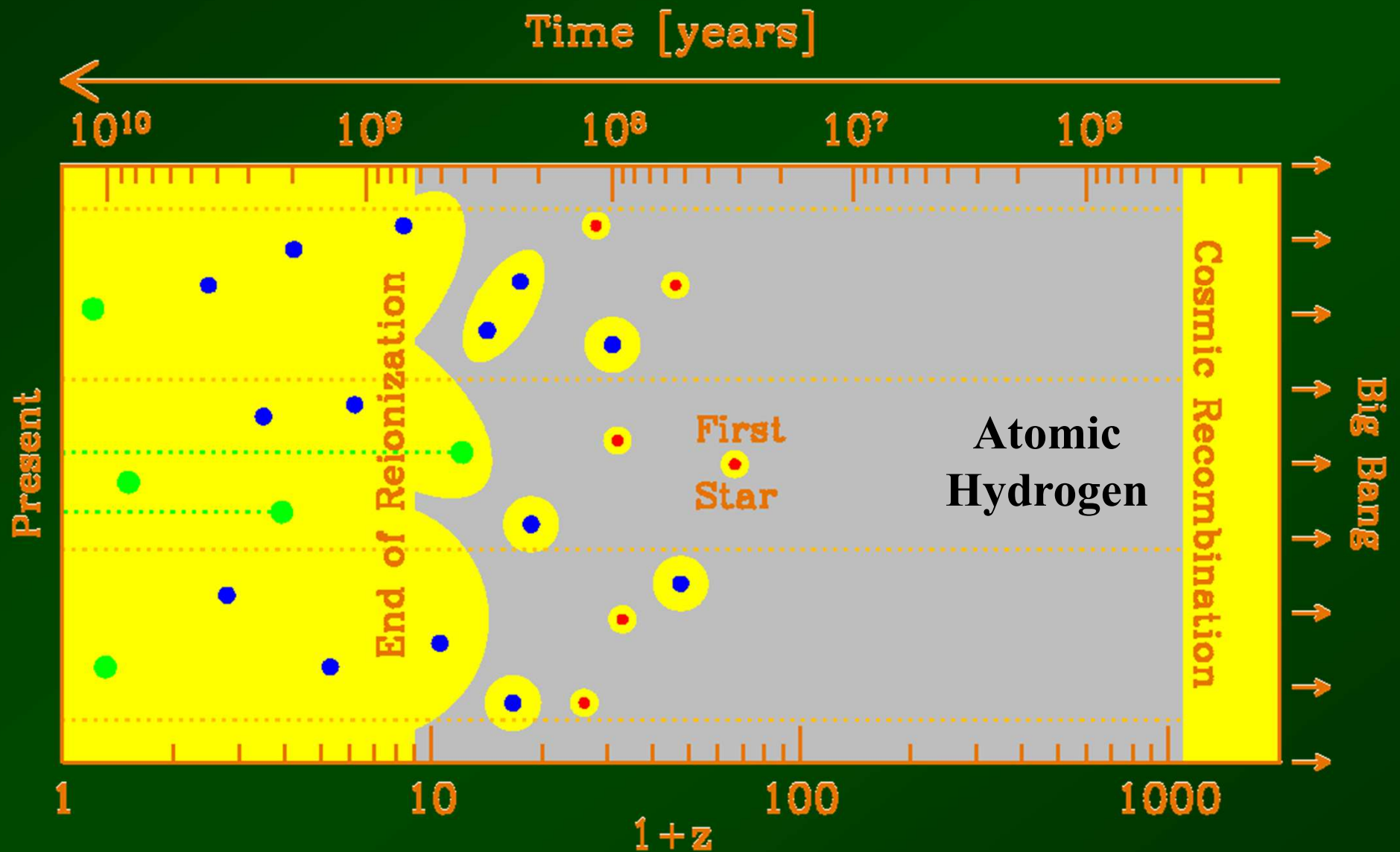
The First Star (theory)

The second
star: feedback

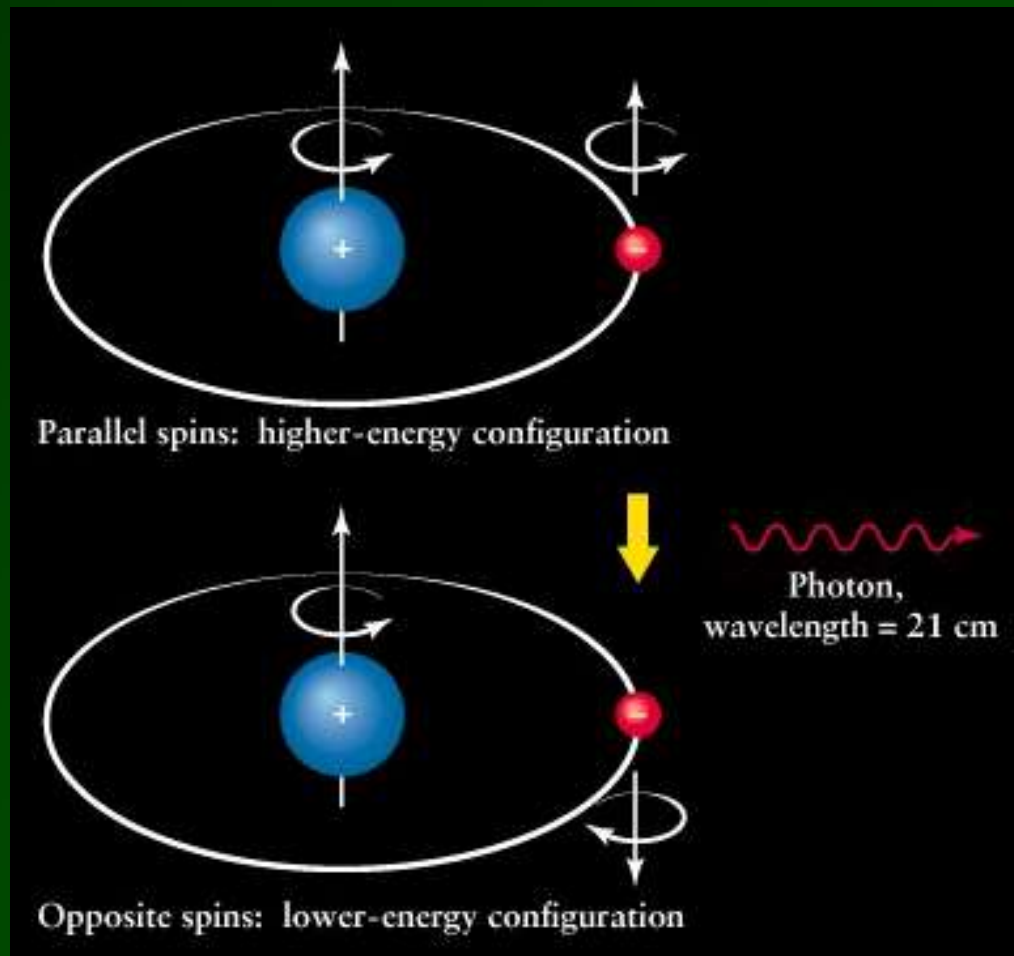
Naoz, Noter,
& RB (2006)



Cosmic History



21-cm Cosmology: The Spin Temperature



$$\lambda = 21 \text{ cm}$$

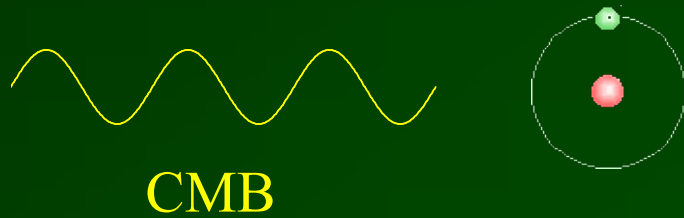
$$\nu = 1420 \text{ MHz}$$

$$E = 5.9 \times 10^{-6} \text{ eV}$$

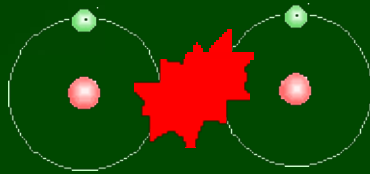
$$\frac{E}{k_B} = T_* = 0.068 \text{ K}$$

$$\frac{n_1}{n_0} = 3 \exp\left\{-\frac{T_*}{T_S}\right\}$$

What determines T_S ?

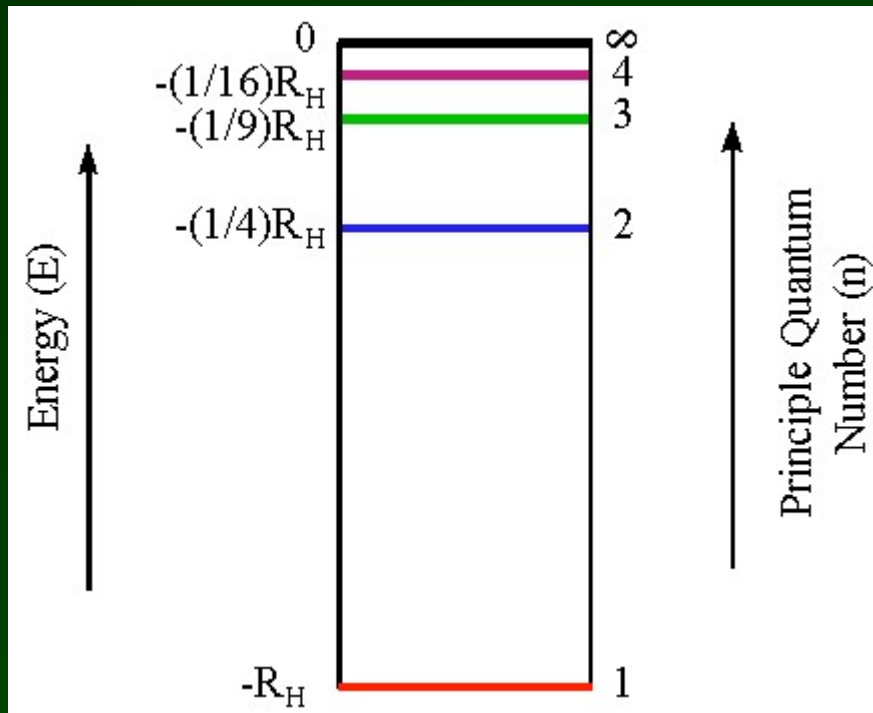


$$T_S \rightarrow T_{\text{CMB}}$$



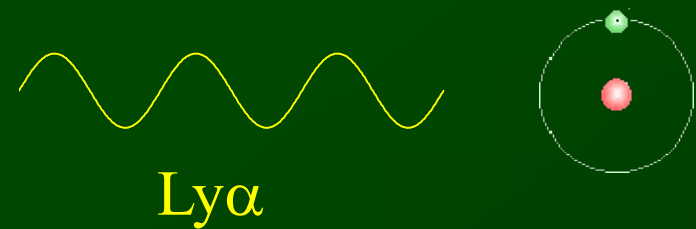
$$T_S \rightarrow T_{\text{gas}}$$

What determines T_S ?

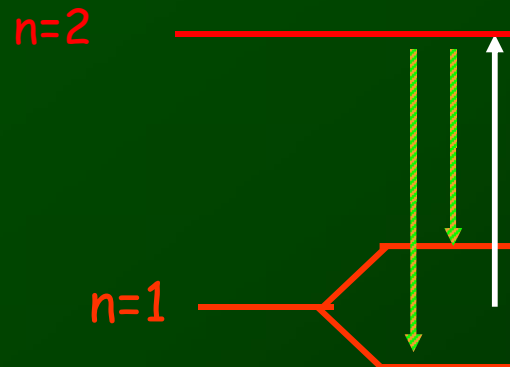


Ly-Limit: 13.6 eV

Ly α : $\frac{3}{4}$ LL = 10.2 eV

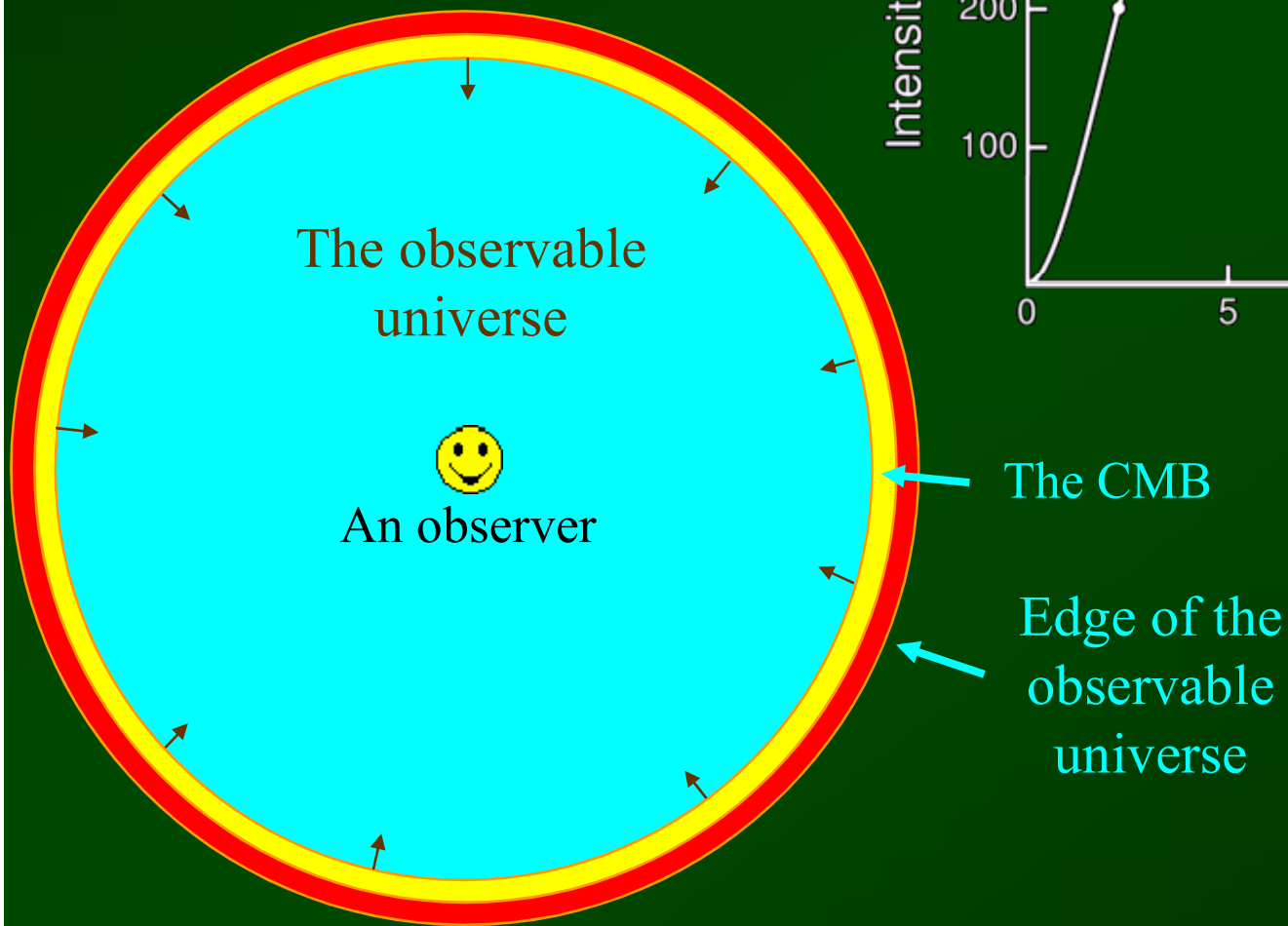
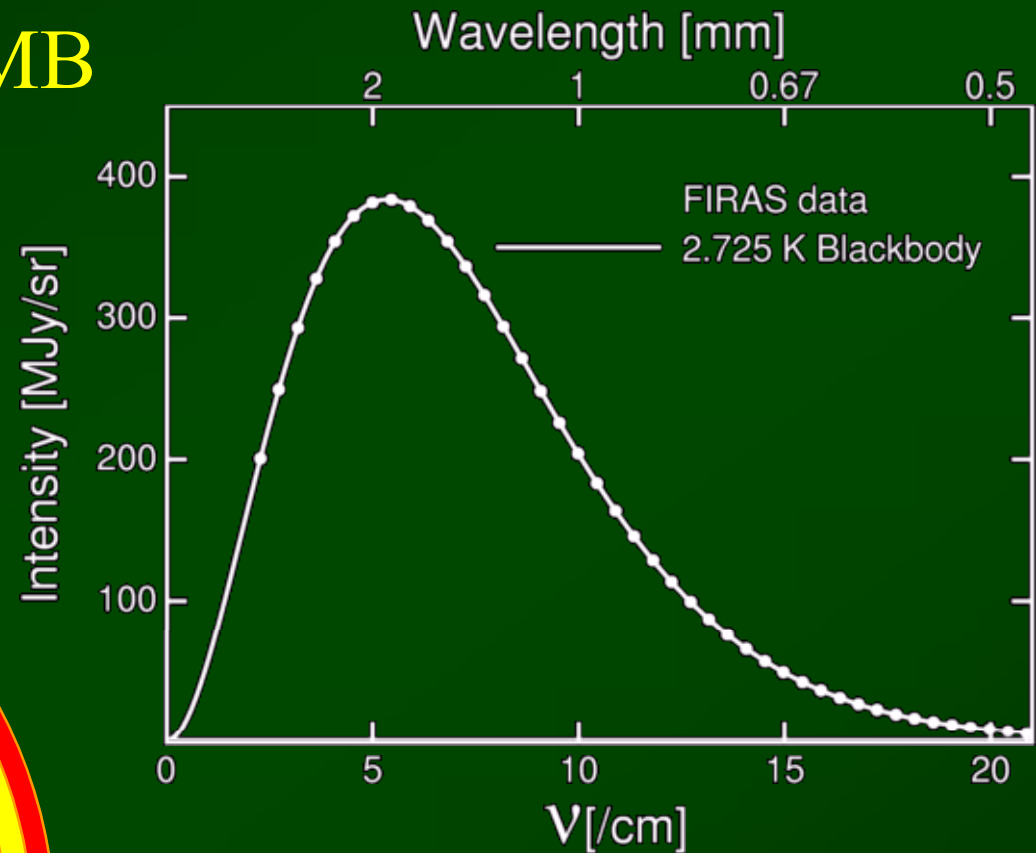


Wouthuysen 1952
Field 1958



$$T_S \rightarrow T_{\text{gas}}$$

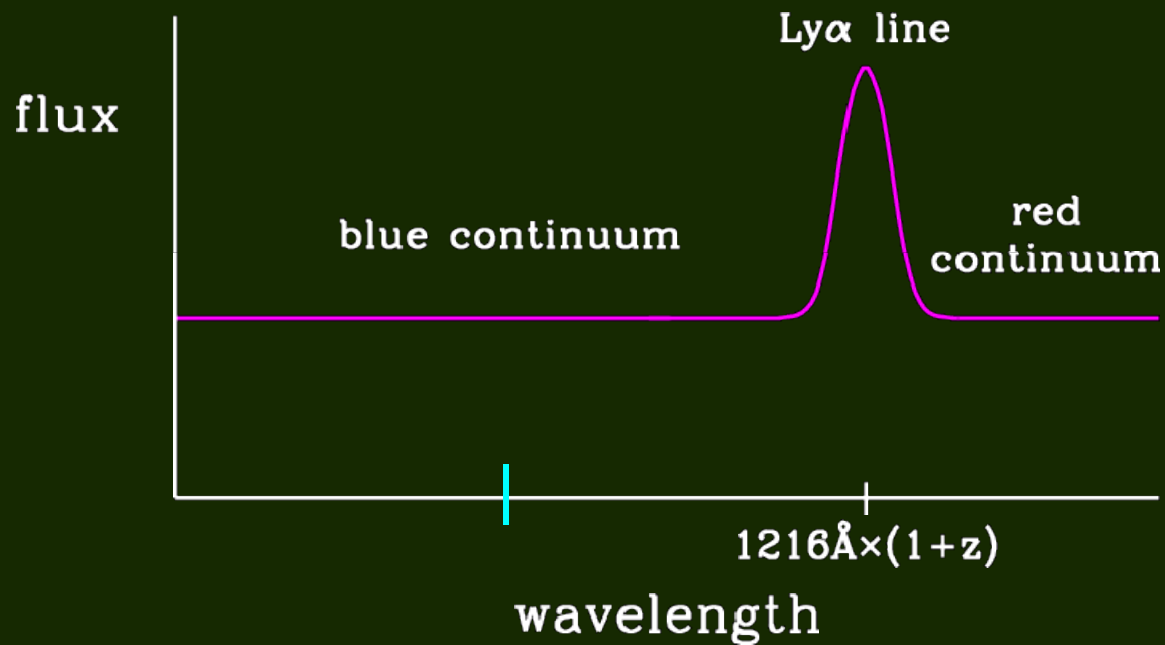
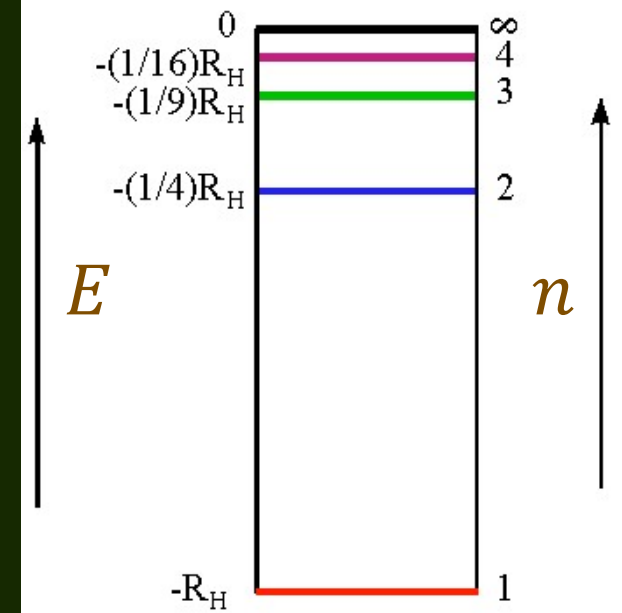
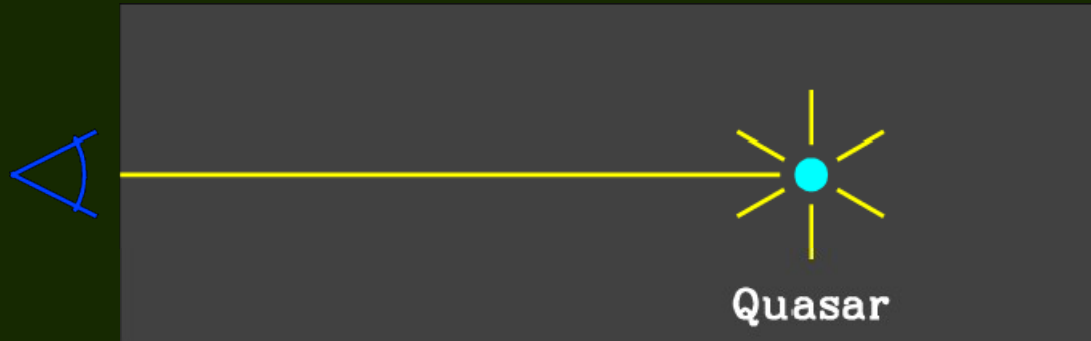
Diffuse Source: The CMB



$$h\nu \ll k_B T$$

$$I_\nu = 2k_B T \nu^2 / c^2$$

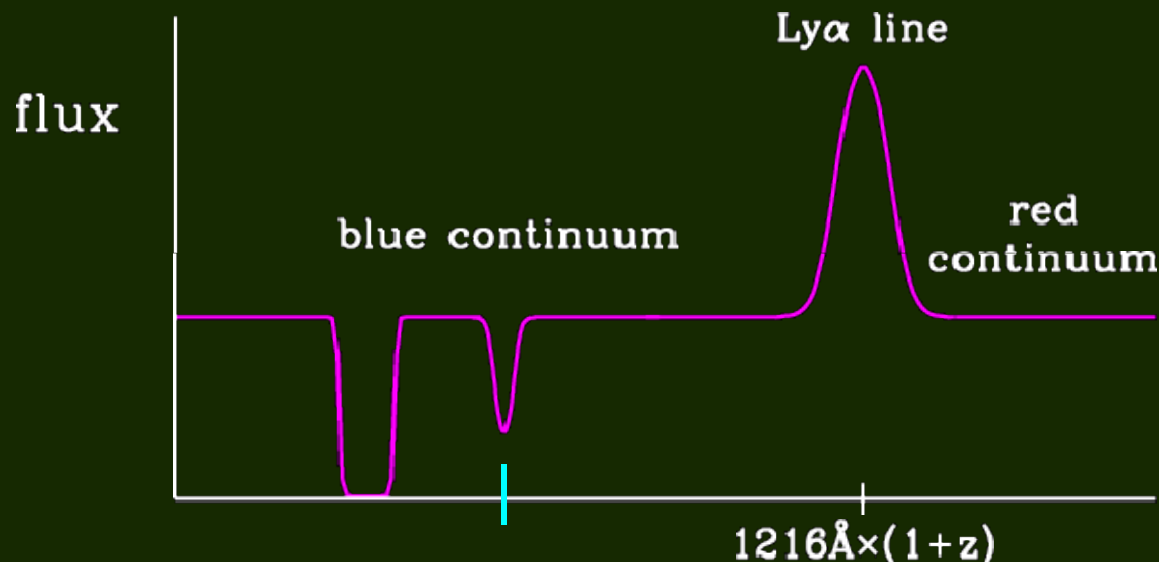
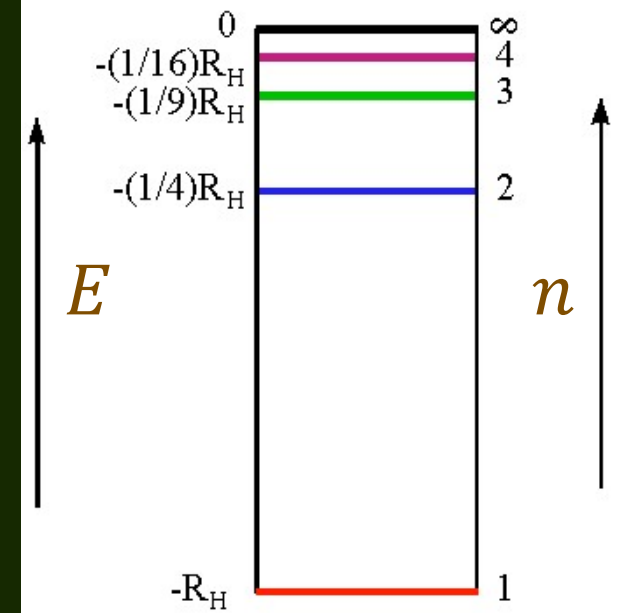
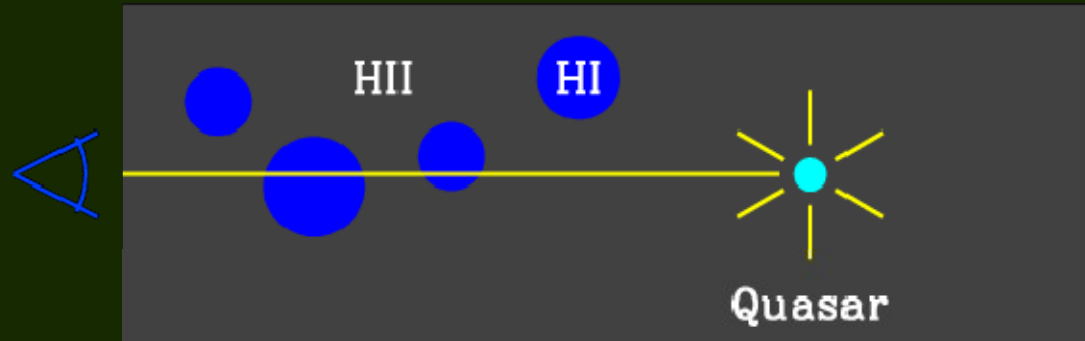
Ly α Spectra:



Resonance Line +
Cosmological Redshift

$$1100\text{\AA} \times (1+z)$$

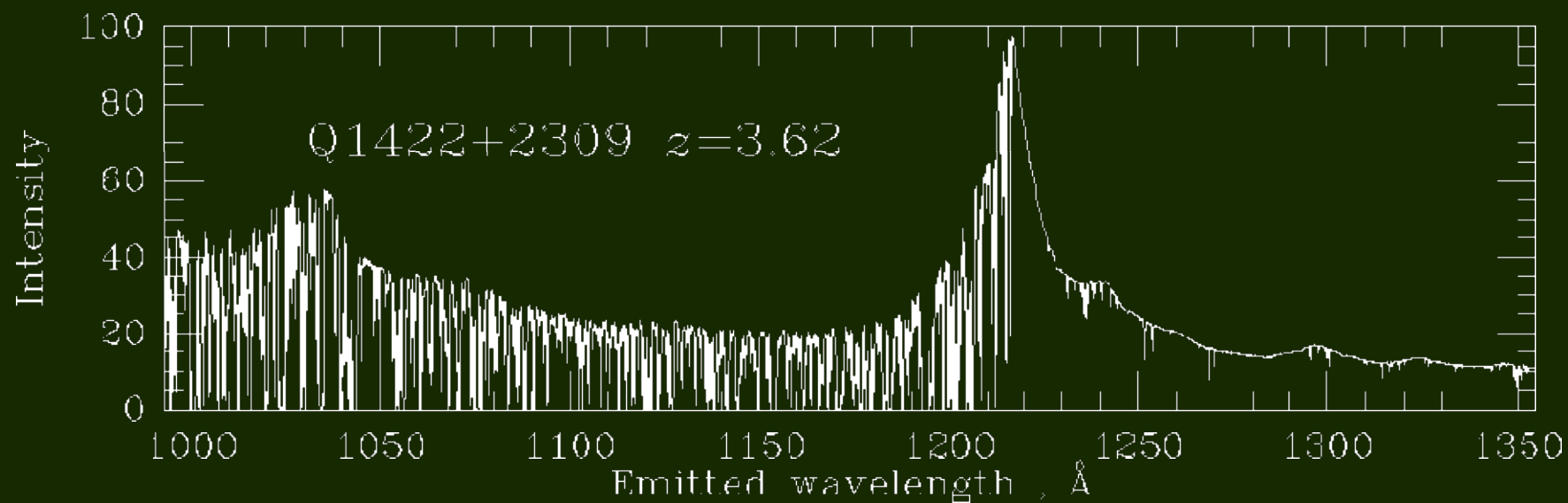
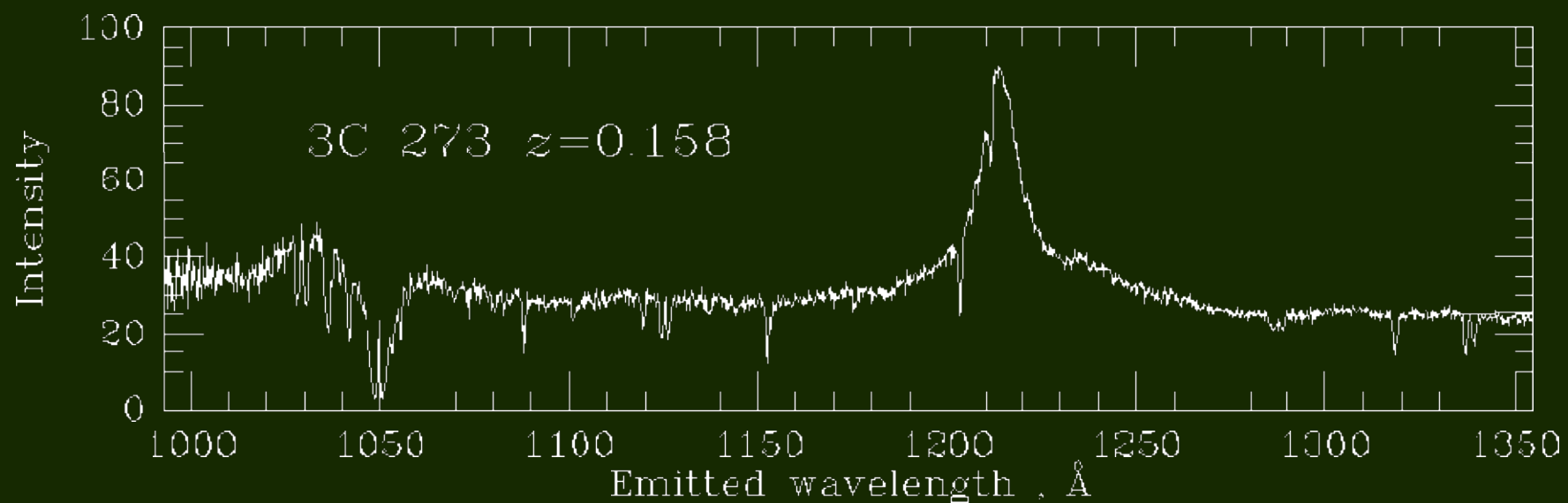
Ly α Spectra: 1D density distribution



Resonance Line +
Cosmological Redshift

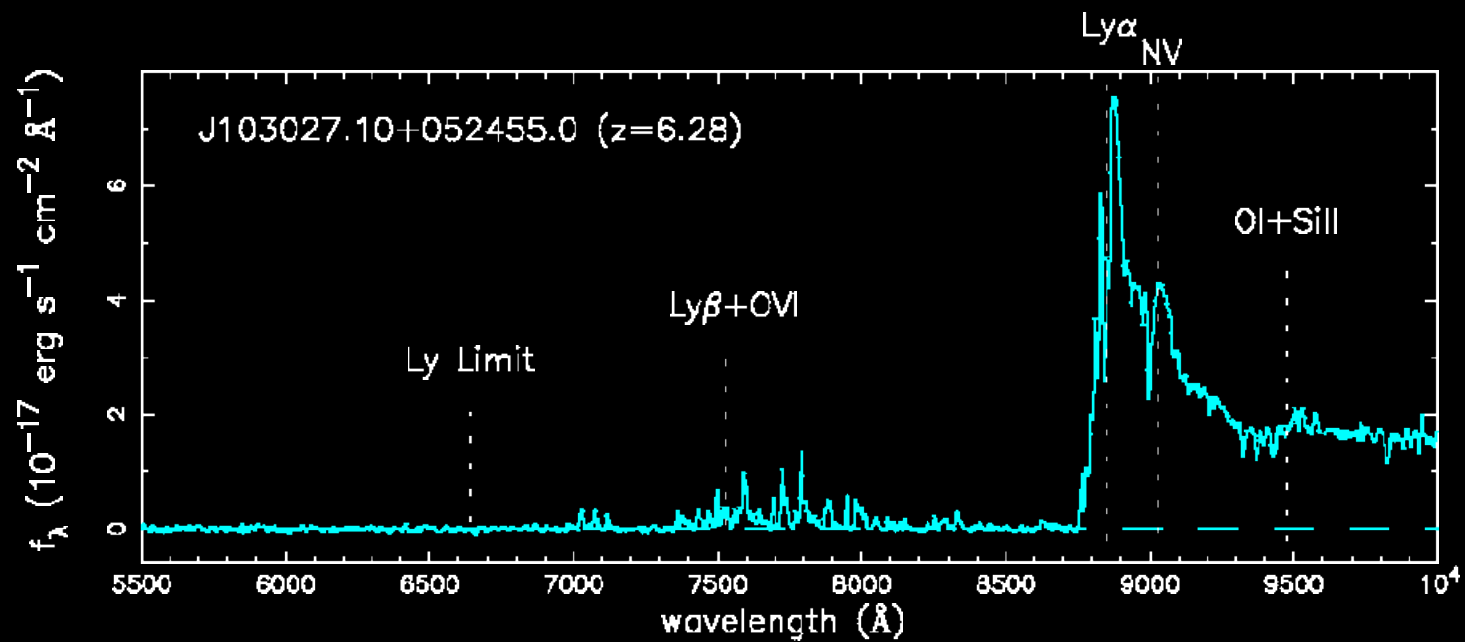
$$1100\text{\AA} \times (1 + z) \\ = 1216\text{\AA} \times (1 + z')$$

Gunn & Peterson 1965:
$$\tau_{\text{GP}} = \frac{\pi e^2 f_{\alpha} \lambda_{\alpha} n_{\text{HI}}}{m_e c H} = 6.62 \times 10^5 \left(\frac{\Omega_b h}{0.0327} \right) \left(\frac{\Omega_m}{0.307} \right)^{-1/2} \left(\frac{1+z}{10} \right)^{3/2}$$



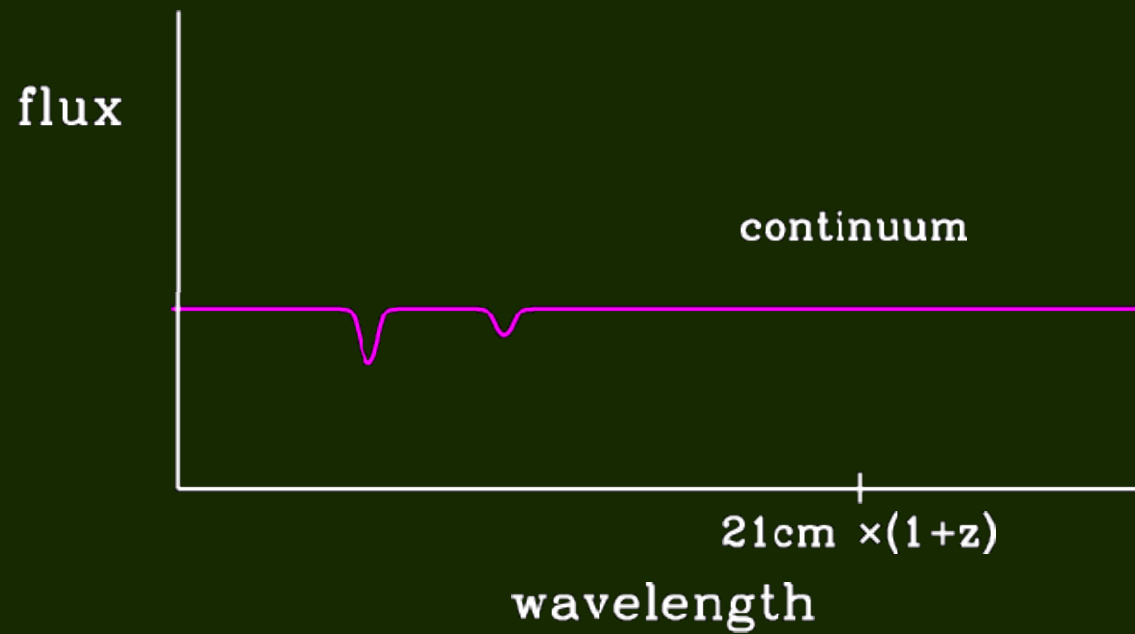
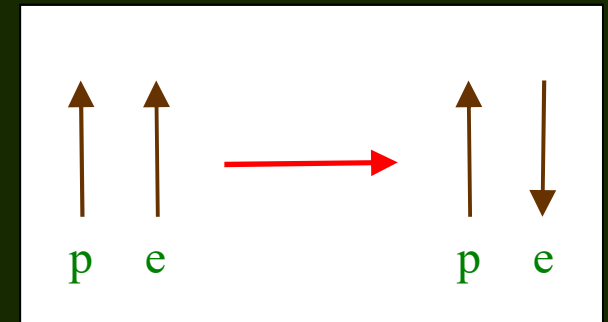
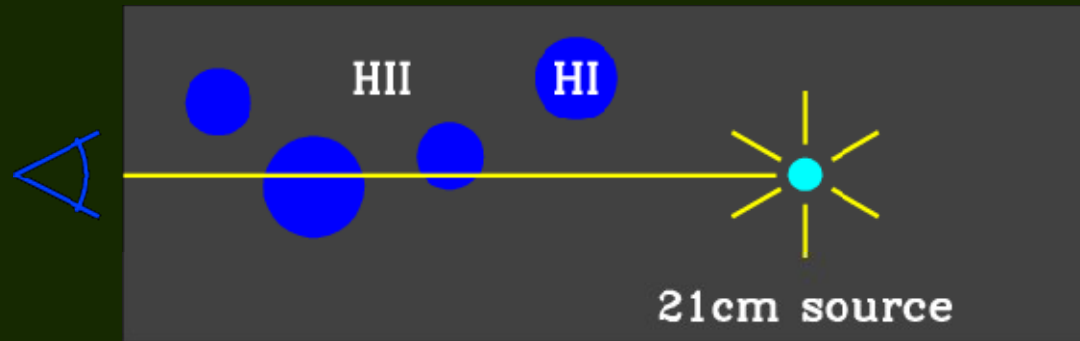
Keck, HST; Mike Rauch
<http://www.astr.ua.edu/keel/agn/forest.html>

Quasar at $z=6.3$



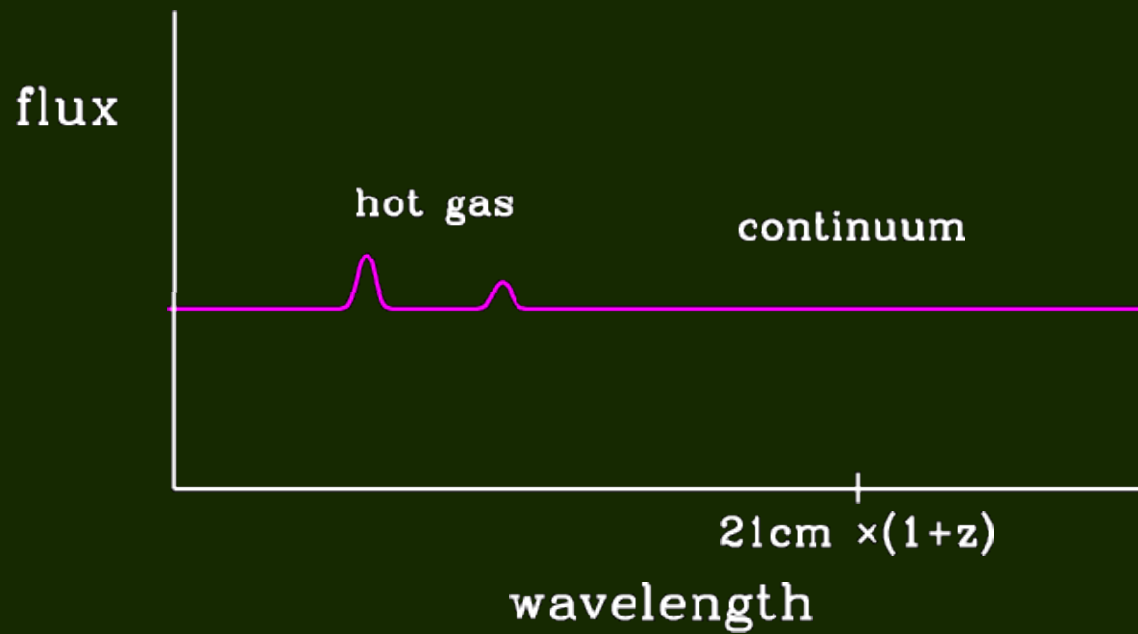
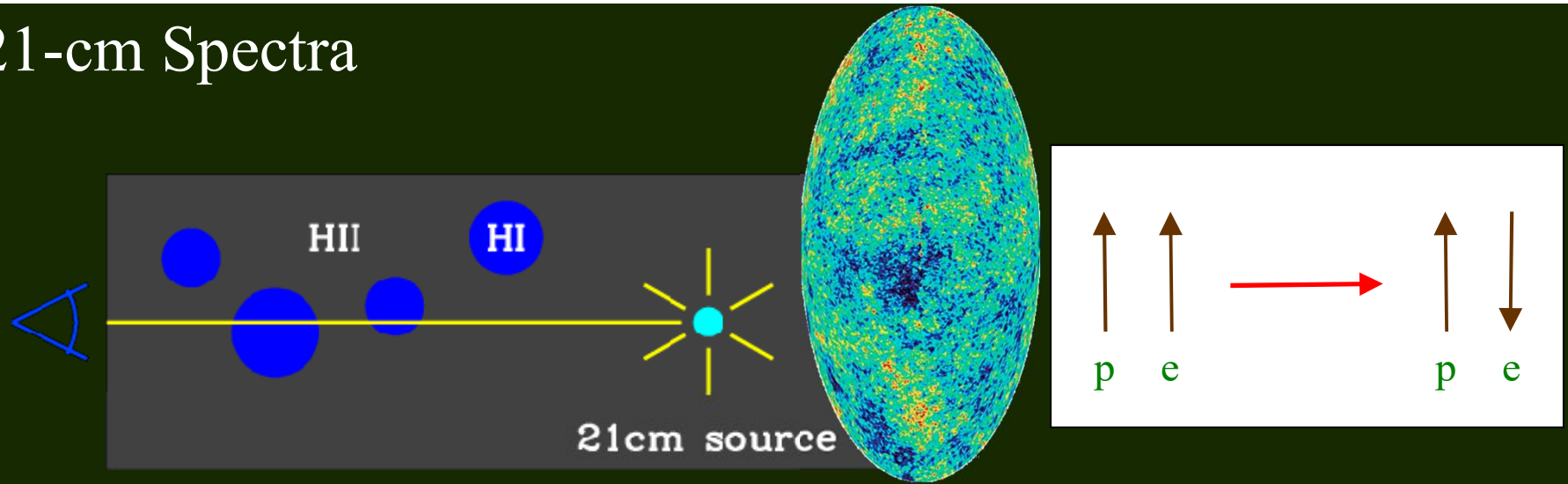
Becker et al. 2001

21-cm Spectra



Resonance Line +
Cosmological Redshift

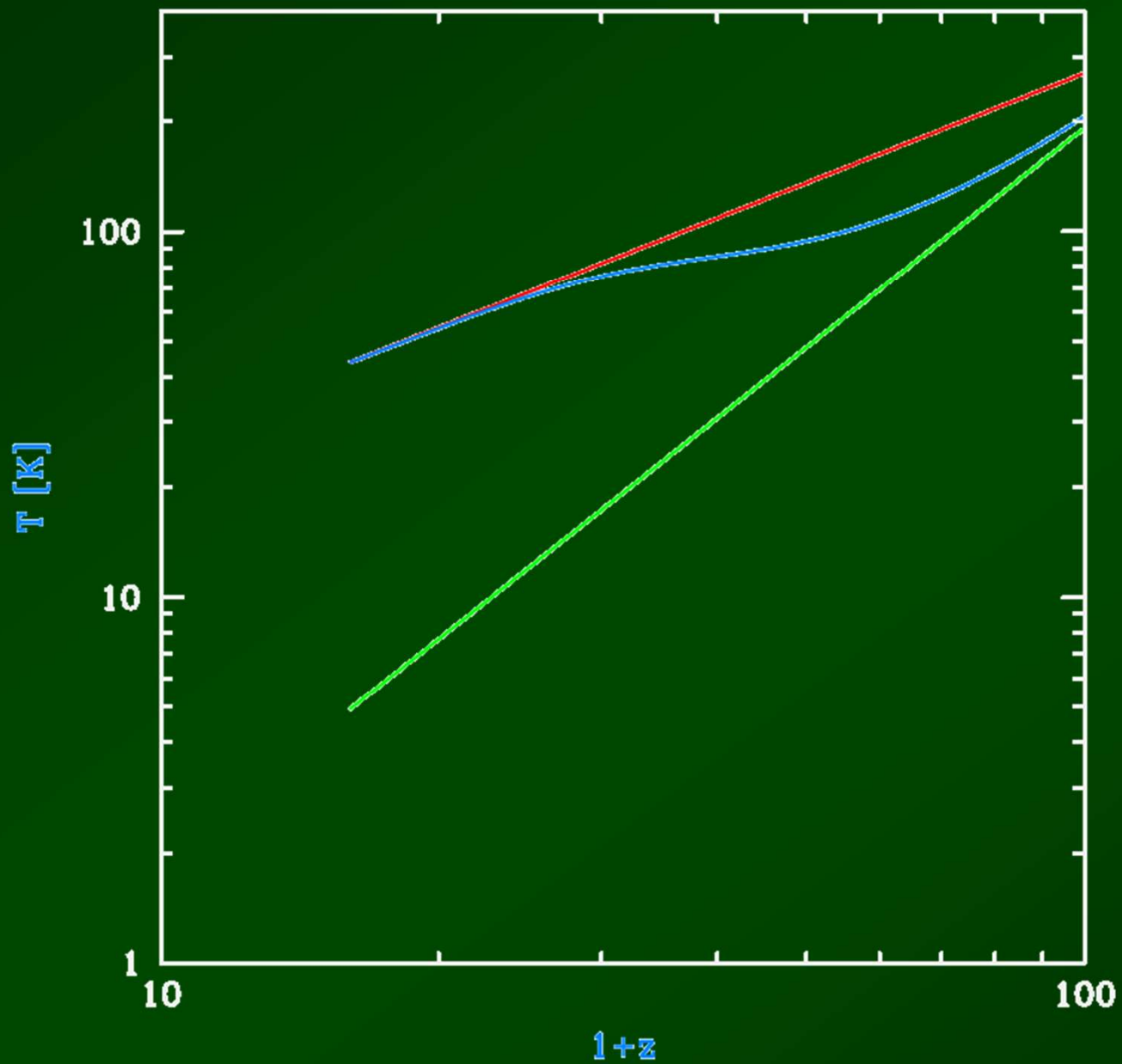
21-cm Spectra



Resonance Line +
Cosmological Redshift



Mean Temperatures

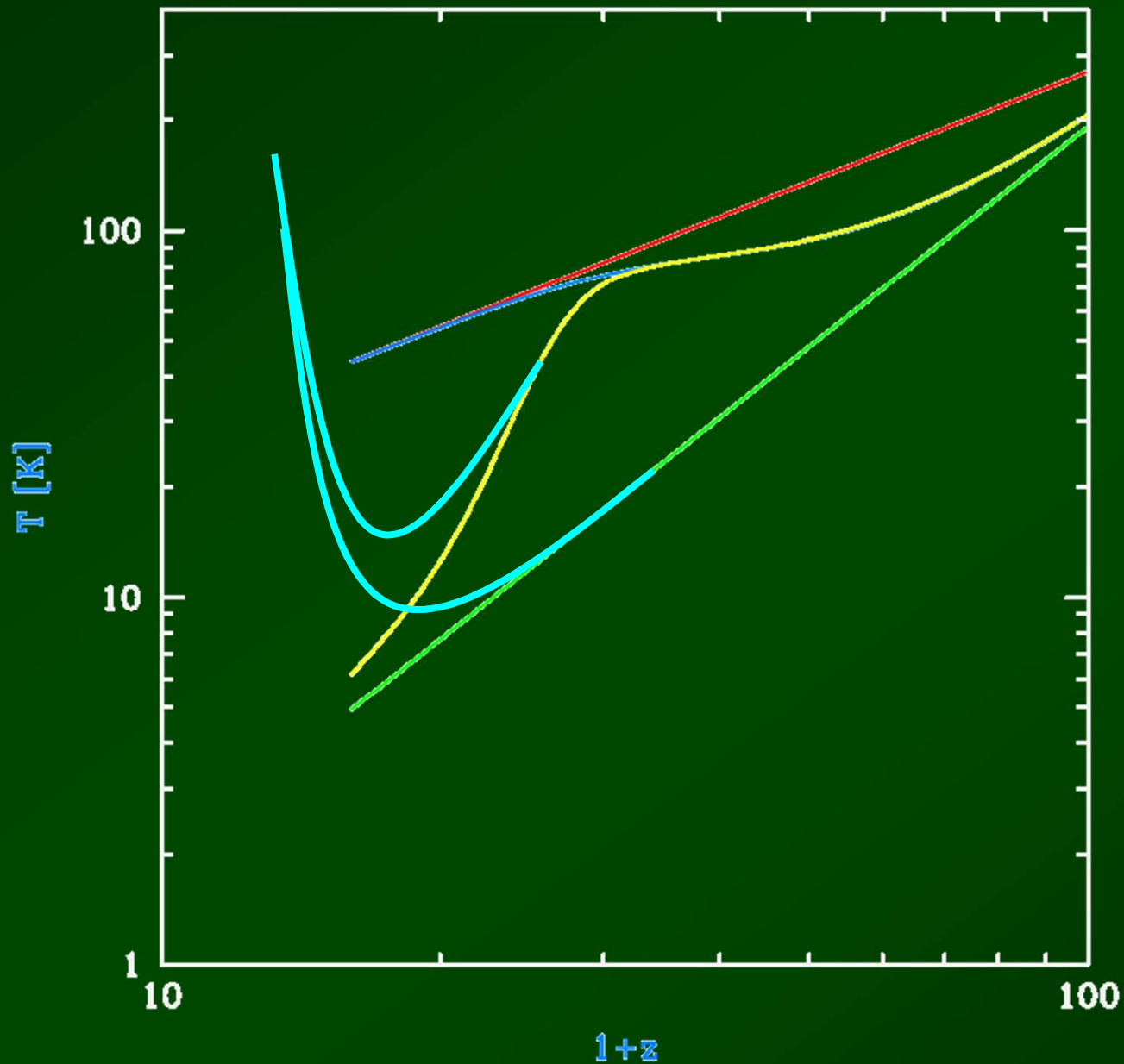


T_{CMB}

T_S

T_k

Mean Temperatures



T_{CMB}

T_S

T_k

+ Ly α

Madau, Meiksin
& Rees 1997

+ Heating

Atomic Physics: 21-cm Line

Spin temperature:

$$\frac{n_1}{n_0} = 3 \exp \left\{ -\frac{T_*}{T_S} \right\}$$

Optical depth:

$$\tau(z) = \frac{3c\lambda_{21}^2 h_P A_{10} n_H I}{32\pi k_B T_S (1+z)(dv_r/dr)}$$

$$\lambda_{21} = 21 \text{ cm}$$

$$A_{10} = 2.85 \times 10^{-15} \text{ s}^{-1}$$

High z :

$$dv_r/dr = H(z)/(1+z)$$

$$\tau(z) = 9.85 \times 10^{-3} \left(\frac{T_{\text{CMB}}}{T_S} \right) \left(\frac{\Omega_b h}{0.0327} \right) \left(\frac{\Omega_m}{0.307} \right)^{-1/2} \left(\frac{1+z}{10} \right)^{1/2}$$

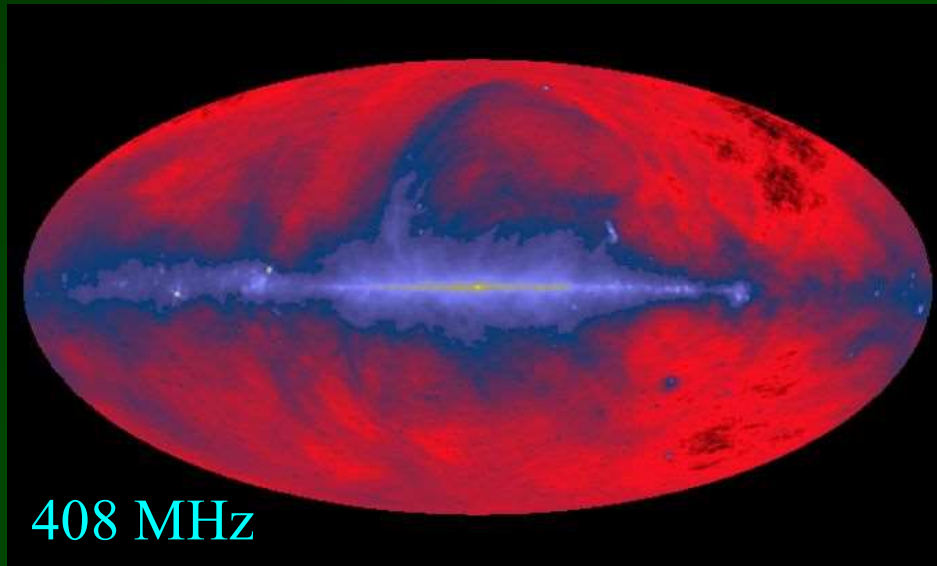
Brightness temperature:

$$I_\nu = 2k_B T_b \frac{\nu^2}{c^2}$$

$$T_b^z = T_{\text{CMB}} e^{-\tau} + T_S (1 - e^{-\tau})$$

$$T_b = (1+z)^{-1} (T_S - T_{\text{CMB}}) (1 - e^{-\tau}) \simeq 26.8 \text{ mK} \left(\frac{\Omega_b h}{0.0327} \right) \left(\frac{\Omega_m}{0.307} \right)^{-1/2} \left(\frac{1+z}{10} \right)^{1/2} \left(\frac{T_S - T_{\text{CMB}}}{T_S} \right)$$

Foregrounds



$$T_{\text{sky}} \sim 200 \text{ K} \\ (\nu = 170 \text{ MHz})$$

=> Large-Scale Fluctuations

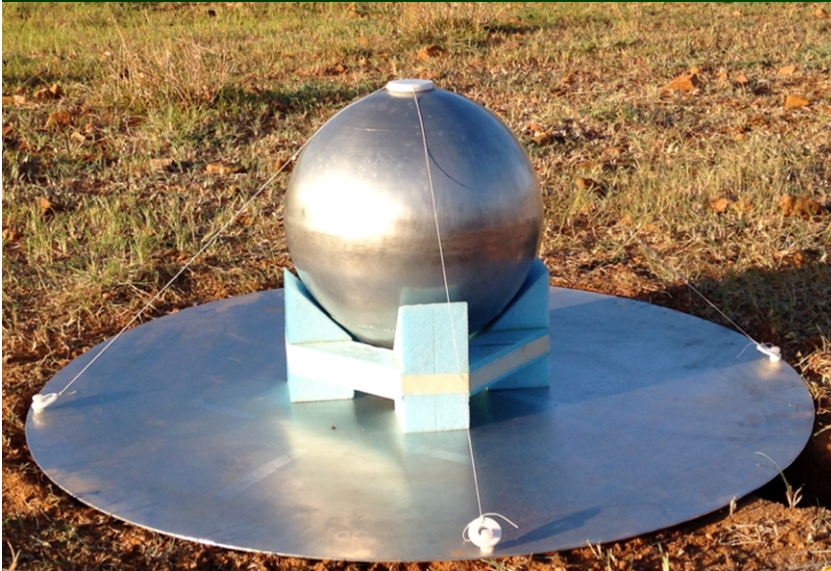
$$\delta T_b = \langle T_b \rangle \sqrt{\frac{k^3 P(k)}{2\pi^2}}$$

$$T_{\text{signal}} \sim 1\text{-}10 \text{ mK}$$

$$T_{\text{current}} \sim 40 \text{ mK}$$

Global 21-cm Experiments

SARAS



EDGES high



LEDA



GMRT

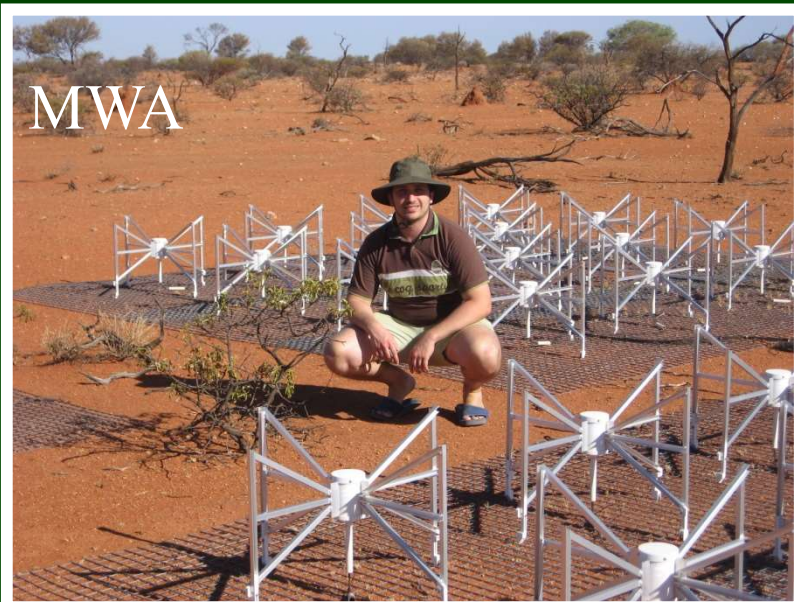


Interferometer Experiments

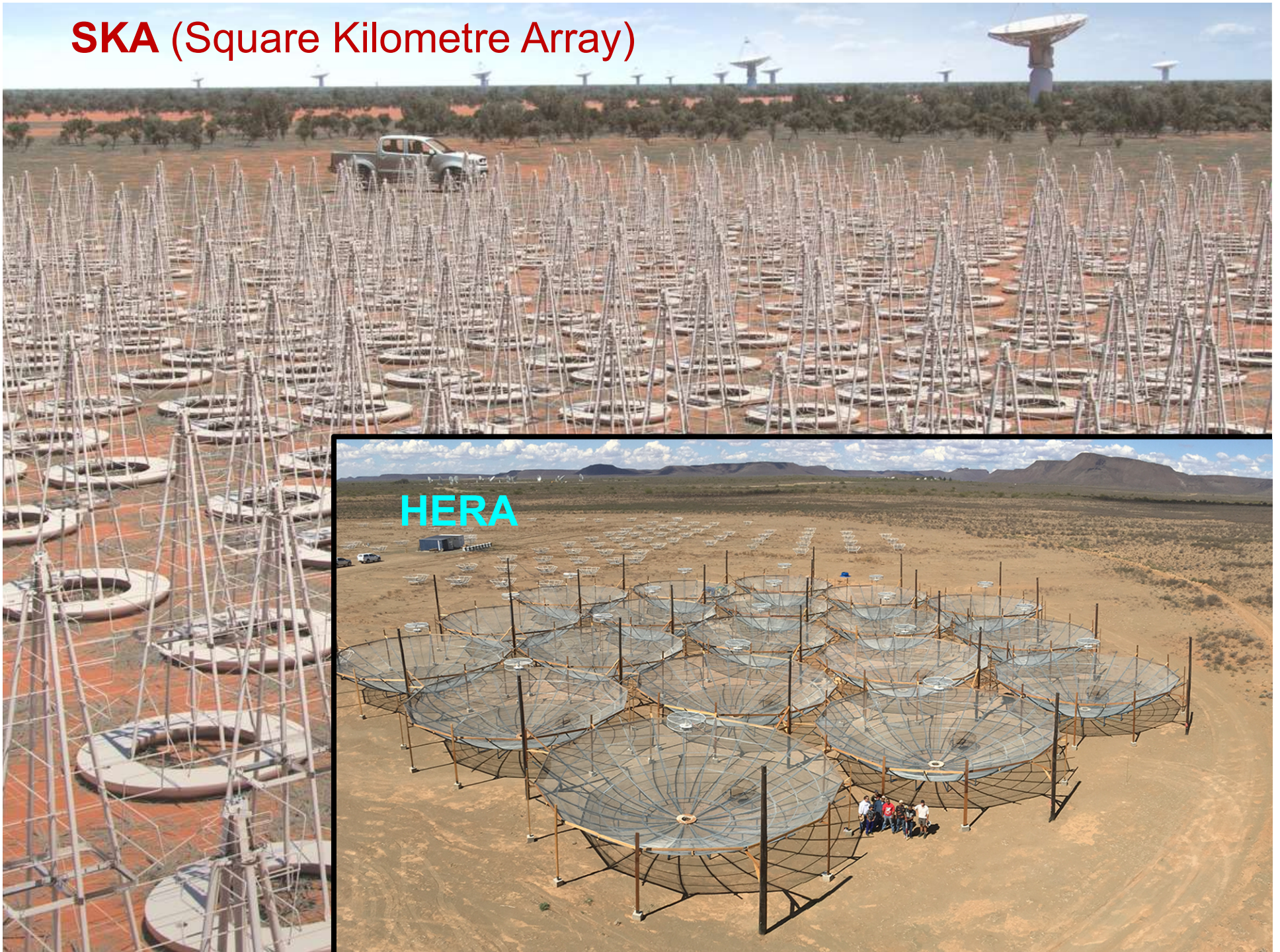
Paper



MWA



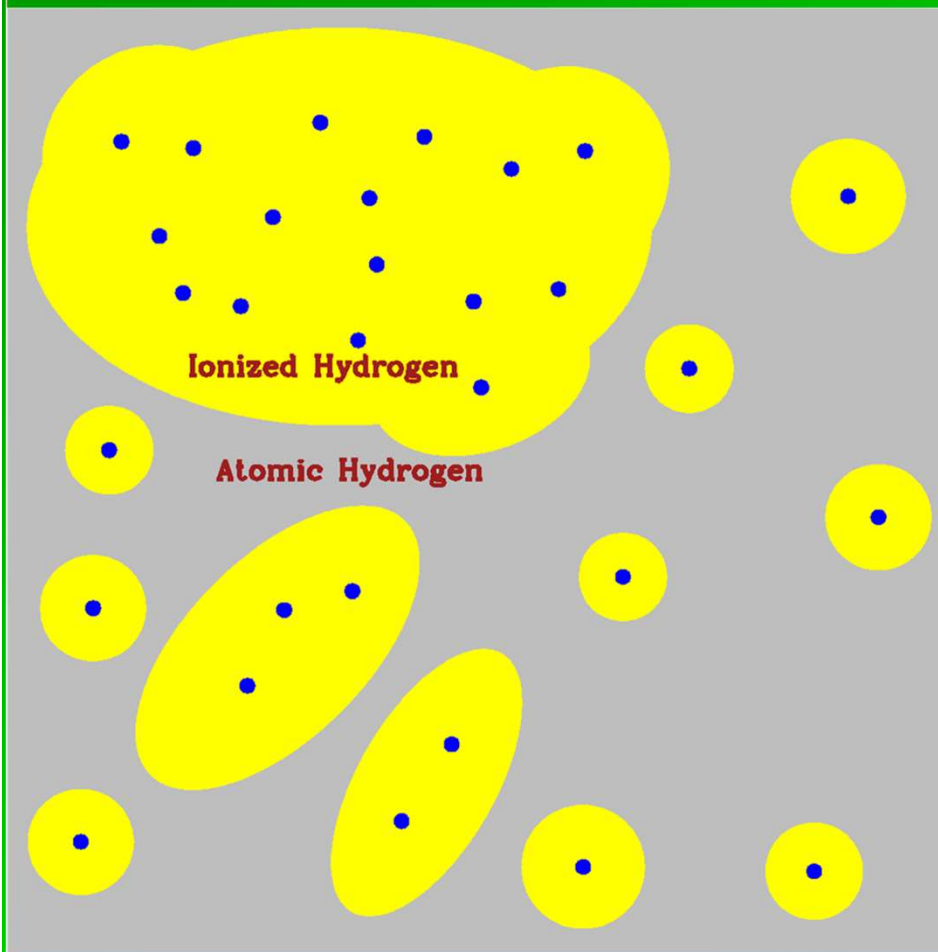
SKA (Square Kilometre Array)



HERA

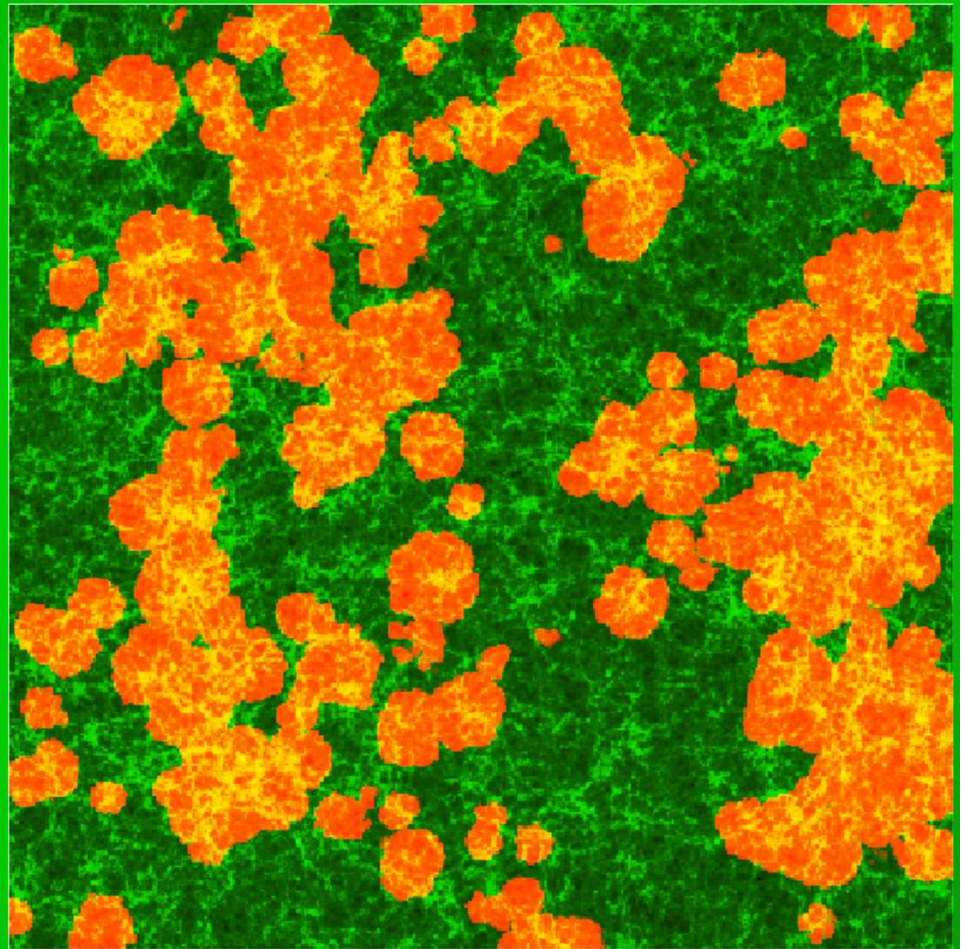


Cosmic Reionization



RB & Loeb 2004

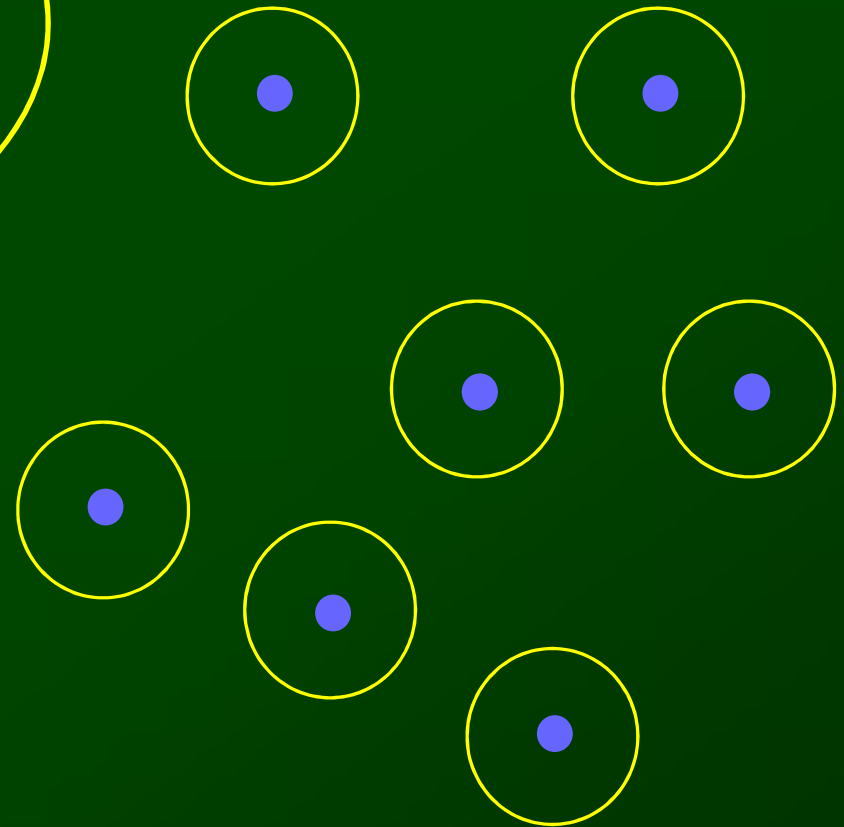
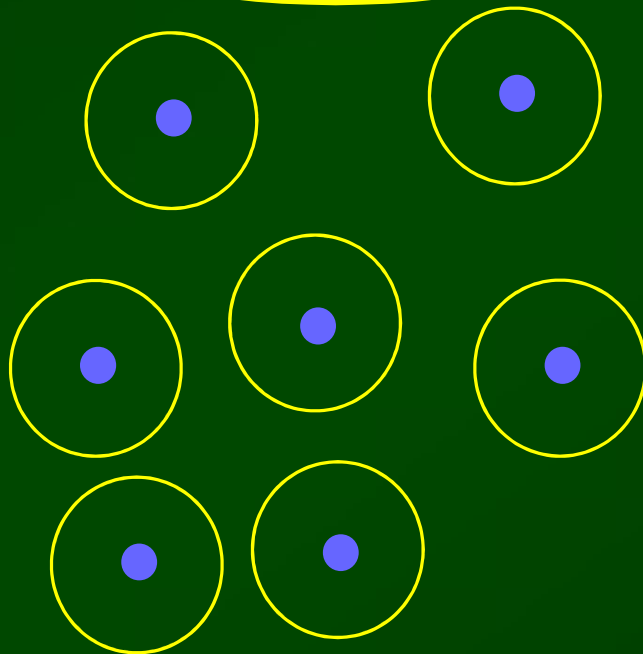
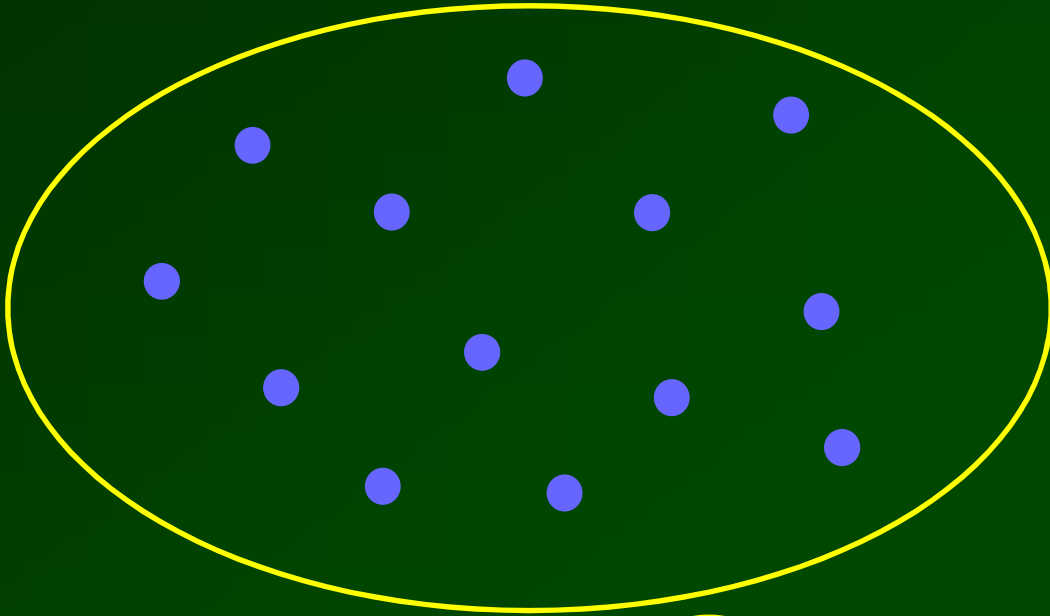
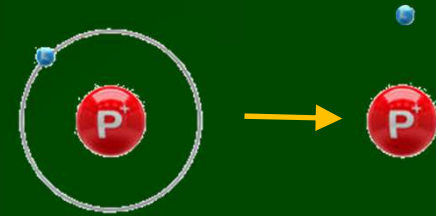
Inside-out reionization



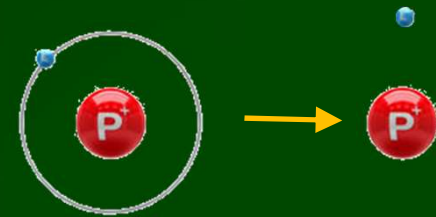
← 100/h Mpc = 0.5° →
Mellema et al. 2006

Furlanetto, Zaldariagga, Hernquist 2004

Reionization

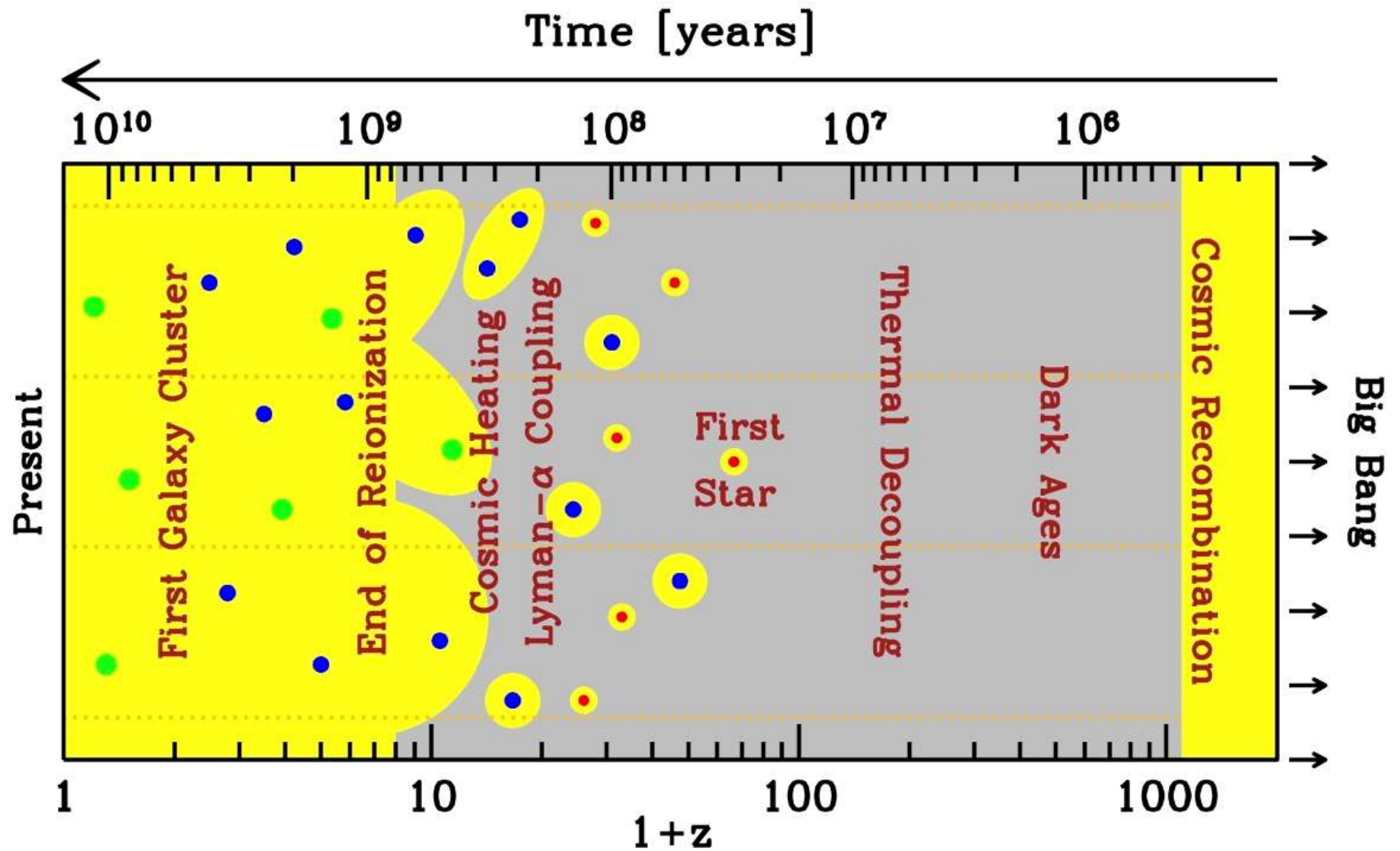


Reionization



21-cm radiation

Cosmic History



21-cm Cosmology: Cosmic dawn

Madau, Meiksin & Rees 1997: Cosmic Dawn
(Ly- α and heating)

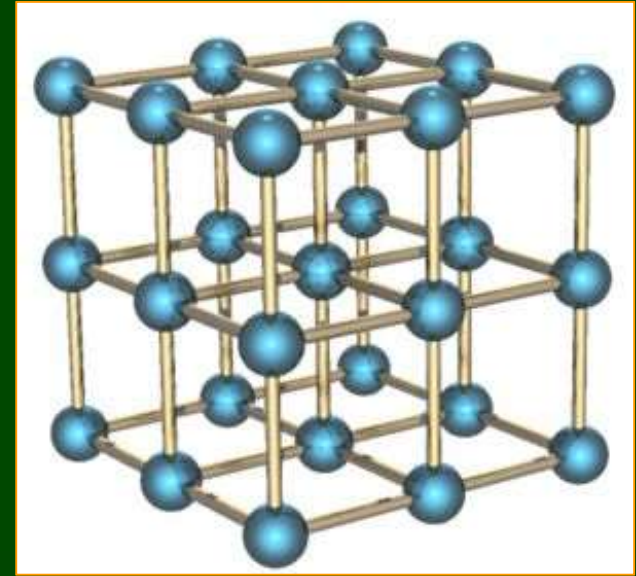
RB & Loeb 2005:
Ly- α fluctuations: $z \sim 20-30$

Pritchard & Furlanetto 2007:
Temperature fluctuations
(X-ray heating)

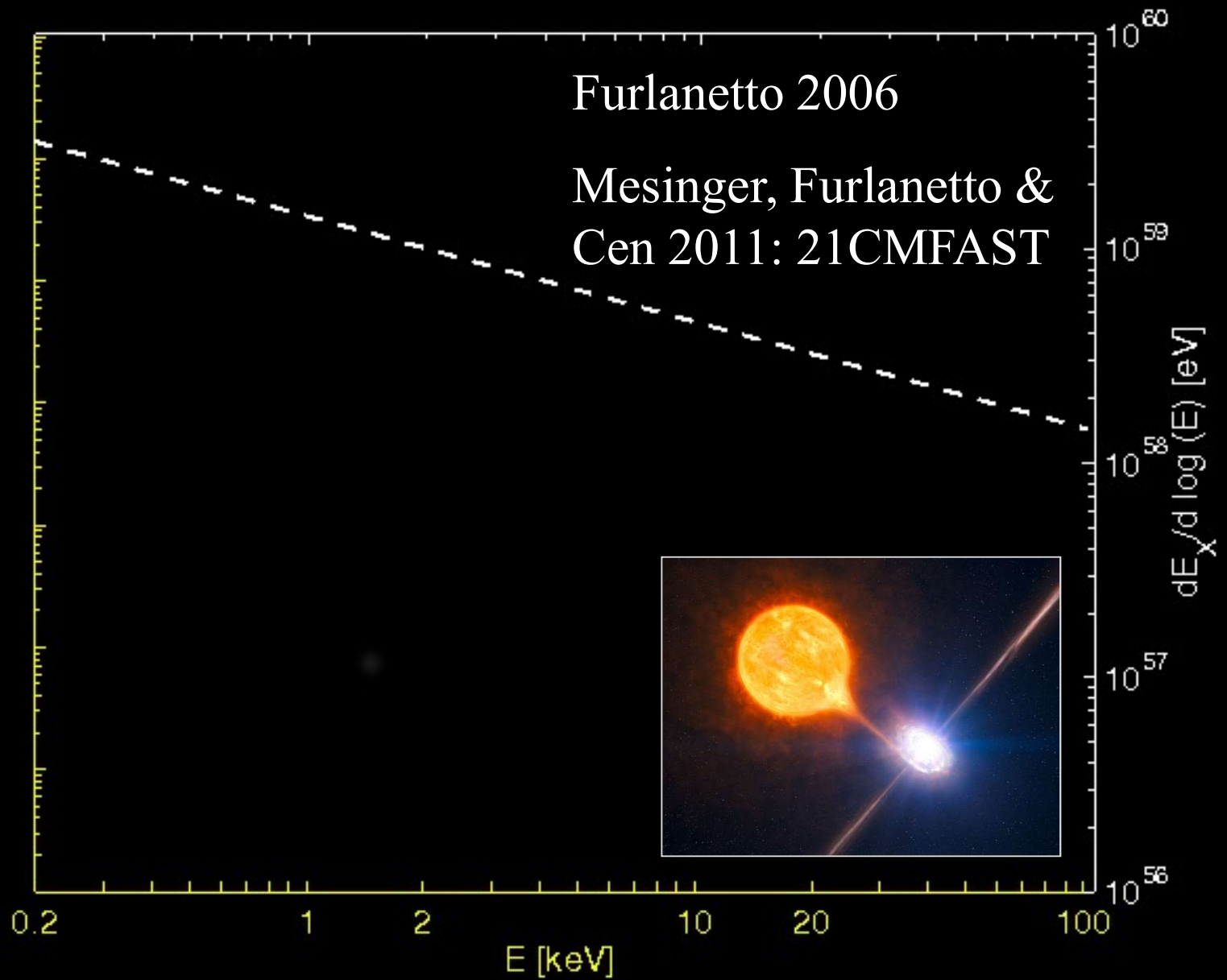
Semi-numerical Simulation

21cmfast, my group, ...

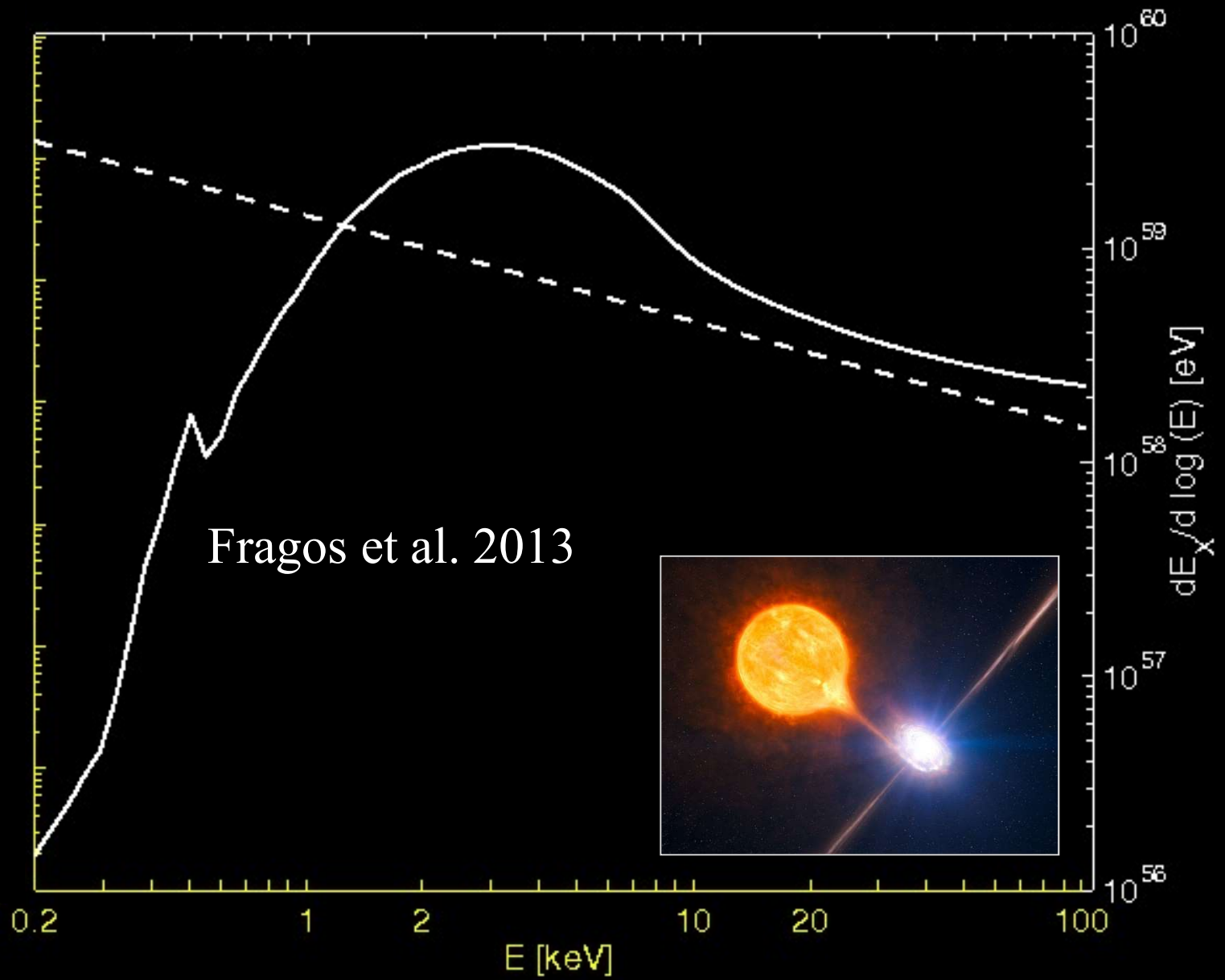
(Itamar Reis)



- In each pixel:
 - Model + simulation results + free parameters
 - Halo abundance, cooling, star formation
 - Ly- α radiation, X-rays, UV
- Numerically:
 - Sum up Ly- α and X-ray intensity, reionization
 - 21-cm image, power spectrum, global signal

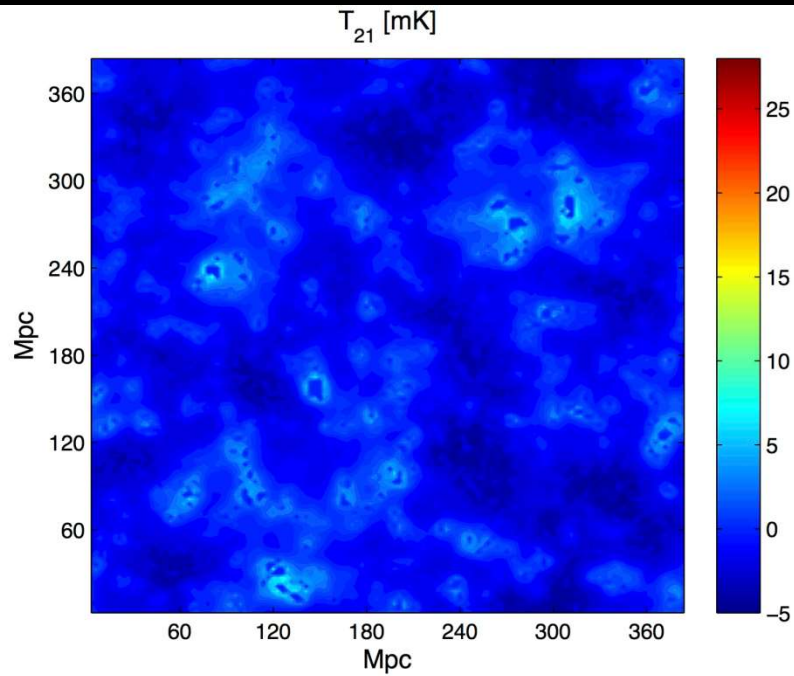


Fialkov, **RB** & Visbal **Nature** 2014

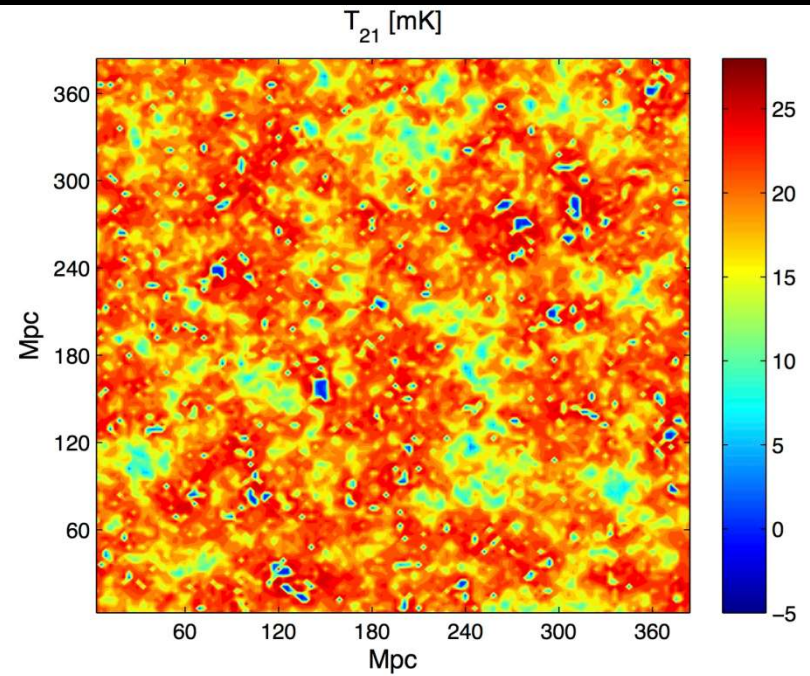


Fialkov, RB & Visbal Nature 2014

Hard X-rays



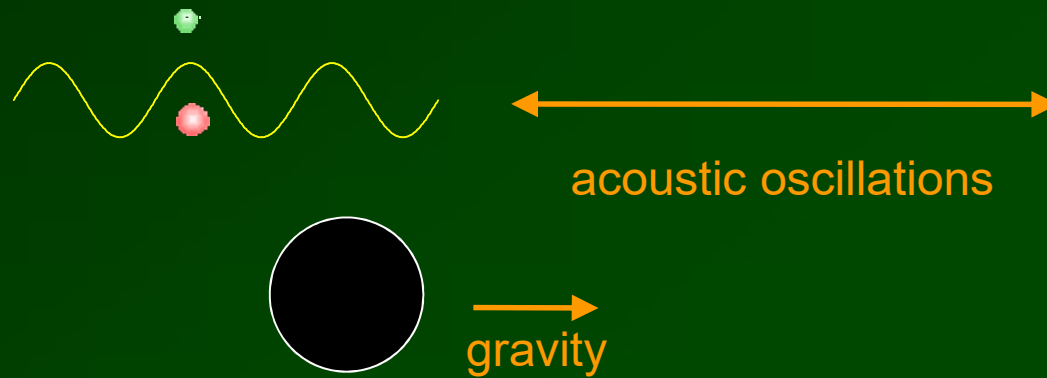
Soft X-rays



$z = 12.1$

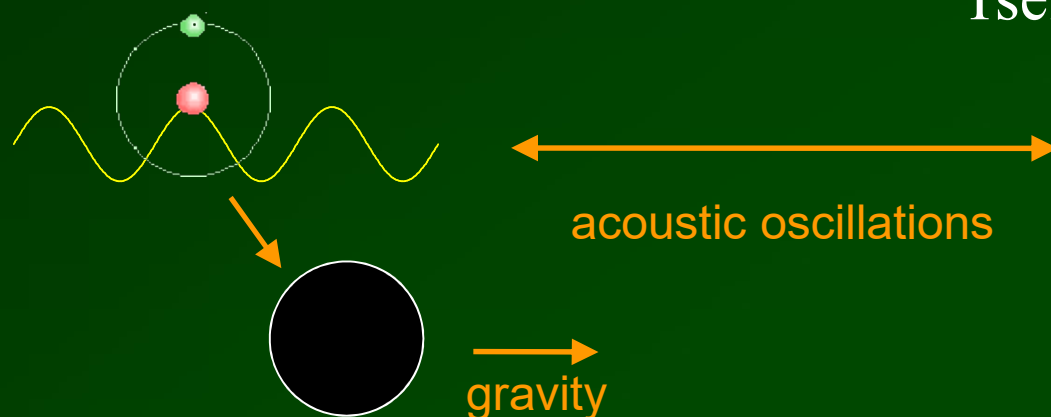
Baryon – Dark Matter Relative (Streaming) Velocity

Tseliakhovich & Hirata 2010

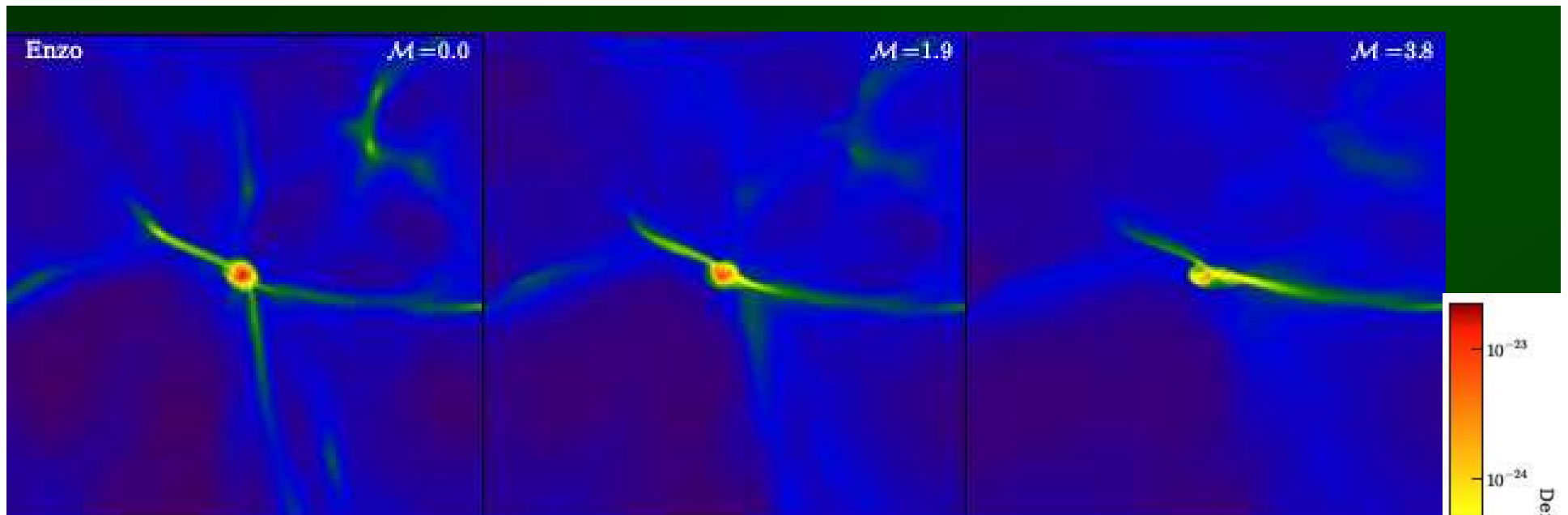


Baryon – Dark Matter Relative (Streaming) Velocity

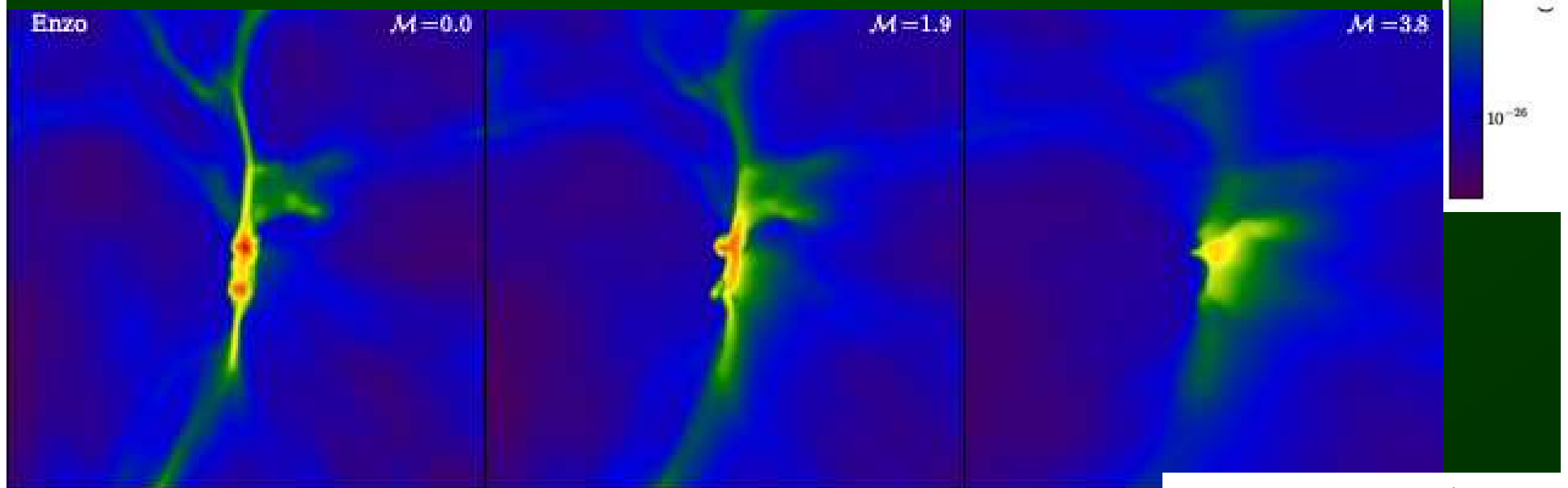
Tseliakhovich & Hirata 2010



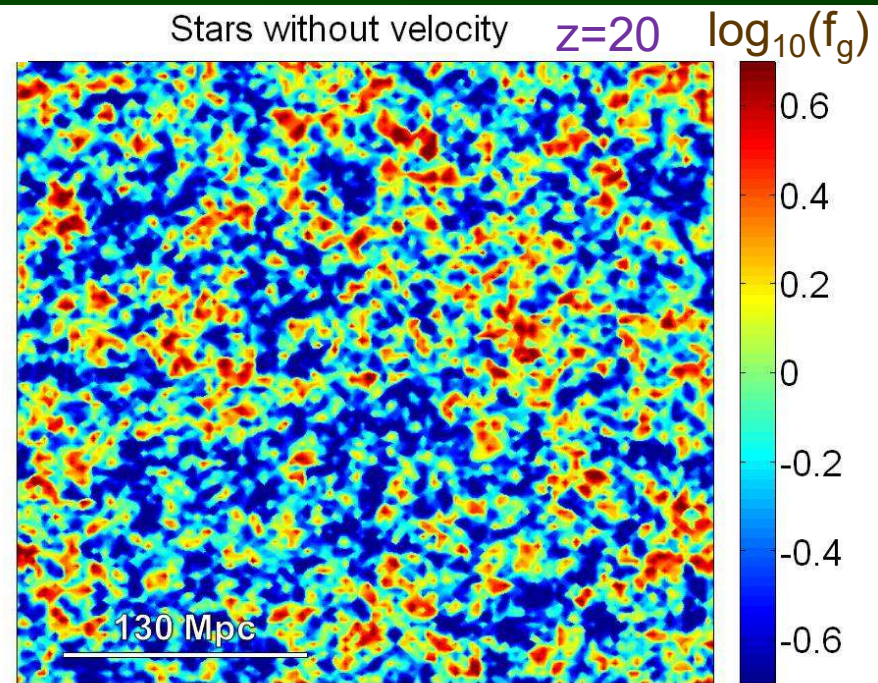
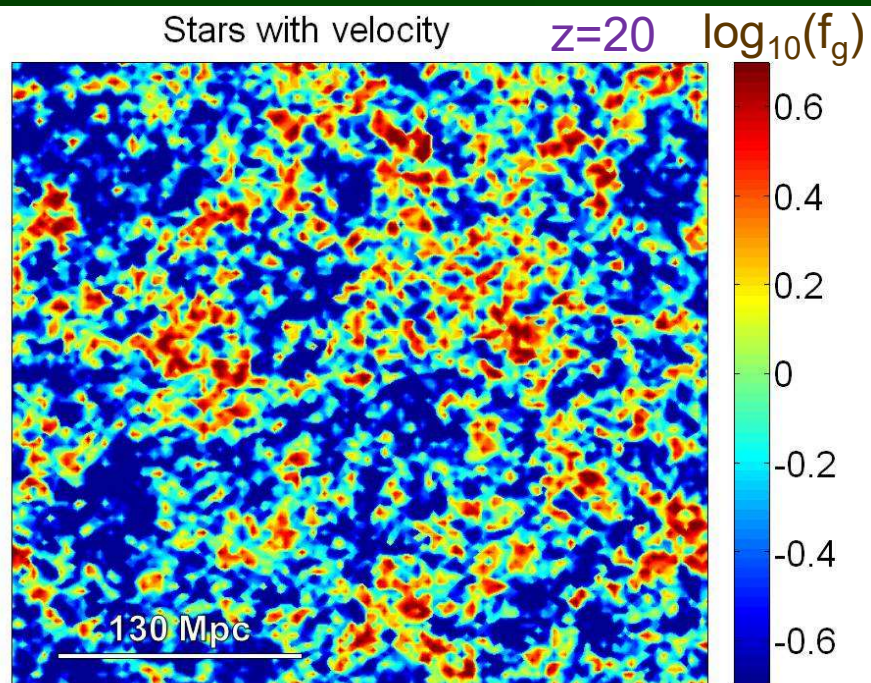
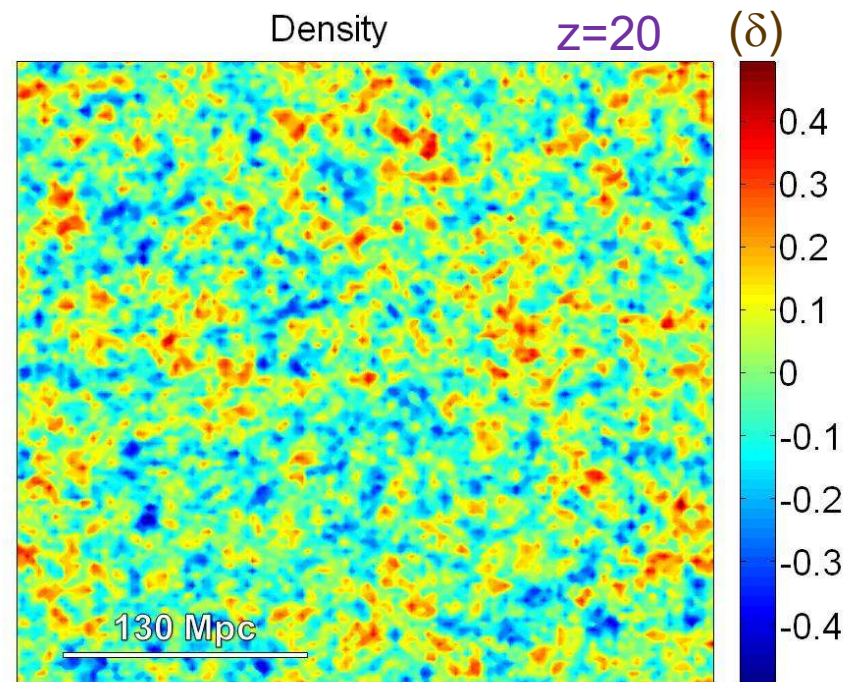
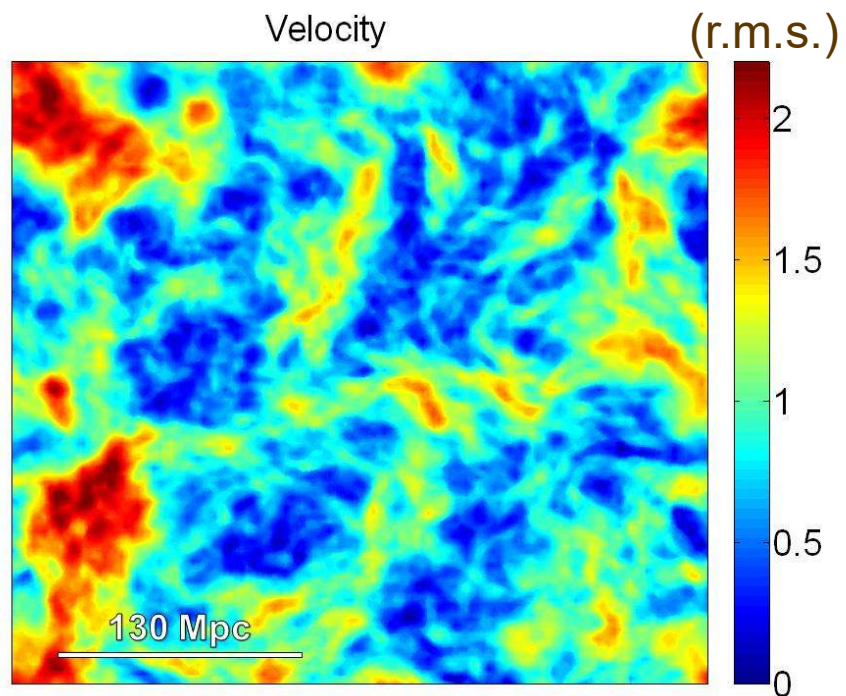
1. $|V_b - V_{\text{cdm}}|^{\text{r.m.s.}} \sim 30 \text{ km/s}$ at $z_{\text{rec}} \sim 5 \text{ } c_s$
2. Varies on large scales
3. BAOs

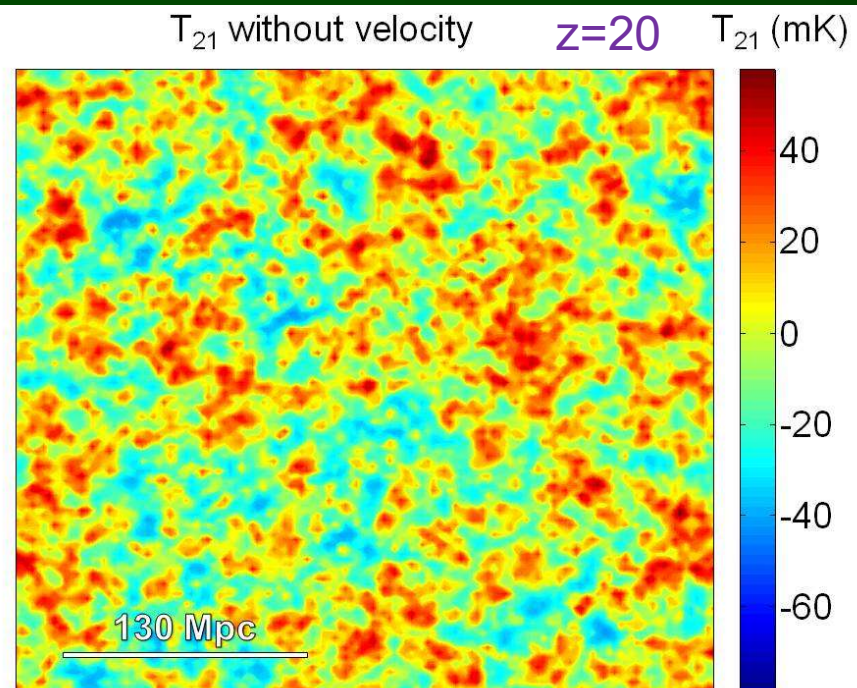
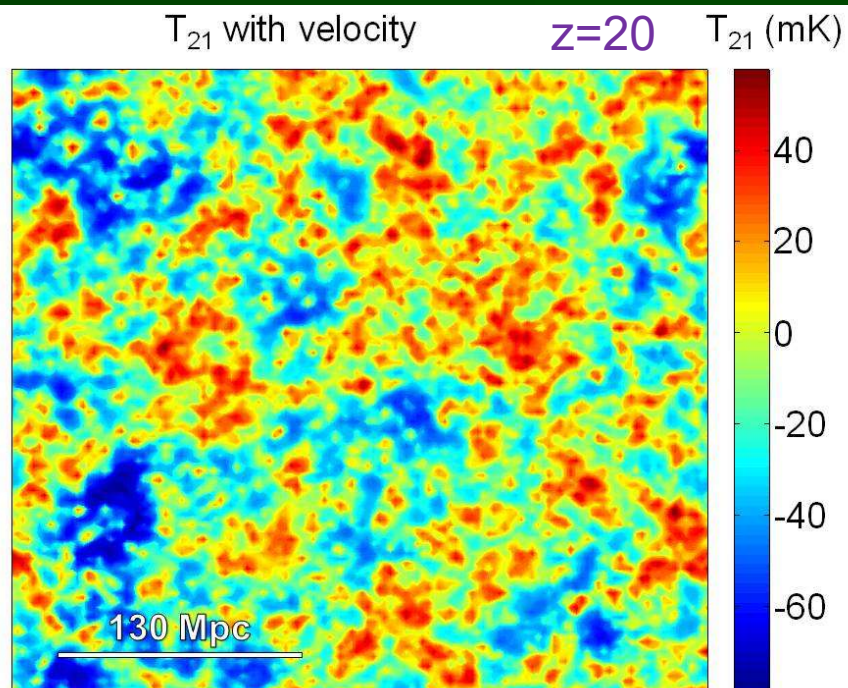
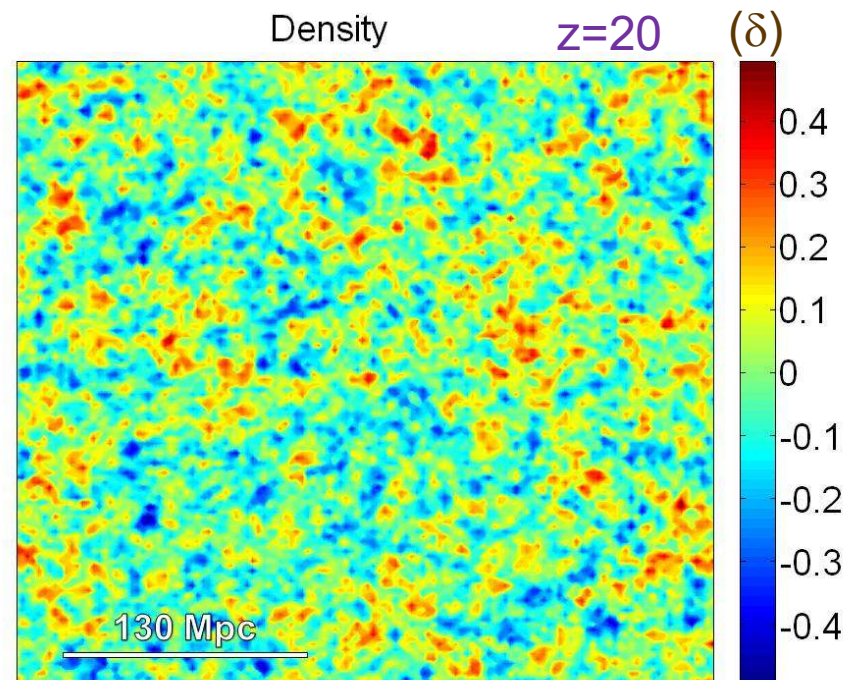
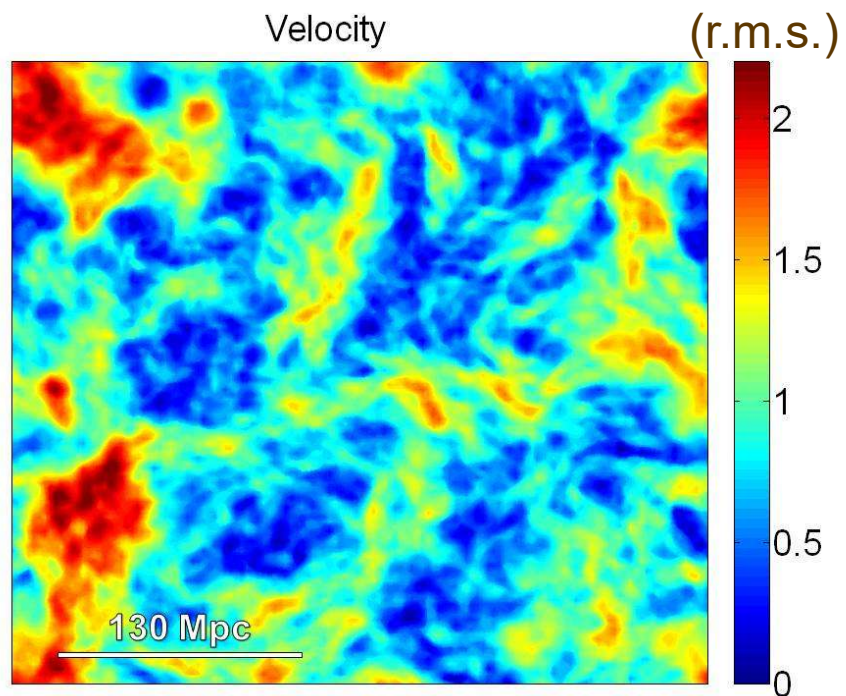


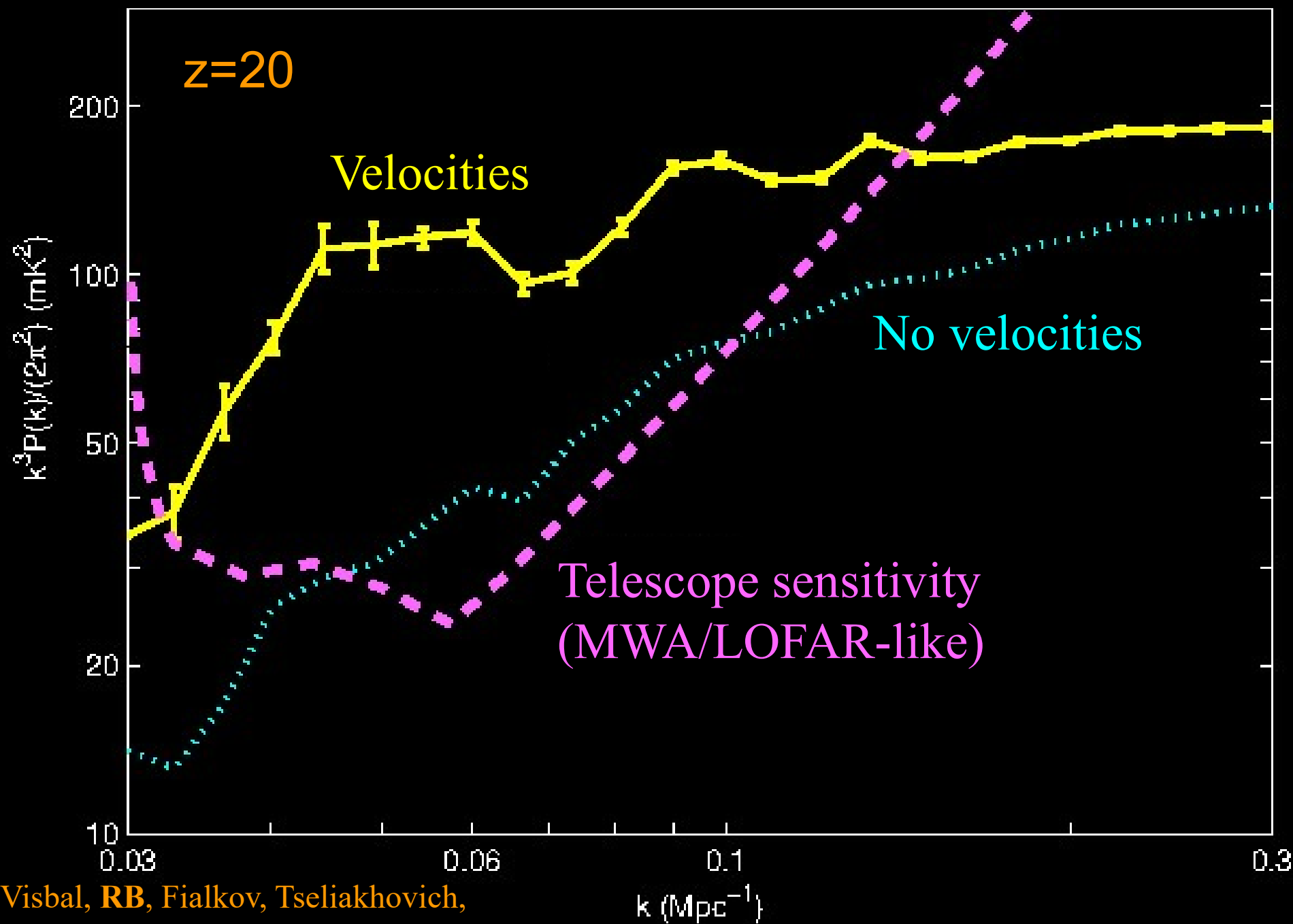
O'Leary & McQuinn 2012 $V \implies$ Gas, $z = 20, M = 2 \times 10^6 M_\odot$



$M = 8 \times 10^5 M_\odot$

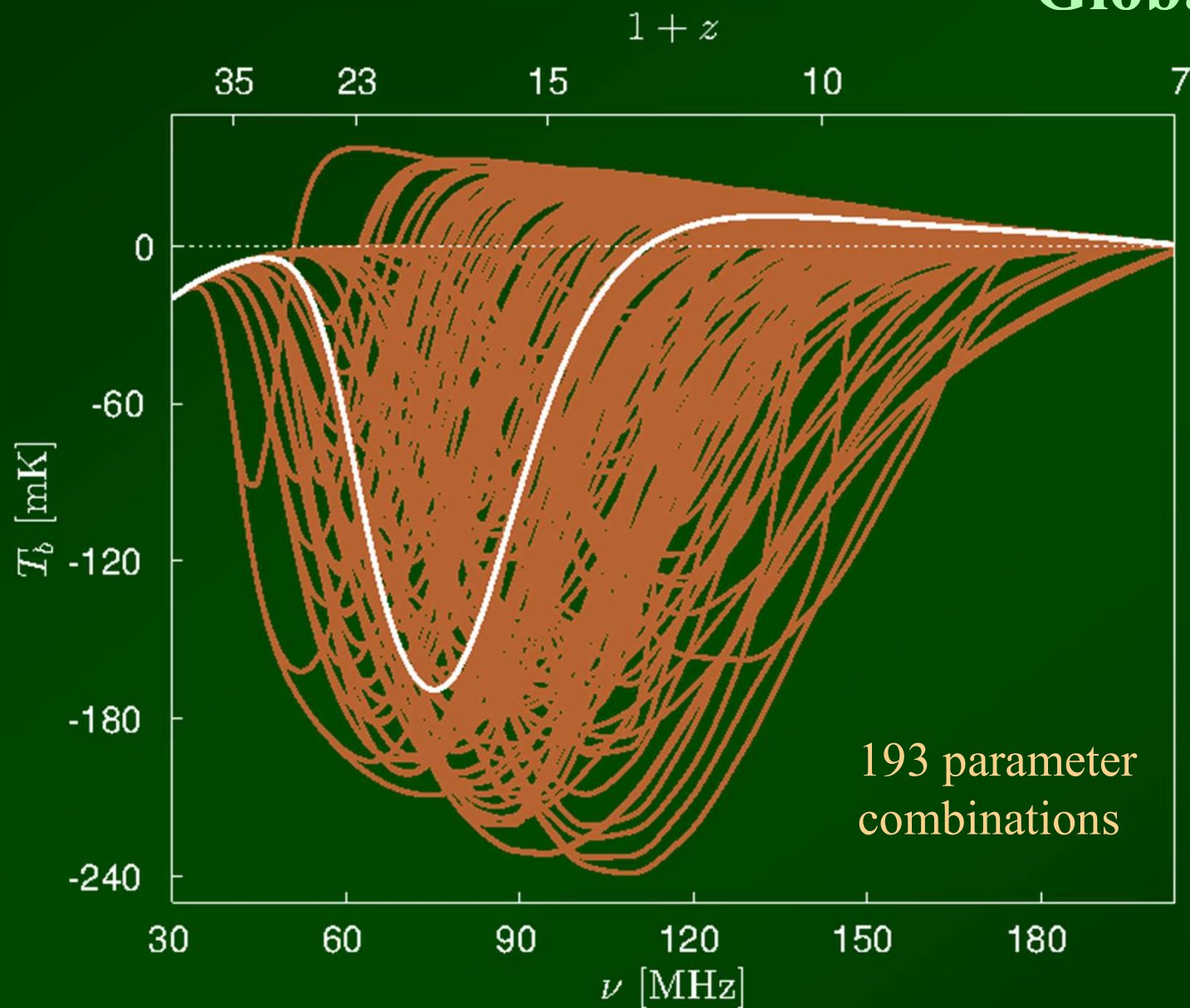






Visbal, **RB**, Fialkov, Tseliakhovich,
& Hirata Nature 2012

Global 21-cm

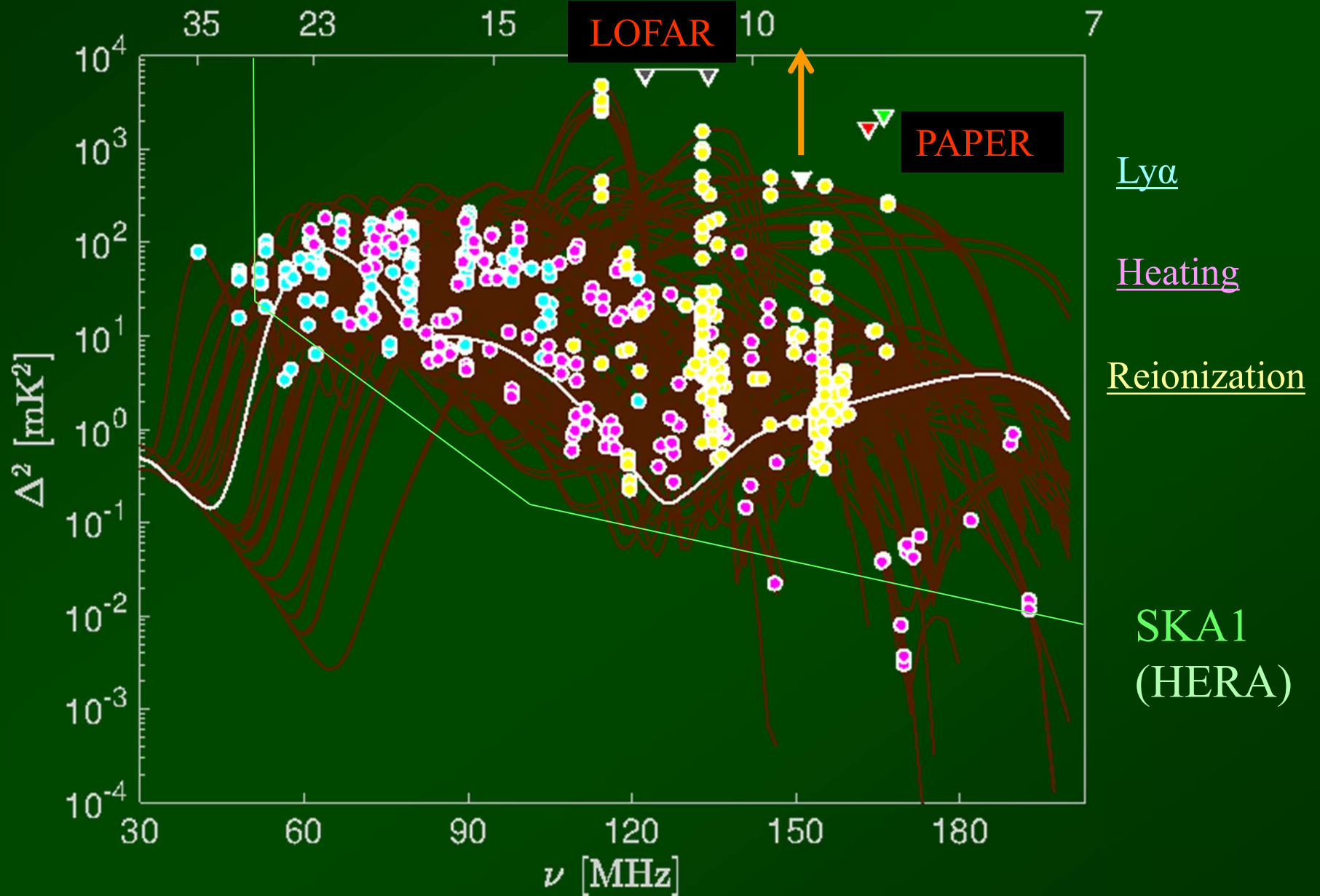


193 parameter
combinations

Cohen, Fialkov,
RB, & Lotem 2017

21-cm Power Spectrum

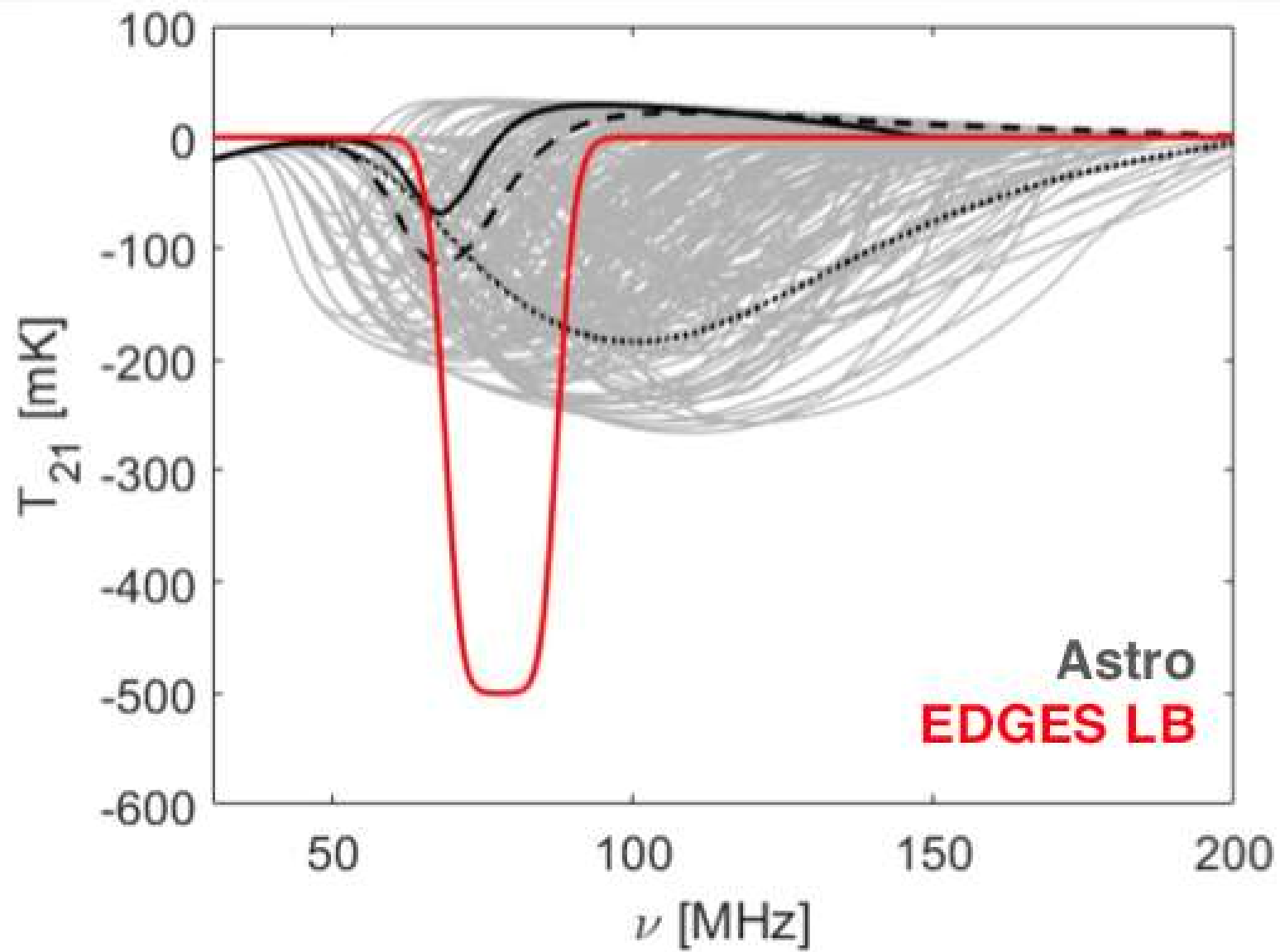
$k=0.1 \text{ Mpc}^{-1}$



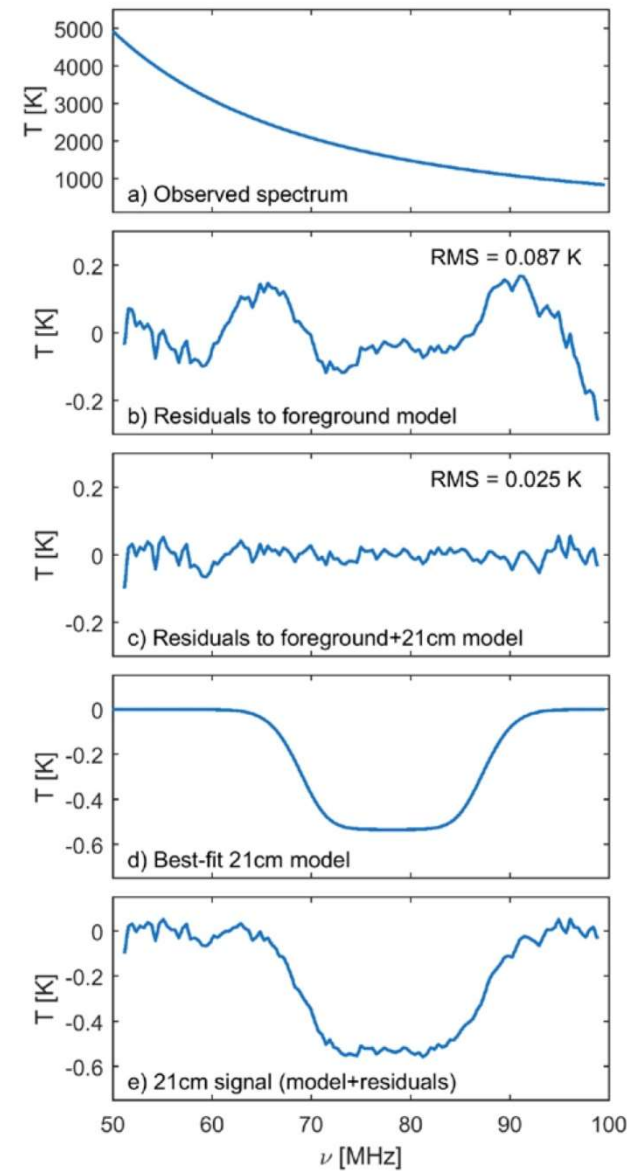
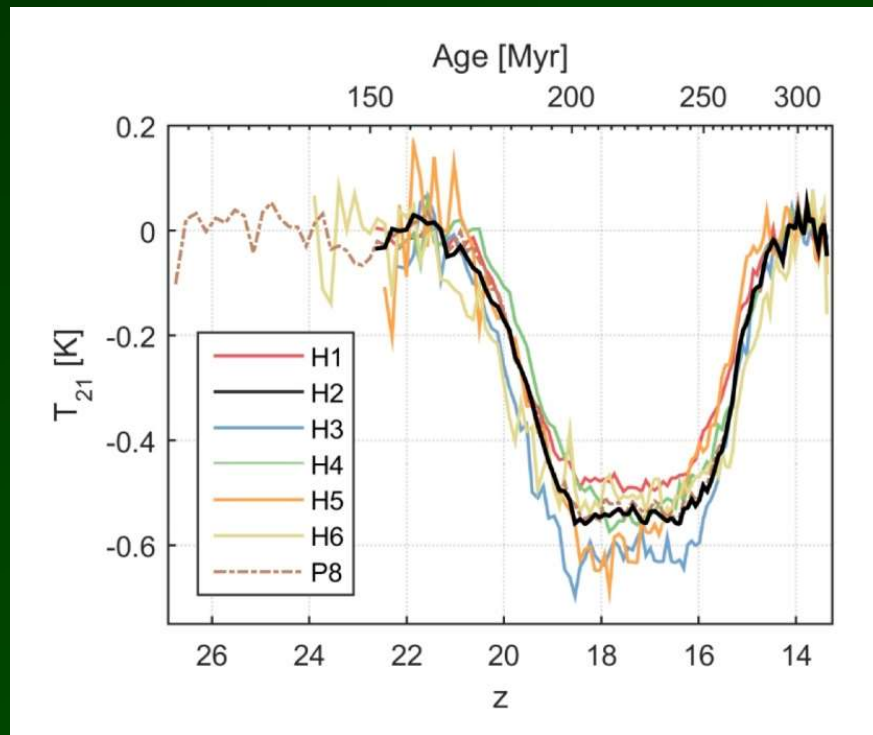
Cohen, Fialkov, RB 2017

EDGES-Low



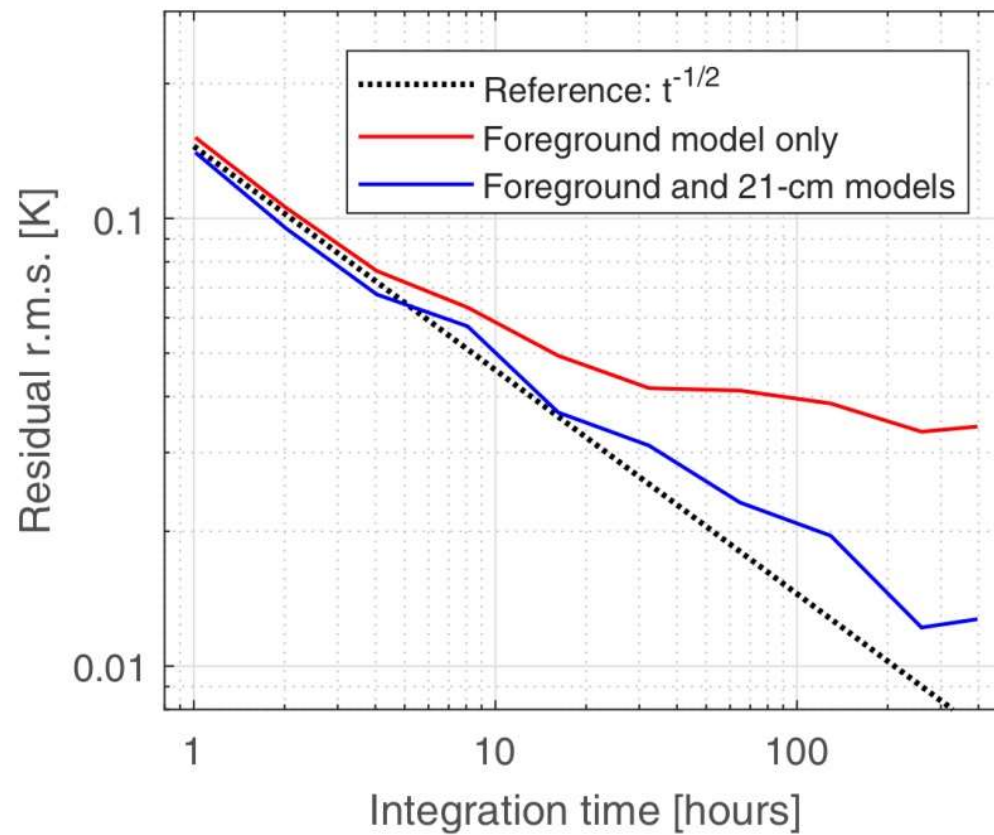


EDGES-Low

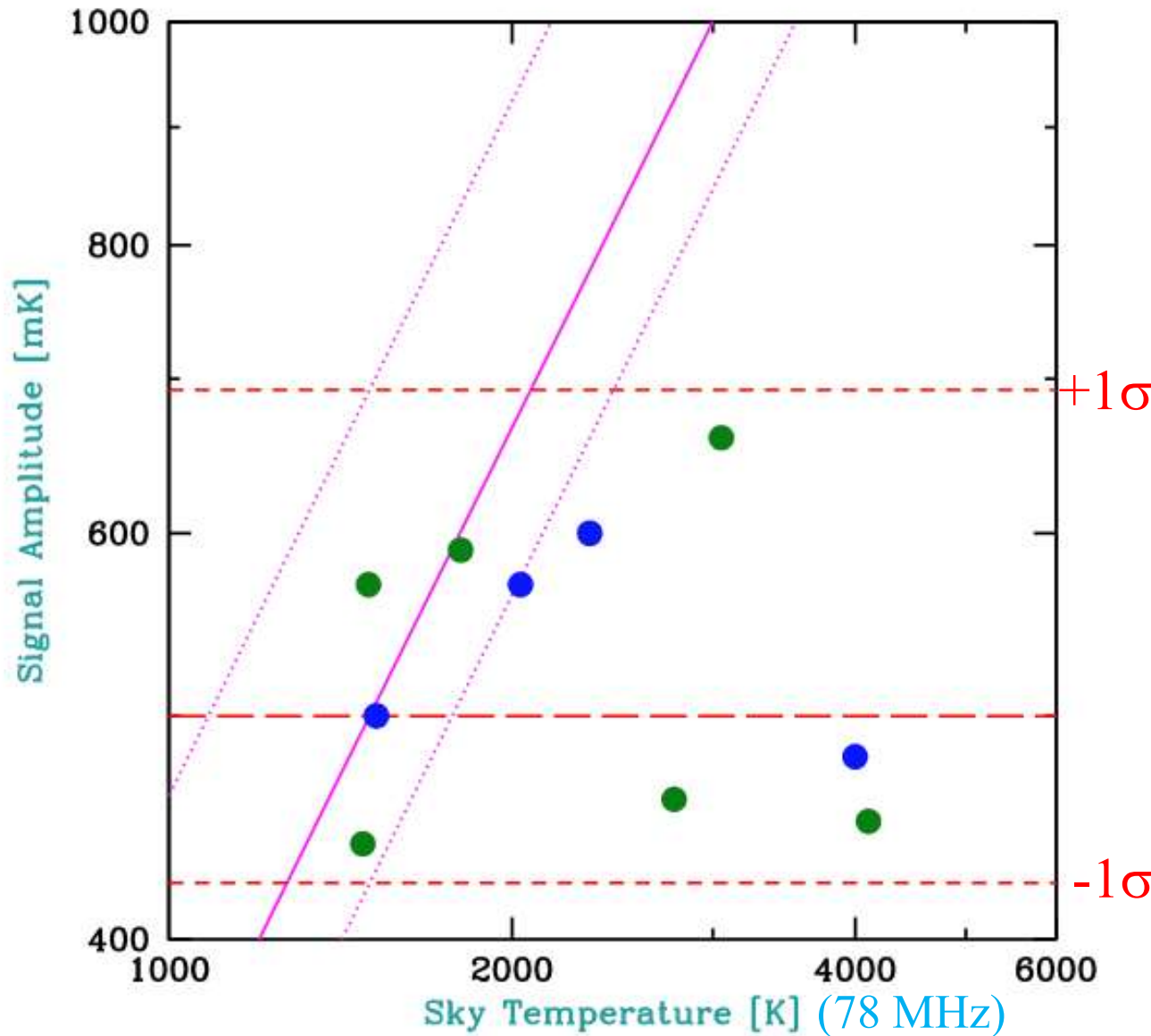


Bowman et al. 2018

EDGES-Low



EDGES-Low

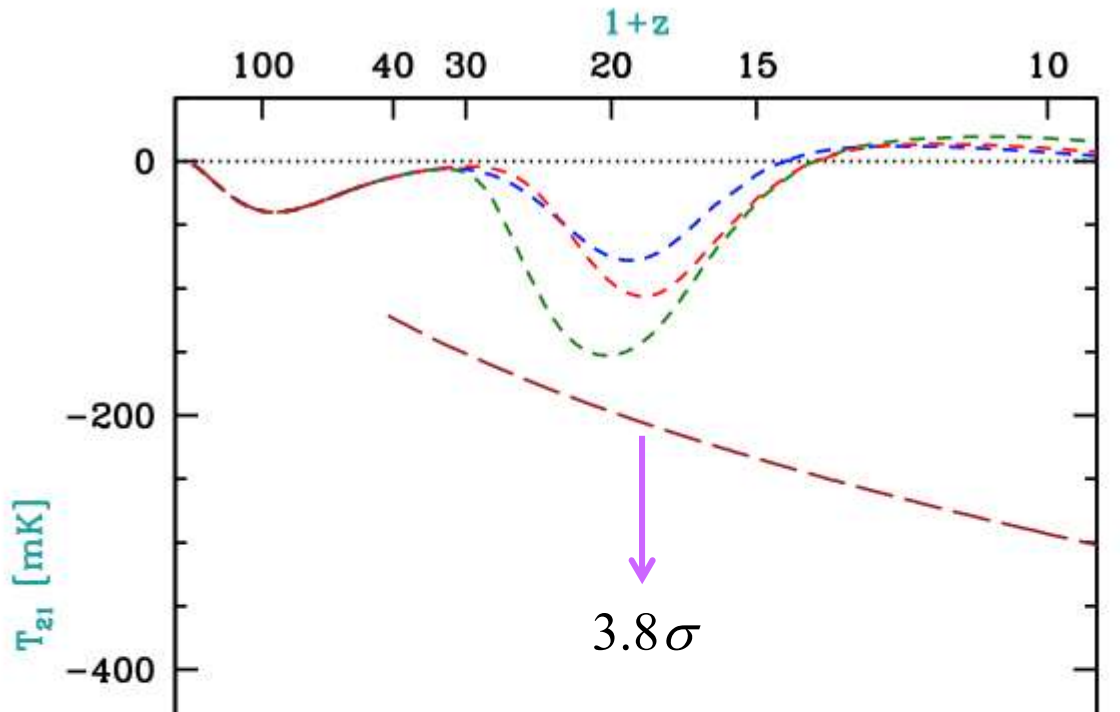


EDGES-Mid

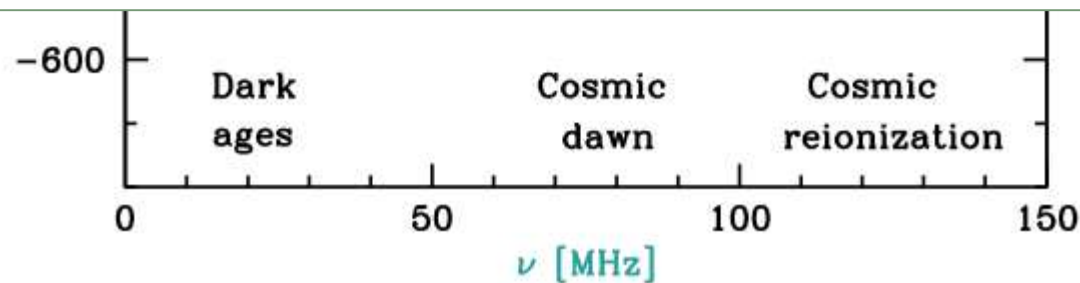
(Nivedita
Mahesh)

Based on:

Bowman et al. 2018



$$T_{21} = 26.8 x_{\text{HI}} \frac{\rho_g}{\bar{\rho}_g} \left(\frac{\Omega_b h}{0.0327} \right) \left(\frac{\Omega_m}{0.307} \right)^{-1/2} \left(\frac{1+z}{10} \right)^{1/2} \left(\frac{T_S - T_{\text{CMB}}}{T_S} \right) \text{ mK}$$



Max absorption:

- No reionization.
- Saturated coupling.
- No heating.

$$\left(\frac{T_S - T_{\text{CMB}}}{T_S}\right)$$

Gas is colder than adiabatic cooling =>

Something cooled it down (heating is easy) =>

X must be even colder (than 5 K at $z=17$) =>

(Cold) dark matter

Dark matter interactions
(Cooling: Dark ages)

Cosmic dawn (WF coupling)



PHYSICAL REVIEW D **89**, 023519 (2014)

Constraining dark matter-baryon scattering with linear cosmology

Cora Dvorkin^{*} and Kfir Blum[†]

*Institute for Advanced Study, School of Natural Sciences,
Einstein Drive, Princeton, New Jersey 08540, USA*

Marc Kamionkowski[‡]

Department of Physics and Astronomy, Johns Hopkins University, Baltimore, Maryland 21218, USA
(Received 22 November 2013; published 27 January 2014)

PHYSICAL REVIEW D **90**, 083522 (2014)

Effects of dark matter-baryon scattering on redshifted 21 cm signals

Hiroyuki Tashiro,¹ Kenji Kadota,² and Joseph Silk^{3,4,5}

PHYSICAL REVIEW D **92**, 083528 (2015)

Heating of baryons due to scattering with dark matter during the dark ages

Julian B. Muñoz, Ely D. Kovetz, and Yacine Ali-Haïmoud

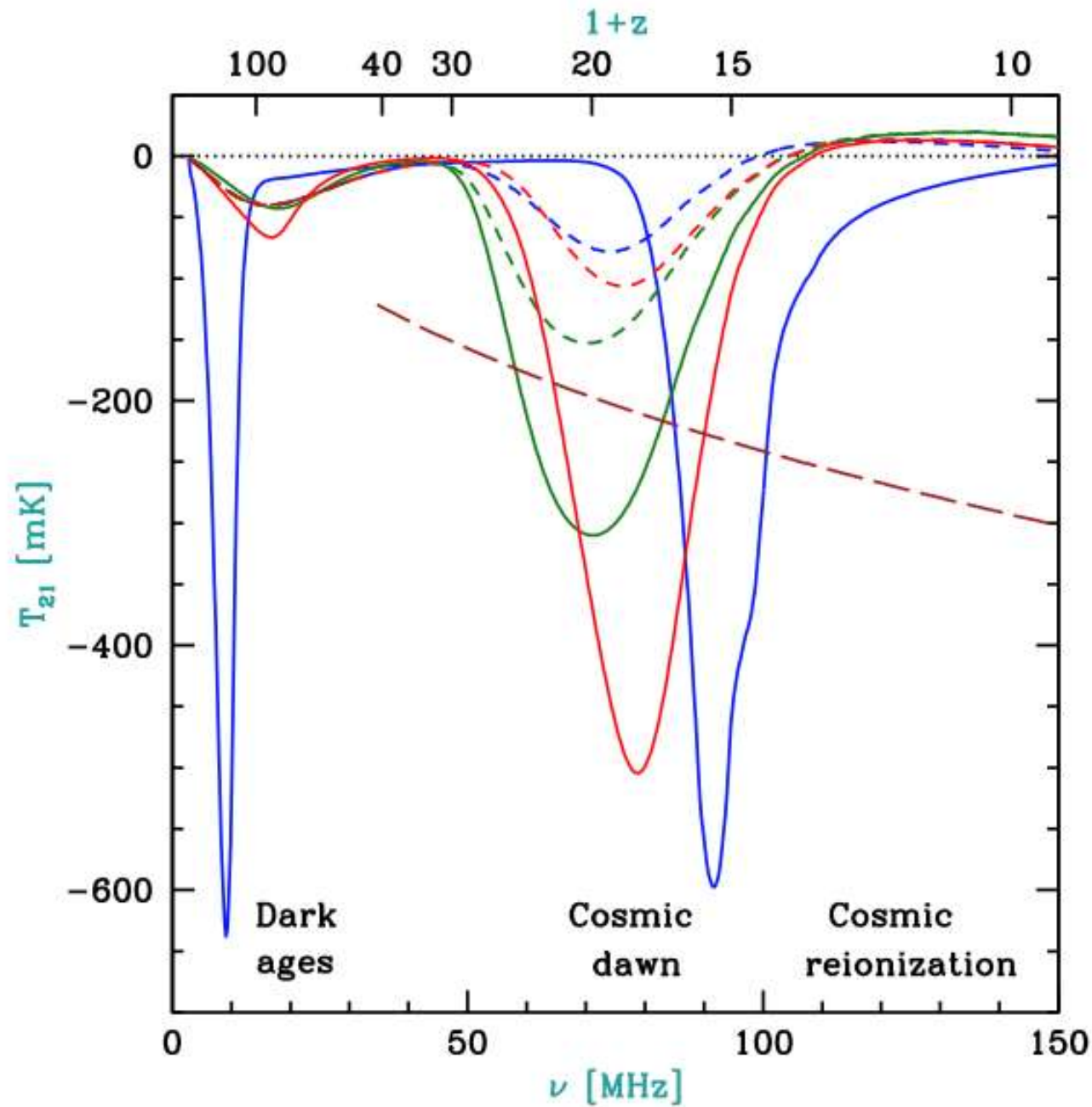
$$\sigma \propto v^n$$

Large at small $v \Rightarrow n=-4$
(Rutherford/Coulomb)

Cosmic dawn: $\min T/v$



The streaming velocity!

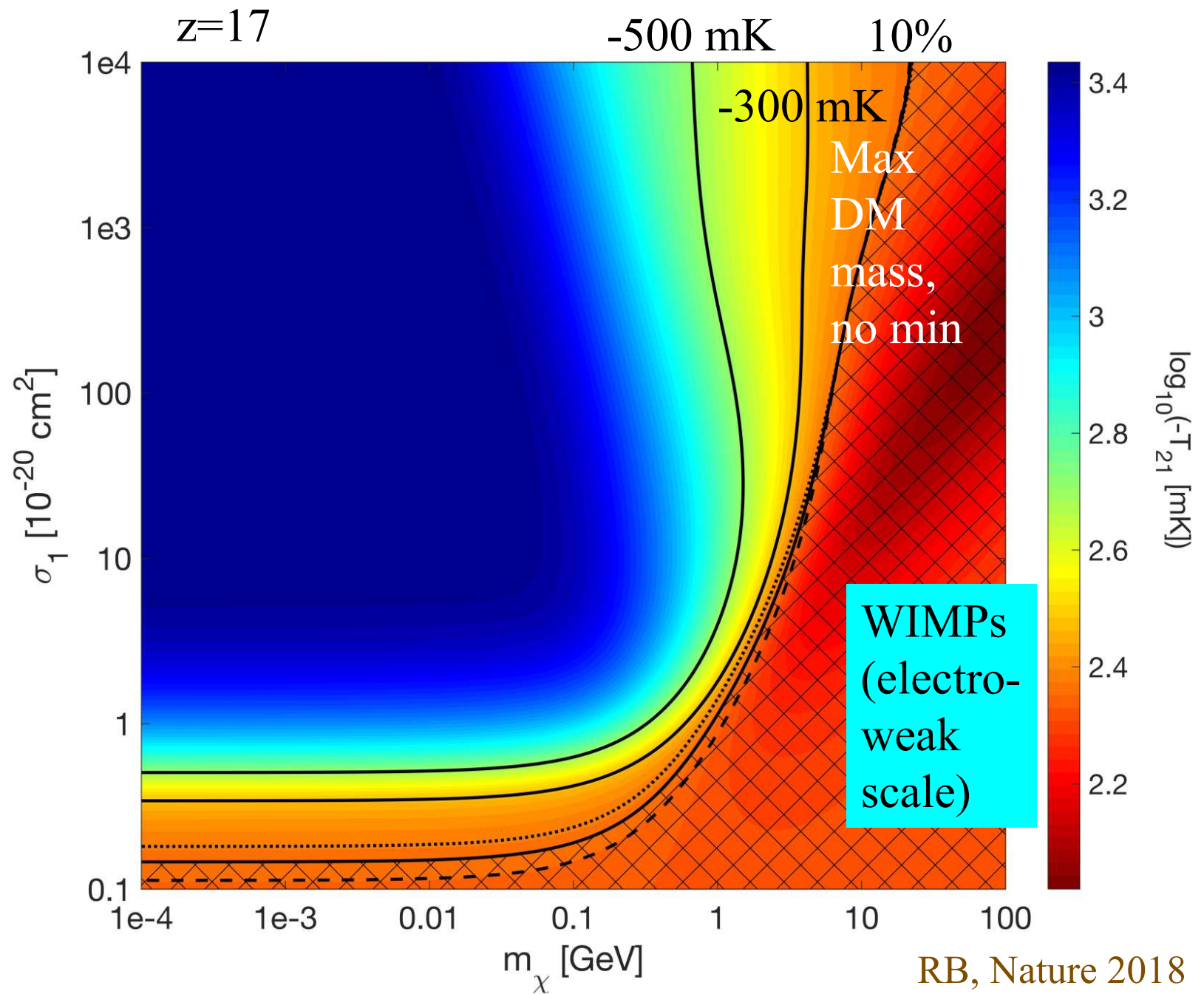


$m_\chi = 0.3$ GeV

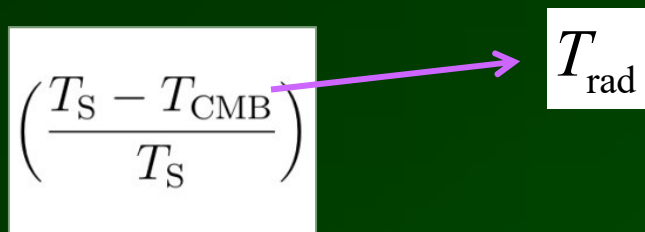
$m_\chi = 3$ GeV

$m_\chi = 0.01$ GeV

RB, Nature 2018



Alternative explanation


$$\left(\frac{T_S - T_{\text{CMB}}}{T_S} \right)$$

$$T_{\text{rad}}$$

Bowman et al. 2018
Feng & Holder 2018

10% of extragalactic radio excess
ARCADE-2: 2006 NASA balloon, 3-90 GHz
Residual with $\nu^{-2.6}$

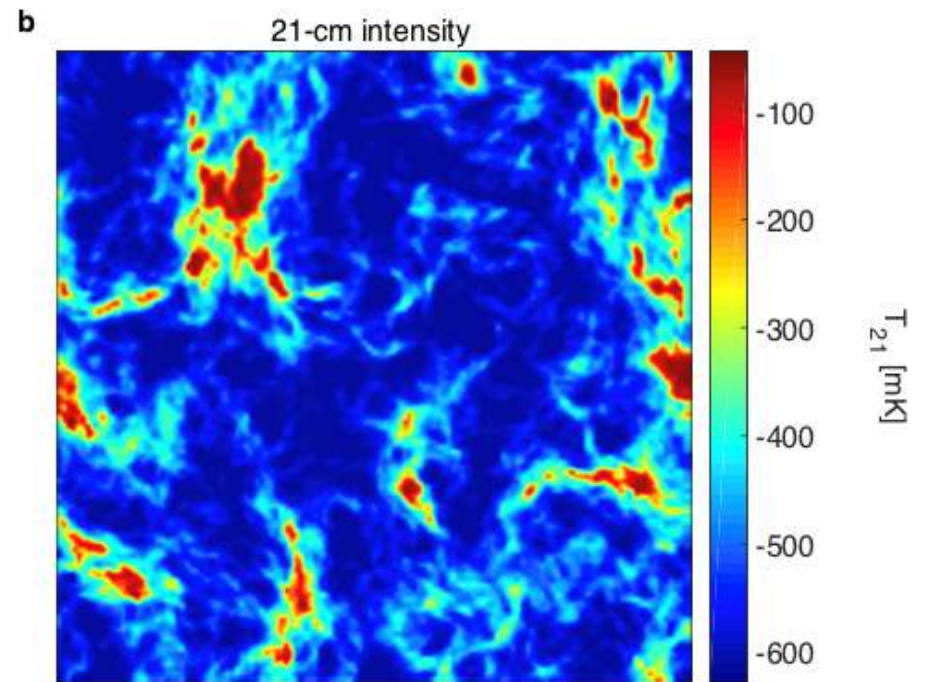
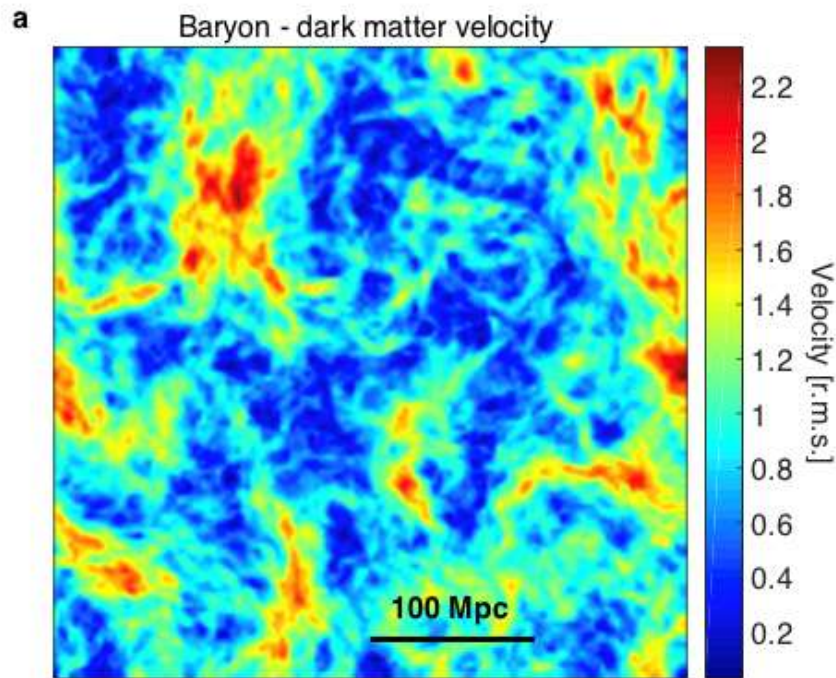
Subrahmanyan & Cowsik 2013

Realistic Galactic modeling => no excess.

Need $z=20$ radio background at MW level, without X-rays.
Mirocha & Furlanetto 2018: $\varepsilon \times 10^3$

RMS fluctuation ~ 140 mK
100 Mpc at $z=17$: $30''$

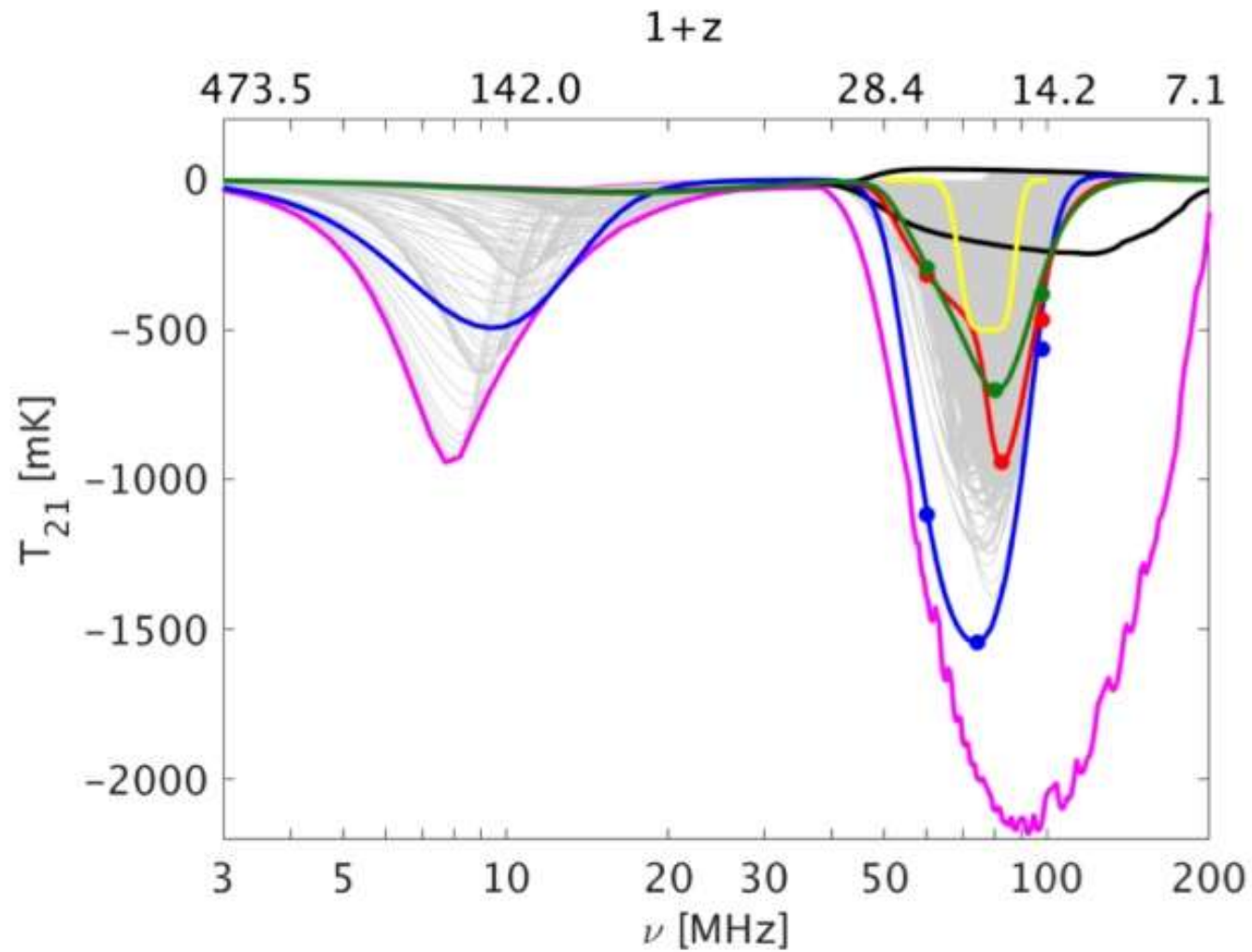
DM cooling fluctuations only



BAOs

RB, Nature 2018

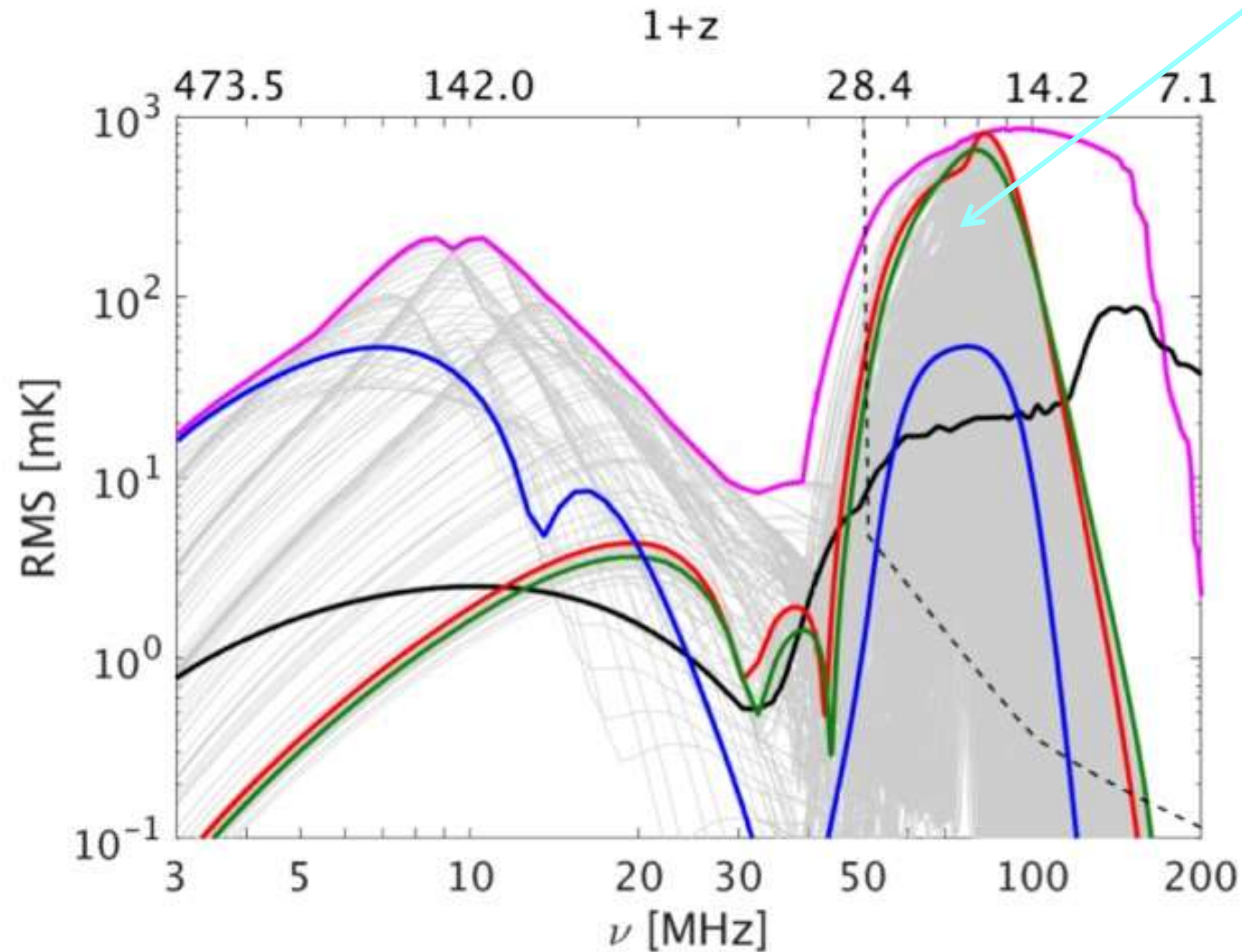
Range (Global)



Fialkov, RB, Cohen, PRL 2018

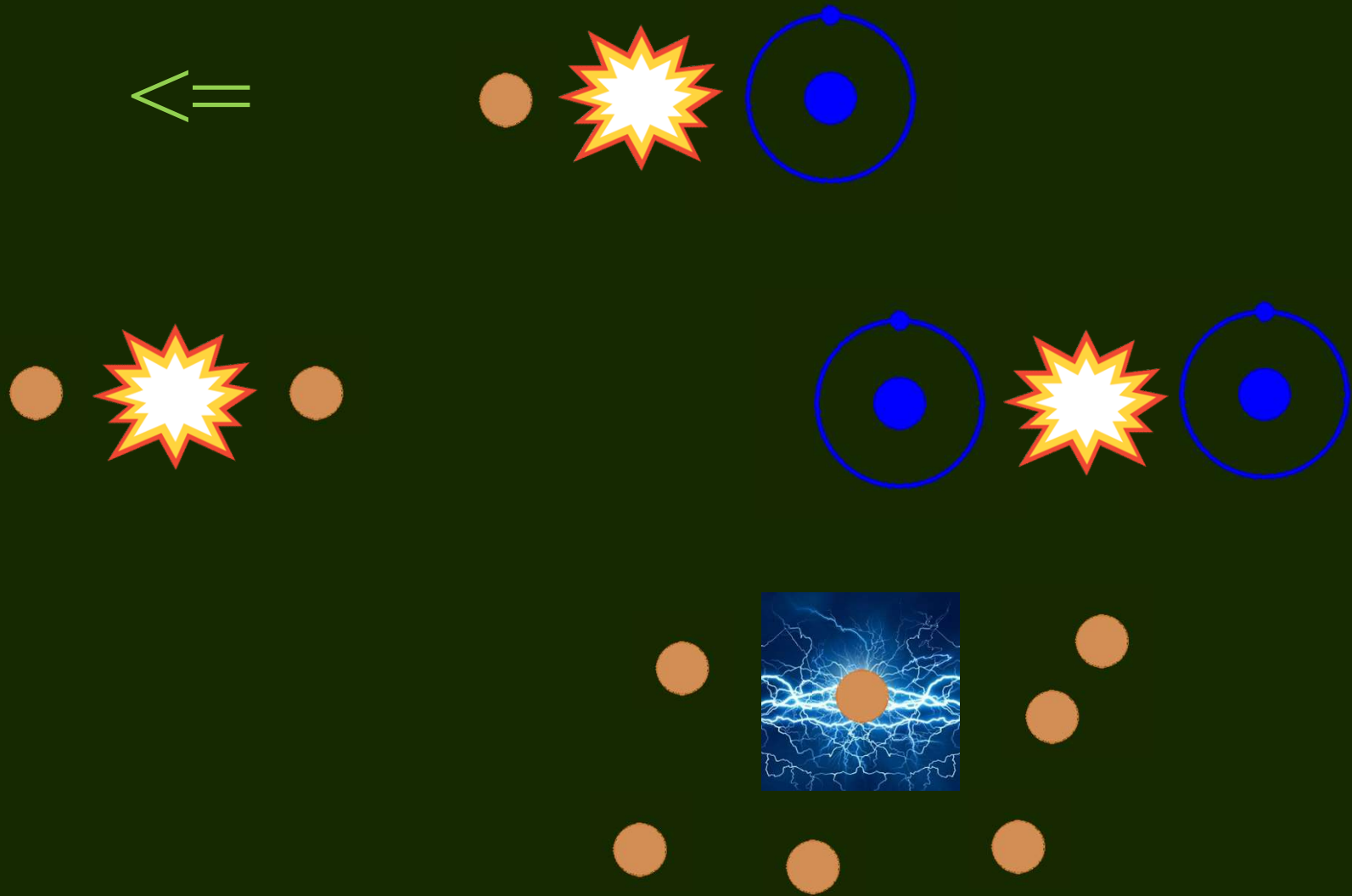
Range (Fluctuation)

ACE
Nenufar

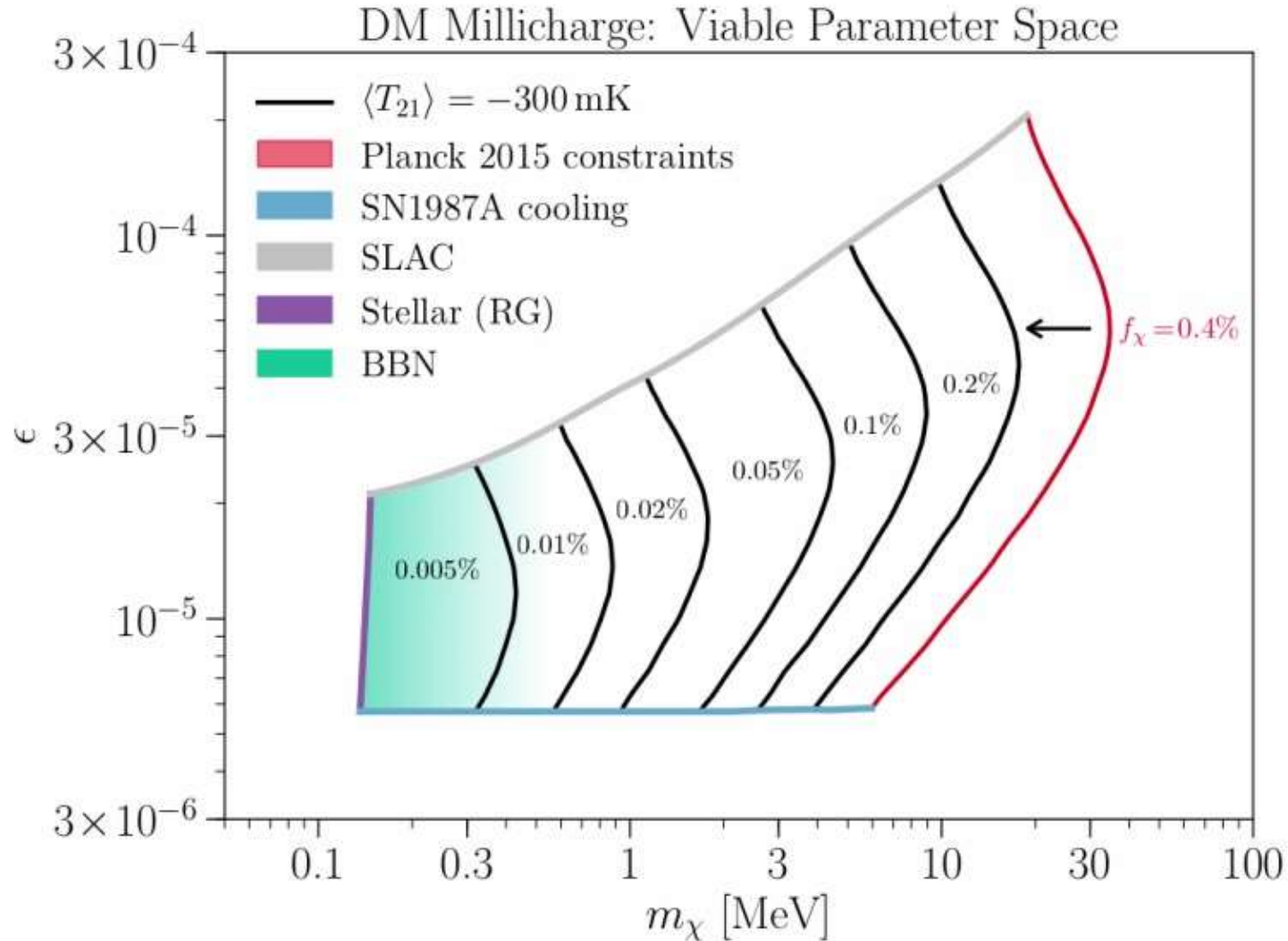


DM cooling
fluctuations
only

Particle physics models



Munoz & Loeb 2018



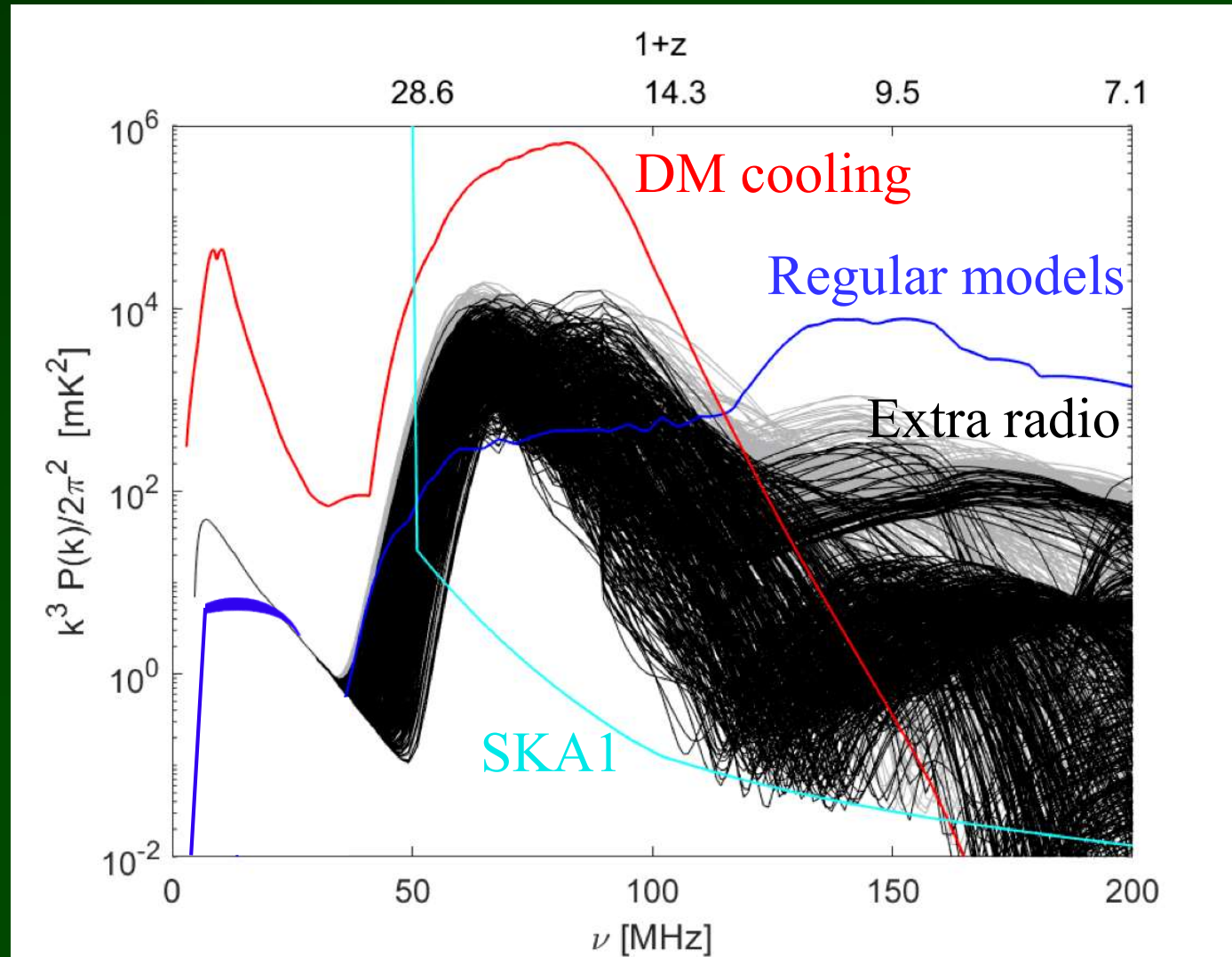
$$\Omega_b h^2 = 0.0224 \pm 0.0001 \quad (\text{Planck 2018})$$

$$\Omega_b h^2 \simeq 0.02170 \pm 0.00026 \quad (\text{BBN})$$

Kovetz, Poulin, Gluscevic, Boddy, RB, Kamionkowski 2018

Alternative explanation

$k=0.1 \text{ Mpc}^{-1}$



Fialkov & RB 2019

Alternative explanation

